



# 60802 Dynamic Time Sync Error – Error Model & Monte Carlo Method Analysis

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November 2021 IEEE 802 Plenary – 802.1 TSN – IEEE/IEC 60802

# Abstract

- Industrial Automation Systems require microsecond-accurate time across long daisy-chains of devices using IEEE Std. 802.1AS™-2020 as specified by IEEE/IEC 60802.
- Simulated protocol and system parameters have thus far either been judged impractical or have failed to meet the time-accuracy requirement.
- An analysis of how errors accumulate suggested that a Monte Carlo method analysis could support fast iteration of potential scenarios and deliver insights into cause and effect.
  - See [60802-McCall-et-al-Time-Sync-Error-Model-0921-v03.pdf](#)
- In this contribution we:
  - Describe a Monte Carlo method analysis programmed in Rstudio
  - Compare the analysis' results to results from previous time series simulations
  - Present a detailed analysis of sensitivities and trade offs
  - Recommend approaches to achieve the stated goals and propose next steps

# Content

- Background & Recap
- Which Errors to Model & How They Add Up
- Monte Carlo Method Analysis Overview (RStudio)
- Comparison with Time Series Simulations
  - 7-Sigma Limit
- Error Analysis
  - Graphical Representation
  - Sensitivities & Trade Offs
- Recommendations & Next Steps

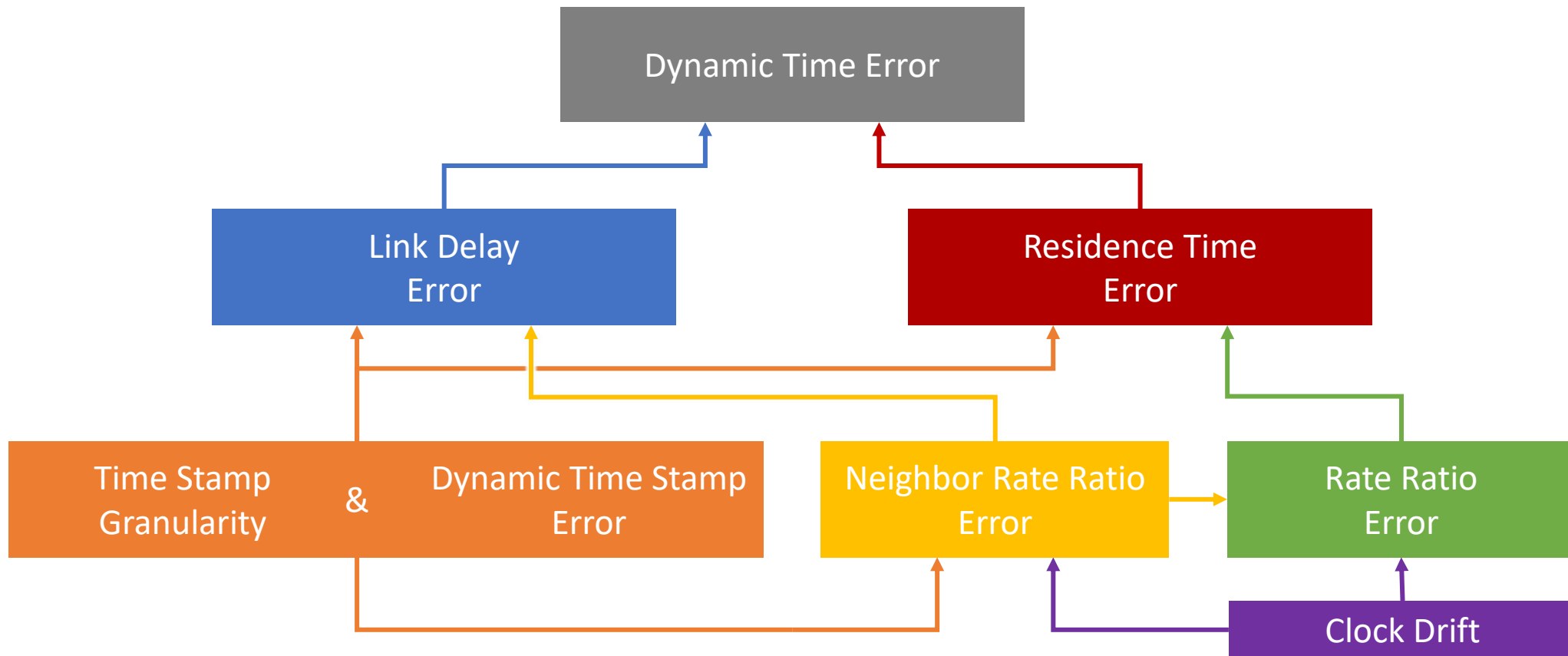
# Background & Recap

# In addition to the abstract...

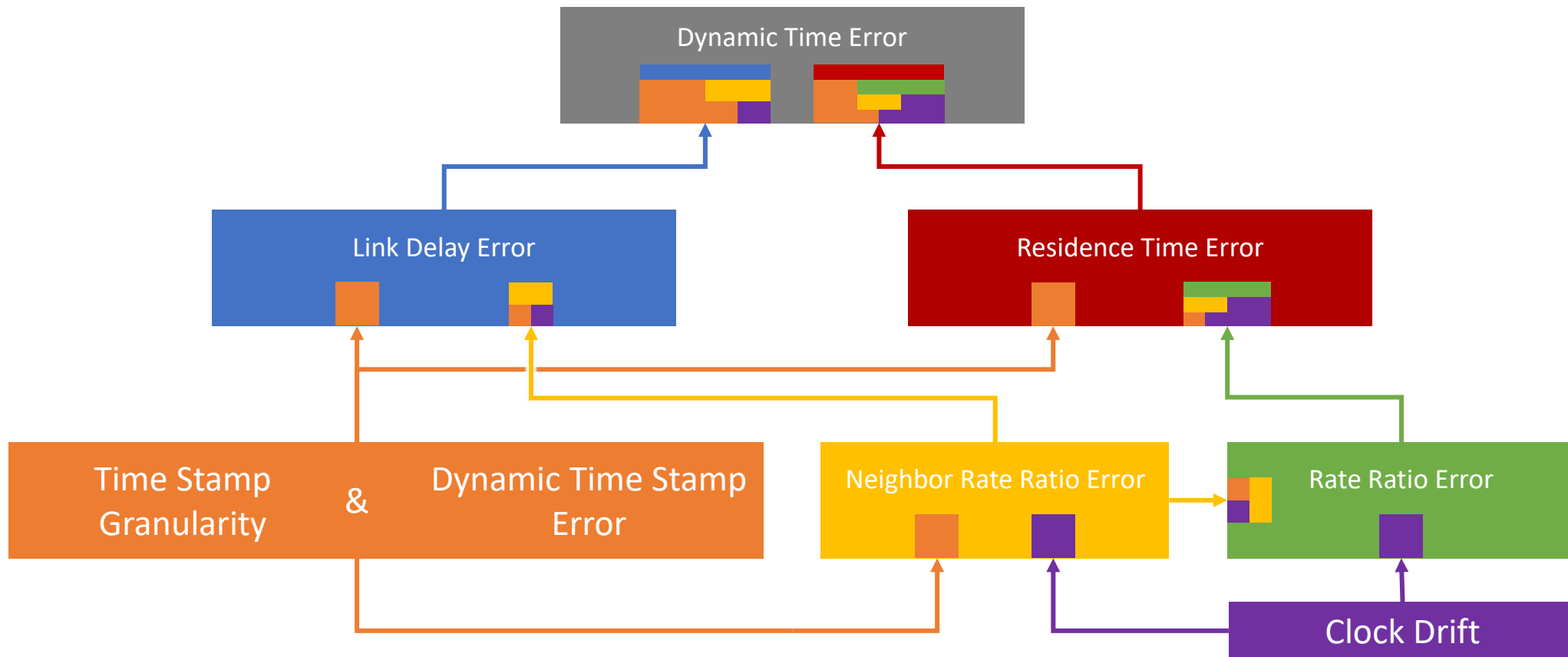
- The Monte Carlo analysis is intended as an addition to the toolbox, not an alternative to Time Series simulation.
- If successful it should provide...
  - The ability to iterate much faster
  - Greater insight into the source of errors and how they accumulate
  - Greater confidence that when selecting parameters to achieve a desired goal
  - Input into future Time Series simulations

# Which Errors to Model & How They Add Up

# Time Sync – Errors to Model



# Time Sync – How Errors Add Up



**All errors in this analysis are caused by either Clock Drift or Timestamp Errors**



# Monte Carlo Method Analysis

Overview of the modelling approach and analysis tool built in RStudio

# Monte Carlo Method Analysis

- Inputs
- Errors, Formulae & Observations
- R & RStudio
  - Script code availability
- Demo

# Input Errors

Error	Distribution	Default Min	Default Max	Equation	Unit
<i>clockDrift<sub>GM</sub></i> ( <i>ClockDrift<sub>GMmin</sub></i> & <i>ClockDrift<sub>GMmax</sub></i> )	Uniform	-0.6	+0.6	$clockDrift_{GM} \sim U(clockDrift_{GMmin}, clockDrift_{GMmax})$	ppm/s
<i>clockDrift</i>	Uniform	-0.6	+0.6	$clockDrift \sim U(-clockDrift, +clockDrift)$	ppm/s
<i>TSGE<sub>TX</sub></i>	Uniform	-4	+4	$TSGE_{TX} \sim U(-TSGE_{TX}, +TSGE_{TX})$	ns
<i>TSGE<sub>RX</sub></i>	Uniform	-4	+4	$TSGE_{RX} \sim U(-TSGE_{RX}, +TSGE_{RX})$	ns
<i>DTSE<sub>TX</sub></i>	Uniform	-2	+2	$DTSE_{TX} \sim U(-DTSE_{TX}, +DTSE_{TX})$	ns
<i>DTSE<sub>RX</sub></i>	Uniform	-1	+1	$DTSE_{RX} \sim U(-DTSE_{RX}, +DTSE_{RX})$	ns

**Formulae below take into account the unit of the input value.  
Formulae in the main section of the September presentation did not.**

# Input Parameters

Error	Default Value	Unit
<i>pDelayInterval</i>	1,000	ms
<i>pDelayTurnaround</i>	10	ms
<i>residenceTime</i>	10	ms

# Input Correction Factor

Error	Default Value	Unit
<i>meanLinkDelay<sub>errorCorrection</sub></i>	0	Value (0-1)
<i>driftRate<sub>errorCorrection</sub></i>	0	Value (0-1)
<i>pDelayRespSync<sub>correction</sub></i>	0	Value (0-1)
<i>mNRRsmoothingN</i>	1	Number (1+)

All formulae in this analysis are ultimately composed of one of these inputs:

Input Errors (**Clock Drift** or **Timestamp Errors**)

Input Parameters

Input Correction Factors

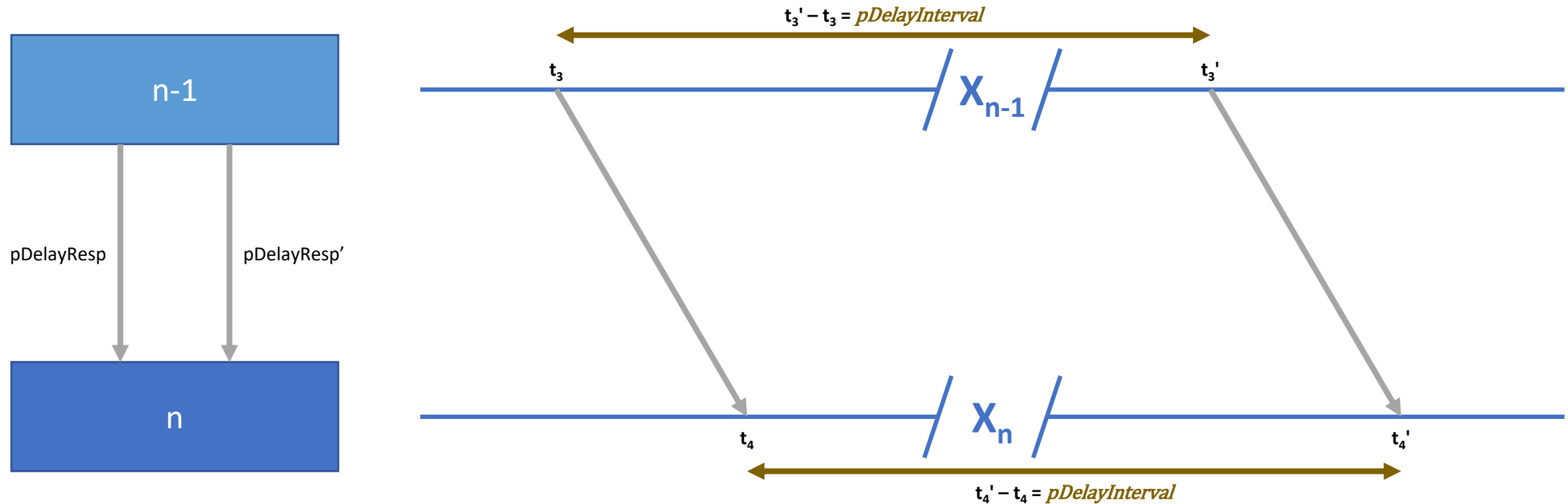
# Input Correction Factors

- This is not a time series analysis, so it's not practical to model the exact mechanism that might be used to implement compensation for errors.
- Three are modelled as an “effectiveness factor”, e.g. a value of 0.75 (75%) means that only 25% of the relevant error will show up in DTE
  - Averaging of Mean Link Delay over time → *meanLinkDelay<sub>errorCorrection</sub>*
  - Measuring and then compensating for Clock Drift → *driftRate<sub>errorCorrection</sub>*
    - See future presentation for potential ways to do this.
  - Averaging of Mean Link Delay over time → *pDelayRespSync<sub>correction</sub>*
- Using timestamps of the N<sup>th</sup> prior pDelayResp messages to reduce *mNRR<sub>error</sub>* is modelled using the *mNRRsmoothingN* factor, which is a whole number with minimum 1.
  - The timestamp of the N<sup>th</sup> pDelayResp message prior to the most recent one is used to calculate mNRR.
    - A value of 1 indicates the 1<sup>st</sup> message prior to the most recent one, i.e. no “smoothing”.
  - See the section on *mNRR<sub>error</sub>* for more detail.

# Error & Error Components – Formatting

Item	Examples using Residence Time	Residence Time errors due to...
Element	<i>residenceTime</i>	
Error in that Element	<i>residenceTime<sub>error</sub></i>	
Component of that error due to another Element	<i>residenceTime<sub>errorTS</sub></i> <i>residenceTime<sub>errorTSdirect</sub></i> <i>residenceTime<sub>errorCD</sub></i> <i>residenceTime<sub>errorRR</sub></i>	All Timestamp Errors Direct Timestamp Errors All Clock Drift Errors Rate Ratio Errors
Next level down... Component of a component	<i>residenceTime<sub>errorRR_TS</sub></i> <i>residenceTime<sub>errorRR_CDdirect</sub></i> <i>residenceTime<sub>errorRR_NRR</sub></i>	All Timestamp components of Rate Ratio Errors Direct Clock Drift component of Rate Ratio Errors NRR error component of Rate Ratio Errors
Next level down... Component of a component of a component	<i>residenceTime<sub>errorRR_NRR_TS</sub></i> <i>residenceTime<sub>errorRR_NRR_CD</sub></i>	Timestamp component of NRR via Rate Ratio Errors Clock Drift component of NRR via Rate Ratio Errors

# Measured Neighbor Rate Ratio (mNRR)



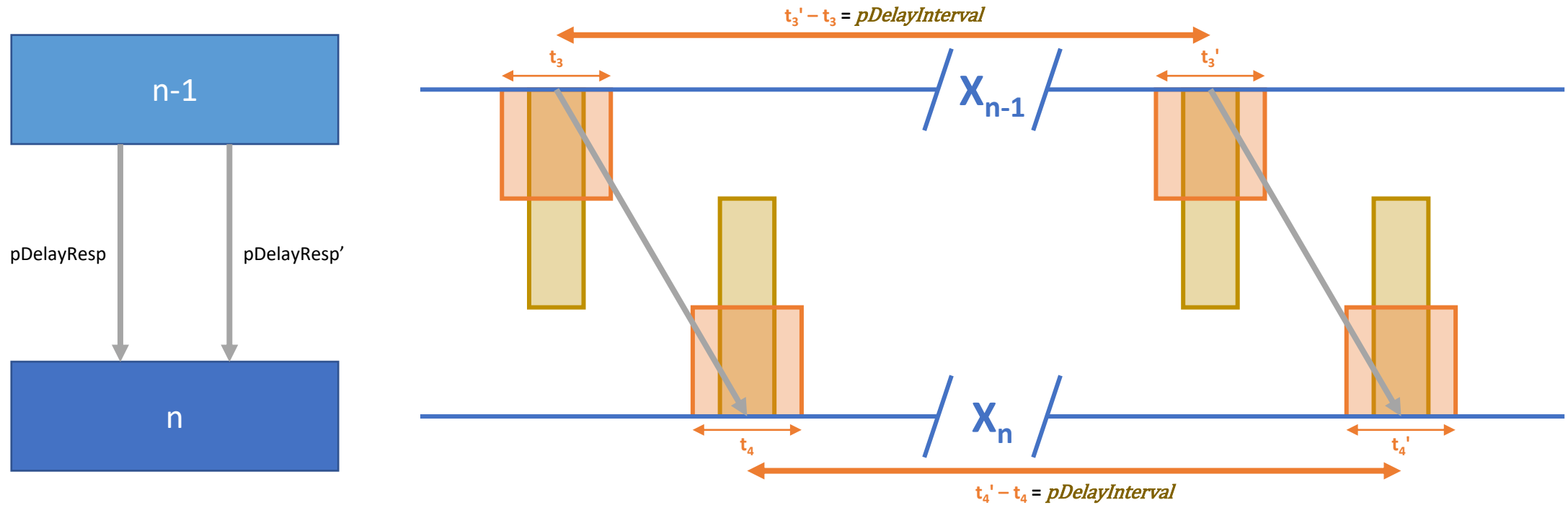
$$mNRR = \left( \frac{(t_4' - t_4)}{(t_3' - t_3)} \right)$$

$$mNRR_{error} = mNRR_{errorTS} + mNRR_{errorCD}$$

ppm



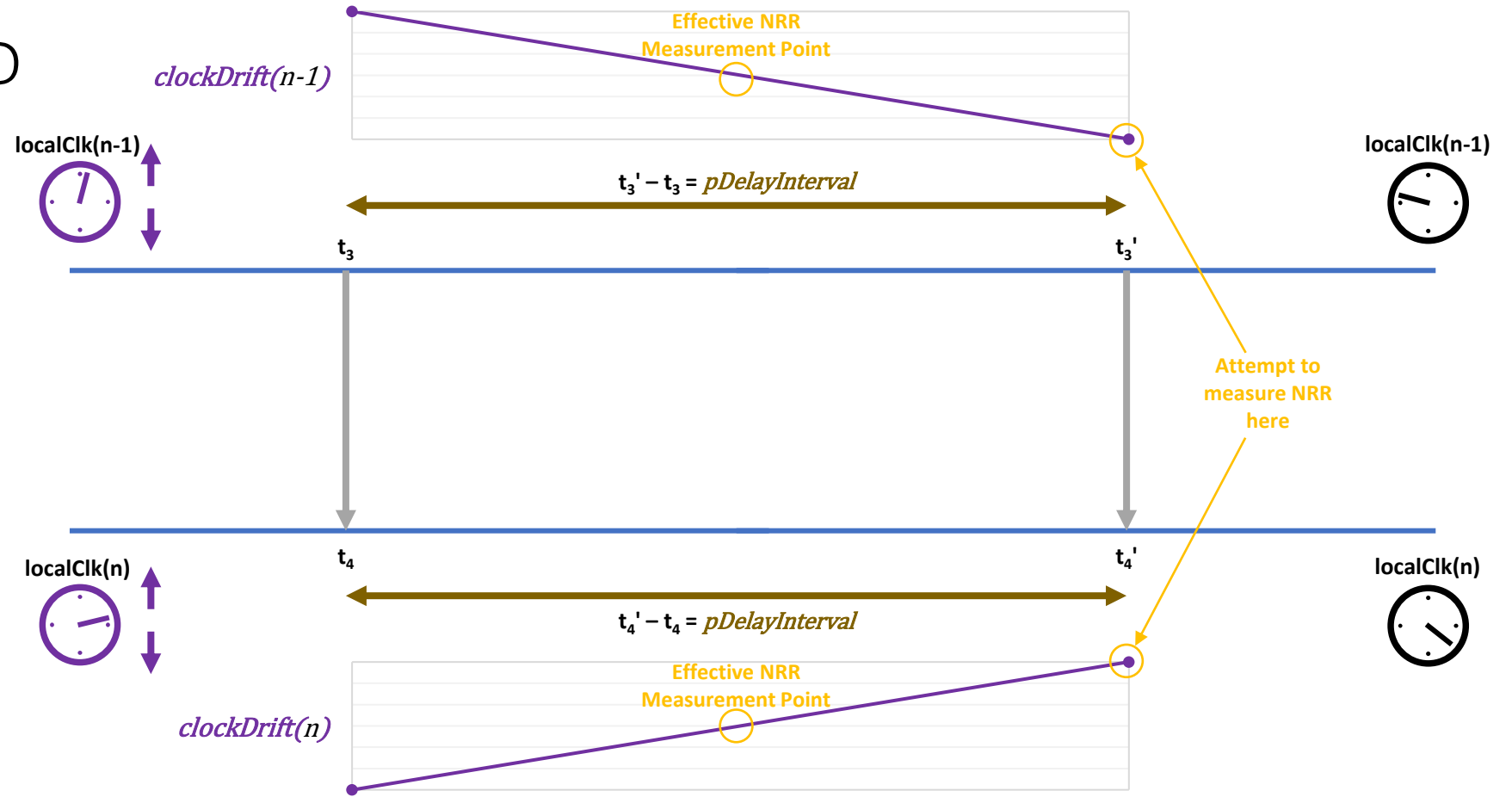
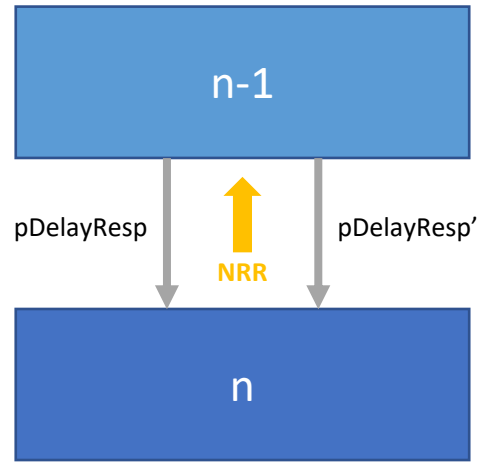
# mNRR<sub>errorTS</sub>



$$mNRR_{errorTS} = \left( \frac{(t_{4PDerror} - t_{4PDerrorPrevious}) - (t_{3PDerror} - t_{3PDerrorPrevious})}{pDelayInterval \times mNRRsmoothingN} \right)$$

ppm

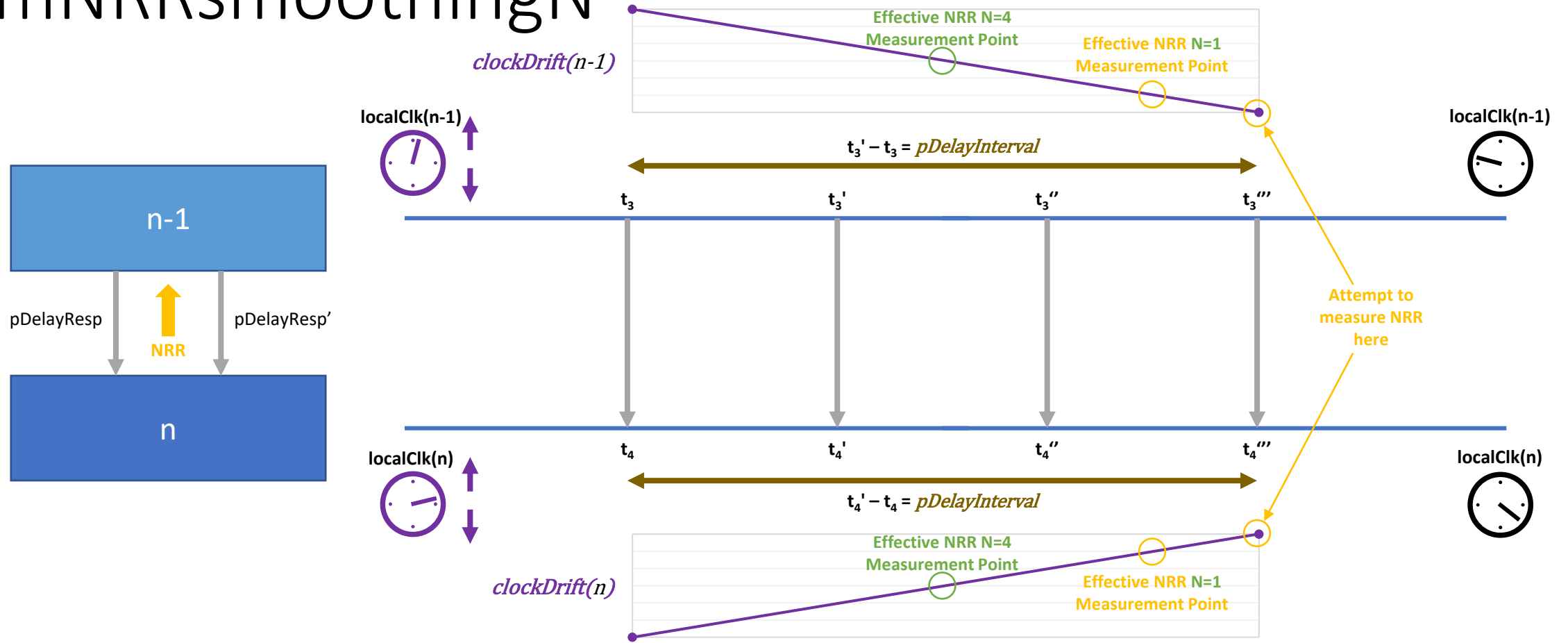
# mNRR<sub>errorCD</sub>



$$mNRR_{errorDrift}(n) = (1 - driftRate_{errorCorrection}) \times mNRR_{smoothingN} \times \left( \frac{pDelayInterval}{2 \times 10^3} \right) (clockDrift(n-1) - clockDrift(n))$$

ppm

# mNRRsmoothingN



$$mNRR_{errorDrift}(n) = (1 - driftRate_{errorCorrection}) \times mNRRsmoothingN \times \left( \frac{pDelayInterval}{2 \times 10^3} \right) (clockDrift(n-1) - clockDrift(n))$$

ppm

# Formulae – $mNRR_{error}$

$$mNRR_{error} = mNRR_{errorCD} + mNRR_{errorTS}$$

ppm

$$mNRR_{errorCD}(n) = (1 - \mathit{driftRate}_{errorCorrection}) \times mNRR_{smoothingN} \times \left( \frac{\mathit{pDelayInterval}}{2 \times 10^3} \right) (\mathit{clockDrift}(n-1) - \mathit{clockDrift}(n))$$

ppm

$$mNRR_{errorTS} = \left( \frac{(t_{4PDerror} - t_{4PDerrorPrevious}) - (t_{3PDerror} - t_{3PDerrorPrevious})}{\mathit{pDelayInterval} \times mNRR_{smoothingN}} \right)$$

ppm

$$t_{3PDerrorPrevious} = \mathit{TSGE}_{TX} + \mathit{DTSE}_{TX}$$

$$t_{4PDerrorPrevious} = \mathit{TSGE}_{RX} + \mathit{DTSE}_{RX}$$

ns

The factors  $t_{3PDerror}$  and  $t_{4PDerror}$  are the same as in the  $\mathit{pDelay}_{error}$  calculation.  
(Same value. No need for new random numbers, as the same  $\mathit{pDelayResp}$  message is used to measure NRR.)

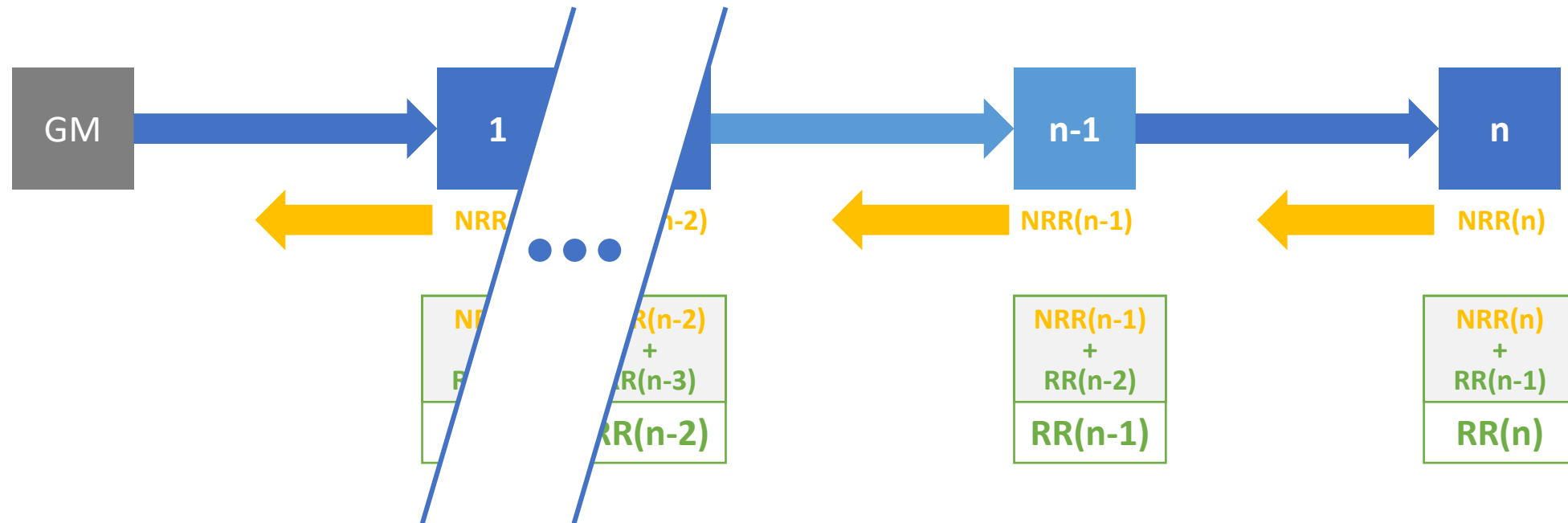
# Observations of $mNRR_{error}$ Behaviour

- Errors in mNRR do not accumulate along the chain of nodes
- An mNRR error due to clock drift at one node will tend to be reversed at the next node.

$$mNRR_{errorCD}(n) = \left( \frac{pDelayInterval}{2 \times 10^3} \right) (\text{clockDrift}(n-1) - \text{clockDrift}(n)) \quad mNRR_{errorCD}(n+1) = \left( \frac{pDelayInterval}{2 \times 10^3} \right) (\text{clockDrift}(n) - \text{clockDrift}(n+1))$$

- This does not apply for mNRR errors due to clock drift at the GM
- mNRR errors due to Timestamp errors are independent of each other. DTE errors at one node due to this component will not tend to be reversed at the next node.
- mNRR errors due to clock drift are modelled as a combination of two uniform distributions (clock drifts at n and n-1) and will have a simple probability distribution
  - Errors due to Timestamp errors are modelled as combinations of eight uniform distributions and will be more complex.

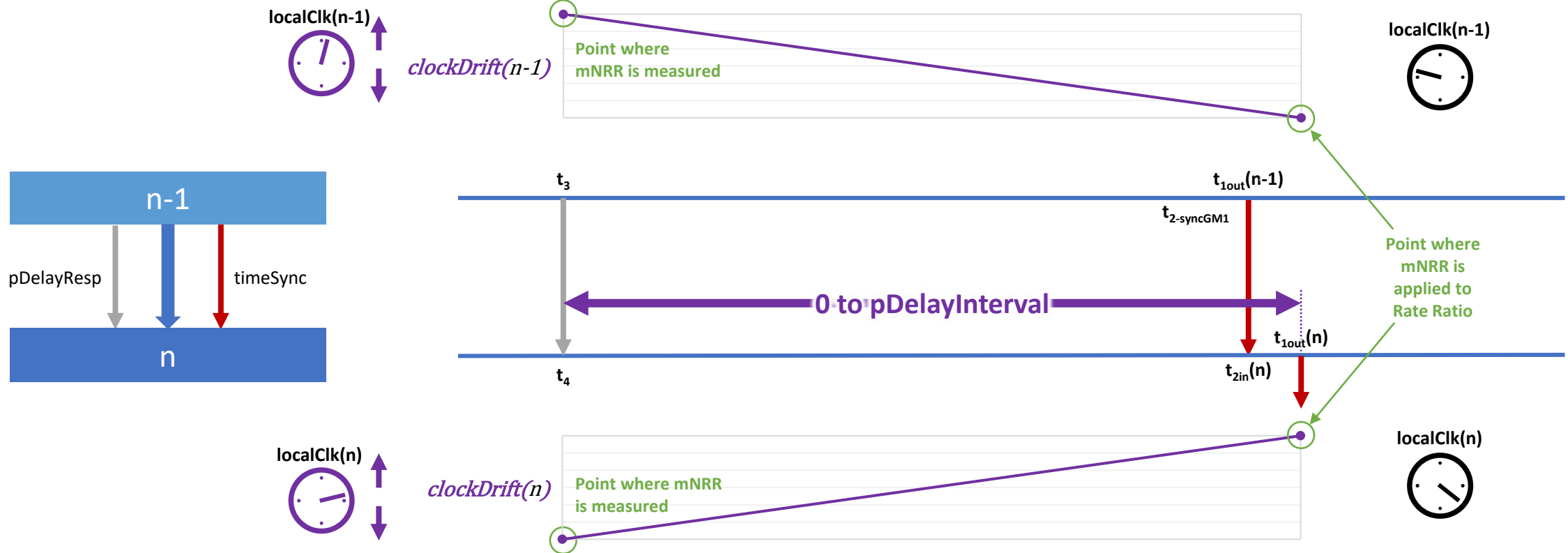
# Rate Ratio Error ( $RR_{error}$ )



$$RR(n) = RR(n - 1) + mNRR(n)$$

$$RR_{error}(n) = RR_{error}(n - 1) + mNRR_{error}(n) + RR_{errorCD}(n)$$

# $RR_{errorCD}$



$$RR_{errorCD}(n) = (1 - driftRate_{errorCorrection}) \times \frac{delay_{mNRR\_Sync}}{10^3} (clockDrift(n-1) - clockDrift(n))$$

ppm

# Formulae – $RR_{error}$

$$RR_{error}(n) = RR_{error}(n - 1) + mNRR_{error}(n) + RR_{errorCD}(n) \quad \text{ppm}$$

$$RR_{errorCD}(n) = (1 - \text{driftRate}_{errorCorrection}) \times \frac{\text{delay}_{mNRR\_Sync}}{10^3} (\text{clockDrift}(n - 1) - \text{clockDrift}(n)) \quad \text{ppm}$$

$$\text{delay}_{mNRR\_Sync} \sim U(0, (1 - \text{pDelayRespSync}_{correction}) \text{pDelayInterval}) \quad \text{ms}$$

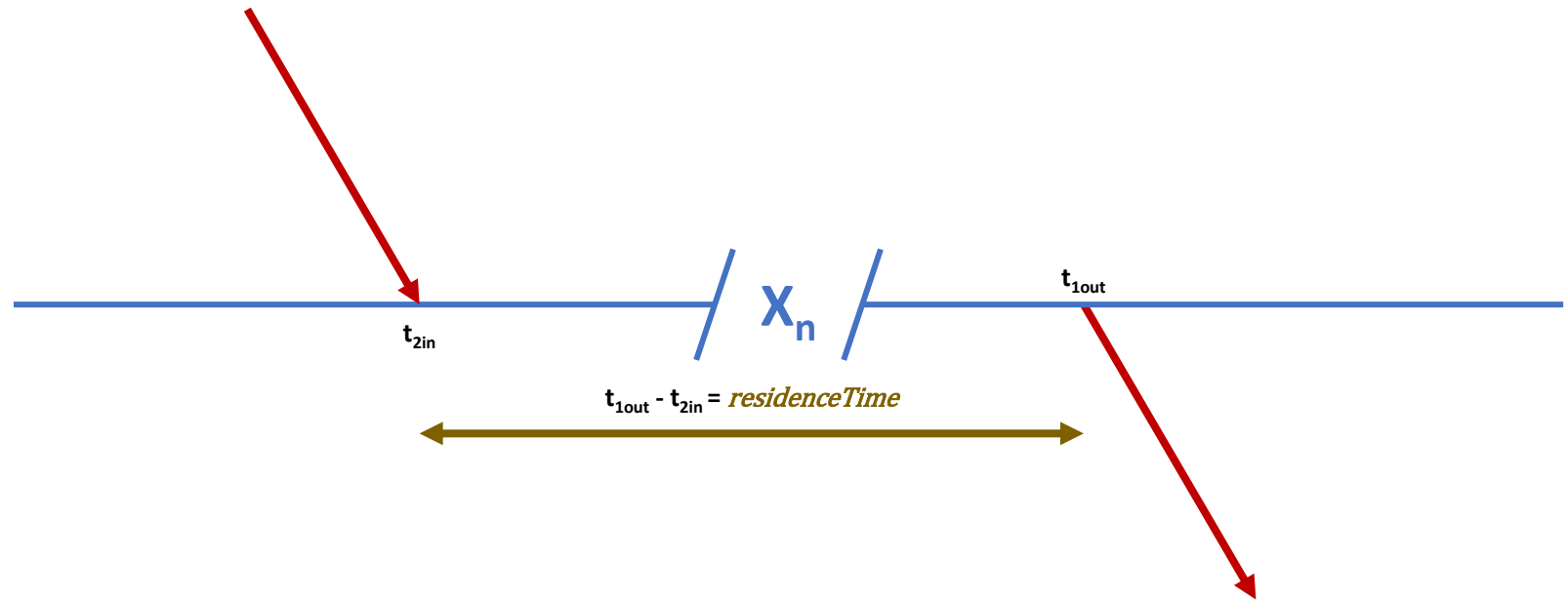
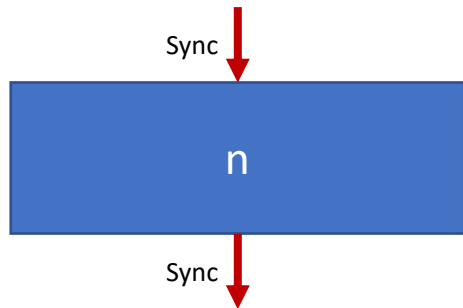
**Does not include any effect of changing clock drift (ppm/s<sup>2</sup>) during Residence Time. See speaker notes in  $RR_{error}$  section for details.**



# Observations of $RR_{error}$ Behaviour

- $mNRR_{error}$  feeds directly into  $RR_{error}$  where the errors accumulate
  - Since  $mNRR_{error}$  due to clock drift ( $mNRR_{errorCD}$ ) at one node tends to reverse at the next node, the component of  $RR_{error}$  due to this ( $RR_{errormNRR\_CD}$ ) will tend not to increase along a chain of devices.
    - This does not apply for error due to GM clock drift as it only appears in  $mNRR_{error}$  at the first hop.
  - $mNRR_{error}$  due to timestamp errors are much less likely to cancel out so  $RR_{error}$  from this source is more likely to increase along a chain of devices.
- $RR_{error}$  due to clock drift during the delay between measurement of NRR and when it is applied to Rate Ratio ( $RR_{errorCD}$ ) could cancel out from one node to the next...but only if the delay at one node is the same as at the next...which is unlikely.
  - $RR_{errorCD}$  is therefore much more likely to increase along a chain of devices than the clock drift component of  $mNRR_{error}$
- $RR_{error}$  due to clock drift can be reduced by decreasing  $pDelayInterval$  which reduces the maximum possible  $delay_{mNRRSync}$ 
  - Similar effect if pDelay messaging can be aligned to occur just before Sync message; modelled using  $pDelayRespSync_{correction}$
  - Note: see earlier in this presentation for the effect reducing  $pDelayInterval$  has on  $mNRR_{error}$

# Residence Time Error ( $residenceTime_{error}$ )



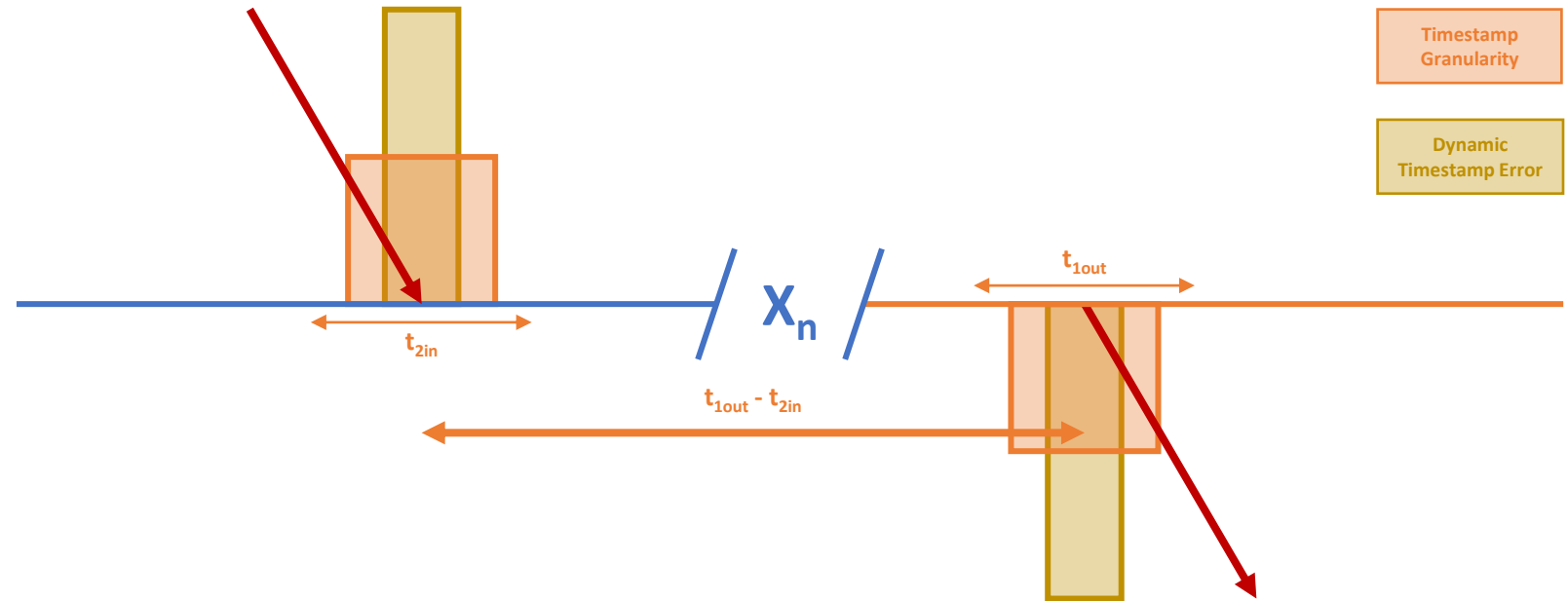
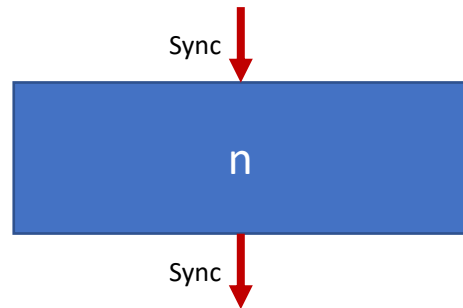
$$residenceTime = RR(t_{1out} - t_{2in})$$

ns

$$residenceTime_{error} = residenceTime_{errorTS} + residenceTime_{errorRR}$$

ns

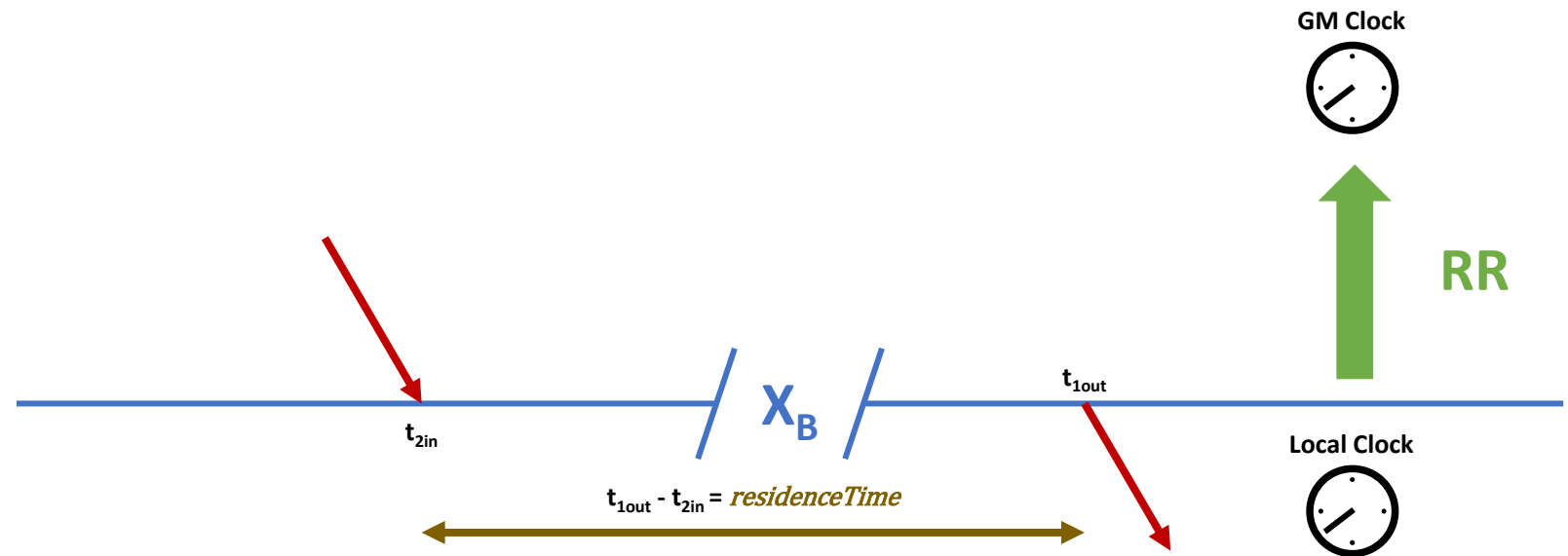
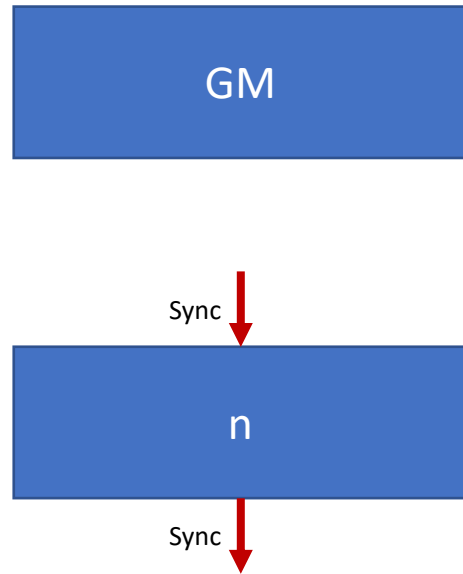
# RT<sub>errorTS</sub>



$$residenceTime_{errorTS} = t_{1Error} - t_{2Error}$$

**ns**

# residenceTime<sub>errorRR</sub>



$$residenceTime_{errorRR} = \frac{RR_{error}}{10^6} (\mathit{residenceTime} \times 10^6)$$

ns

$$= RR_{error} \times \mathit{residenceTime}$$

ns

# Formulae – residenceTime<sub>error</sub>

$$residenceTime_{error} = residenceTime_{errorTS} + residenceTime_{errorRR} \quad \text{ns}$$

$$residenceTime_{errorTS} = t_{1Error} - t_{2Error} \quad \text{ns}$$

$$t_{2Error} = TSGE_{RX} + DTSE_{RX} \quad t_{1Error} = TSGE_{TX} + DTSE_{TX} \quad \text{ns}$$

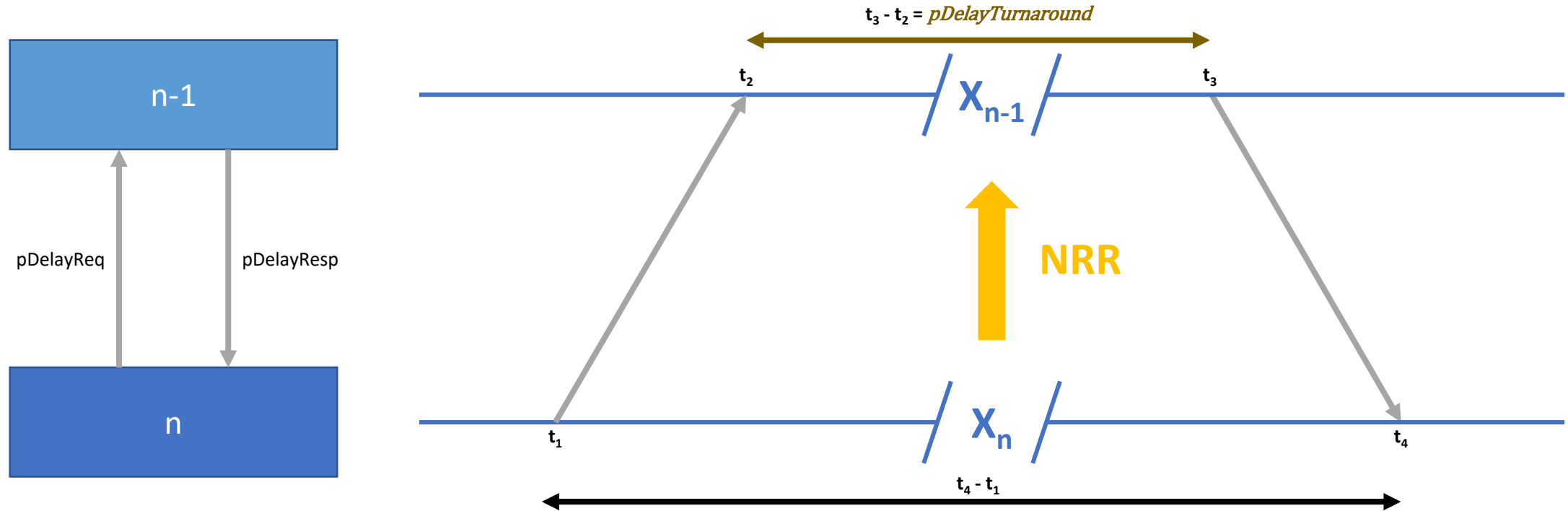
$$residenceTime_{errorRR} = \frac{RR_{error}}{10^6} (\mathbf{residenceTime} \times 10^6 + residenceTime_{errorTS}) \quad \text{ns}$$

$$= RR_{error} \times \left( \mathbf{residenceTime} + \frac{residenceTime_{errorTS}}{10^6} \right) \quad \text{ns}$$

# Observations of $\text{residenceTime}_{\text{error}}$ Behaviour

- $\text{residenceTime}_{\text{error}}$  due to timestamp error is independent of Residence Time.
  - Reducing Residence Time will have no effect on this source of error.
- $\text{residenceTime}_{\text{error}}$  due to  $\text{RR}_{\text{error}}$  is proportional to Residence Time
  - Reducing Residence Time can reduce this source of error.
- Since larger  $\text{RR}_{\text{error}}$  is more likely further along a chain of devices, the amount of Residence Time Error at each node is also likely to increase.
  - For example: the component of DTE due to Residence Time Error after 100 hops is more likely to be larger from errors in nodes 51-100 than from nodes 1-50.

# meanLinkDelay



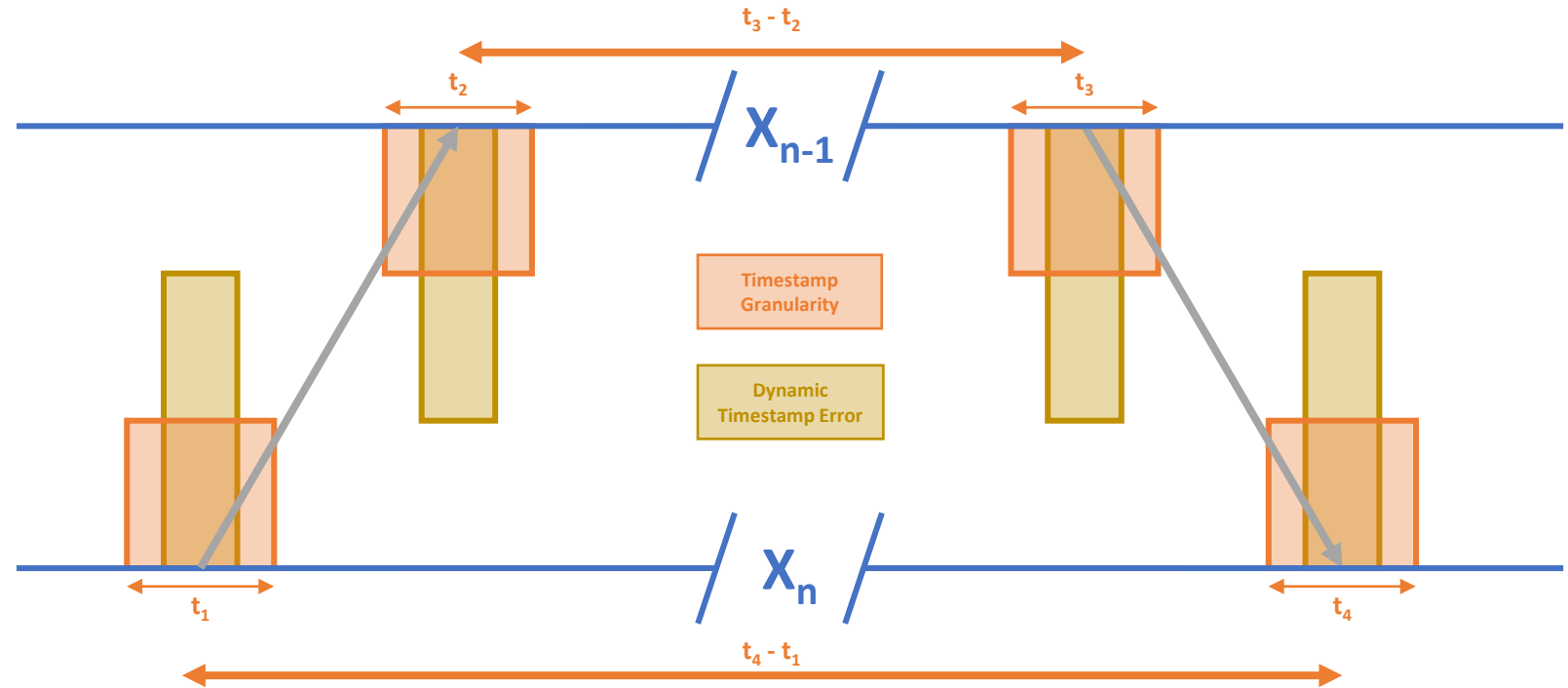
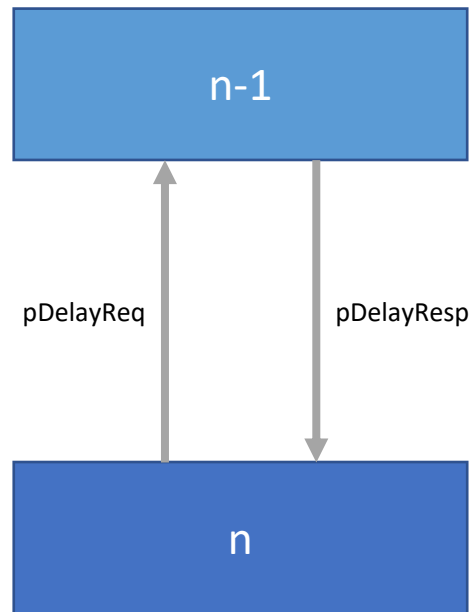
$$meanLinkDelay = RR \left( \frac{(t_4 - t_1) - NRR(t_3 - t_2)}{2} \right)$$

ns

$$meanLinkDelay_{error} = (1 - meanLinkDelay_{errorCorrection})(pDelay_{errorTS} + pDelay_{errorNRR} + pDelay_{errorRR})$$

ns

# pDelay<sub>errorTS</sub>

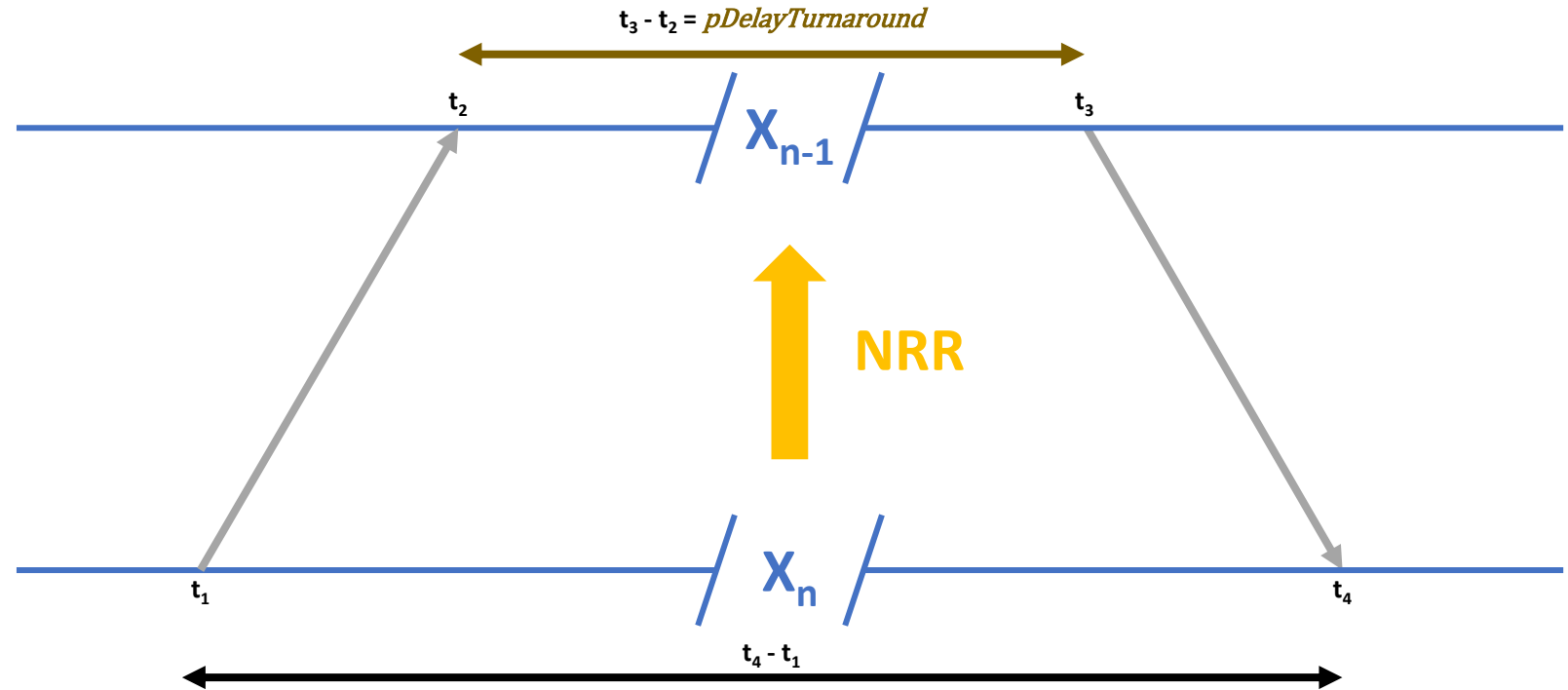
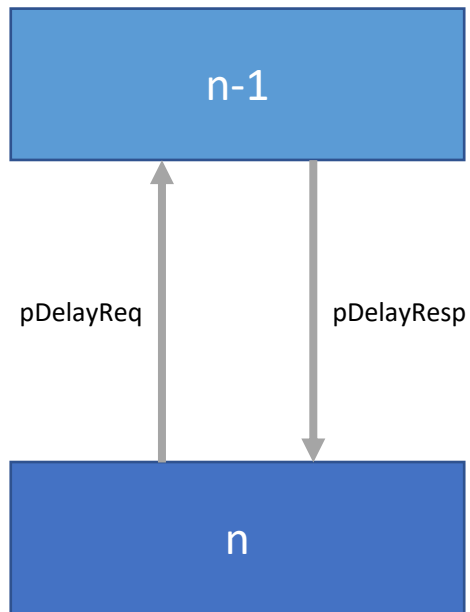


$$pDelay_{errorTS} = \frac{(t_{4PDerror} - t_{1PDerror}) - (t_{3PDerror} - t_{2PDerror})}{2}$$

ns



# pDelay<sub>errorNRR</sub>



$$pDelay_{errorNRR} = mNRR_{error} \left( \frac{pDelayTurnaround}{2} \right)$$

ns

# Formulae – meanLinkDelay<sub>error</sub>

$$\text{meanLinkDelay}_{\text{error}} = (1 - \text{meanLinkDelay}_{\text{errorCorrection}})(p\text{Delay}_{\text{errorTS}} + p\text{Delay}_{\text{errorNRR}} + p\text{Delay}_{\text{errorRR}}) \quad \text{ns}$$

$$p\text{Delay}_{\text{errorTS}} = \frac{(t_{4PD\text{Error}} - t_{1PD\text{Error}}) - (t_{3PD\text{Error}} - t_{2PD\text{Error}})}{2} \quad \text{ns}$$

$$t_{1PD\text{Error}} = \text{TSGE}_{\text{TX}} + \text{DTSE}_{\text{TX}} \quad t_{2PD\text{Error}} = \text{TSGE}_{\text{RX}} + \text{DTSE}_{\text{RX}} \quad \text{ns}$$

$$t_{3PD\text{Error}} = \text{TSGE}_{\text{TX}} + \text{DTSE}_{\text{TX}} \quad t_{4PD\text{Error}} = \text{TSGE}_{\text{RX}} + \text{DTSE}_{\text{RX}} \quad \text{ns}$$

$$p\text{Delay}_{\text{errorNRR}} = \frac{m\text{NRR}_{\text{error}}}{10^6} \left( \frac{p\text{DelayTurnaround} \times 10^6}{2} \right) \quad \text{ns}$$

$$= m\text{NRR}_{\text{error}} \left( \frac{p\text{DelayTurnaround}}{2} \right) \quad \text{ns}$$

$$p\text{Delay}_{\text{errorRR}} = \frac{\text{RR}_{\text{error}}}{10^6} (p\text{Delay} + (1 - p\text{Delay}_{\text{errorCorrection}})(p\text{Delay}_{\text{errorTS}} + p\text{Delay}_{\text{errorNRR}})) \quad \text{ns}$$

# Observations of $\text{meanLinkDelay}_{\text{error}}$ Behaviour

- $\text{meanLinkDelay}_{\text{error}}$  due to timestamp error is independent of  $\text{pDelayTurnaround}$ .
  - Reducing  $\text{pDelayTurnaround}$  will have no effect on this source of error.
- $\text{meanLinkDelay}_{\text{error}}$  due to  $\text{mNRR}_{\text{error}}$  is proportional to  $\text{pDelayTurnaround}$ 
  - Reducing  $\text{pDelayTurnaround}$  can reduce this source of error.
- The actual Link Delay is not a significant source of error
  - Only needs to be included as part of  $\text{pDelay}_{\text{errorRR}}$ ...which is small enough to ignore for the purposes of this analysis

# Formulae – Top Level

$$DTE(x) = \sum_{n=1}^x (\text{meanLinkDelay}_{error}(n) + \text{residenceTime}_{error}(n)) \quad \text{ns}$$

$$\text{meanLinkDelay}_{error} = (1 - \text{meanLinkDelay}_{errorCorrection}) (\text{pDelay}_{errorTS} + \text{pDelay}_{errorNRR} + \text{pDelay}_{errorRR}) \quad \text{ns}$$

$$\text{residenceTime}_{error} = \text{residenceTime}_{errorTS} + \text{residenceTime}_{errorRR} \quad \text{ns}$$

**The current analysis does not include factors shown in grey.  
x is number of hops.**

# Special Cases

$$\mathit{clockDrift}(0) = \mathit{clockDrift}_{GM}$$

For the first hop ( $n = 1$ ),  $n - 1 = 0$ , i.e. the first device in chain, which is the GM.

$$\mathit{residenceTime}_{error}(x) = 0$$

For the last hop ( $n = x$ ), the Sync message is not passed on so there is no Residence Time Error.

# Analysis Carried Out Using r & RStudio

- **r** is available here: <https://www.r-project.org/>
  - Open source license: [various](#), but mostly GNU GPL v2 and GPL v3
- **RStudio** is available here: <https://www.rstudio.com/products/rstudio/download/>
  - Open source license: [GNU Affero GPL v3](#)
- Model uses `write.csv` and `write.table` functions, which are part of R.Utils package
  - Install in RStudio by typing...  
`install.packages("R.utils")`  
...in the console window.

# Reasons for Choosing r & RStudio

- Powerful tools for building the model then carrying out statistical analysis of the results.
  - Example: Q-Q plot to determine if dataset has a normal distribution with a single command.
- Simple scripting language.
- Easy to generate many charts to visualise the results
- Can also output results to a file for further analysis and graphing.
  - Used to generate visualisation of how errors accumulate.

# Availability of Analysis Script

- Intention is to make the script code available under an open source license
  - Probably [BSD 3-Clause](#)
  - Other licenses are an option; feedback welcome.
  - Timing TBD. Target is before the end of the year.
- Current plan is to simply make the script code available, not to set up an open source project (e.g. GitHub)
  - If someone wants to make this an open source project it isn't a problem, we just don't have the resources to commit to doing it properly.



# RStudio

## Environment Variables

## Script

The screenshot displays the RStudio interface with four main components highlighted by red arrows:

- Script Editor:** Shows a script titled "IEEE 802.1AS Time Sync Error Model & Monte Carlo Analysis". It includes a header with author information (David McCall, Intel Corporation) and a table of input variables and their descriptions.
- Environment Pane:** Lists various objects created in the environment, including summary statistics (e.g., RErrorTS\_MEAN, RErrorTS\_SIGMA) and large numeric vectors (e.g., RErrorTS\_SUM, RErrorTSdirect\_MAXabs).
- Console:** Shows the execution of an R script. The output includes a list of input variables and their values, followed by a table of summary statistics for the error model results.
- Plots:** A plot titled "Dynamic Time Error at hop 100" showing a probability density function. The x-axis is labeled "ns" and ranges from -4000 to 4000. The y-axis is labeled "Probability Density" and ranges from 0e+00 to 4e-04. The plot shows a bell-shaped curve centered at 0. Below the plot, summary statistics are provided: "At hop 100 minDTE\_SUM = -4140 maxDTE\_SUM = 3810".

## Console

## Plots

# RStudio Script Code Summary

- Configuration (Output? Hops? Runs? More charts? Seed value?)
- Inputs (see above)
- Initialize tracking vectors (all represented as a vector – a one dimensional array – of length “hops”)
- Hop 1
  - For all runs. Each Error Input, Error Element and Component is represented as a vector of length “runs”.
  - Calculate main values that contribute to DTE
    - First hop, so  $\text{hop}(n-1)$  is  $\text{hop}(0)$  i.e. the Grand Master
  - Also calculate values of error components for analysis
  - Calculate MAXabs, MEAN and SIGMA for all error elements & components and record in tracking vectors.
- Loop: Hops 2+
  - For all runs, one hop at a time.
  - Mostly the same as Hop 1, but errors accumulate where appropriate.
    - No Residence Time for the last hop
  - Data from previous hops, other than Clock Drift, is not maintained, but tracking vectors record key information (MAXabs, MEAN and SIGMA for all error elements & components).
- Plot Charts

# Demo

Lenovo Thinkpad T480

Intel(R) Core(TM) i5-8350U CPU @ 1.70GHz 1.90 GHz

16GB RAM

(While running Webex & background corporate apps)

# Results

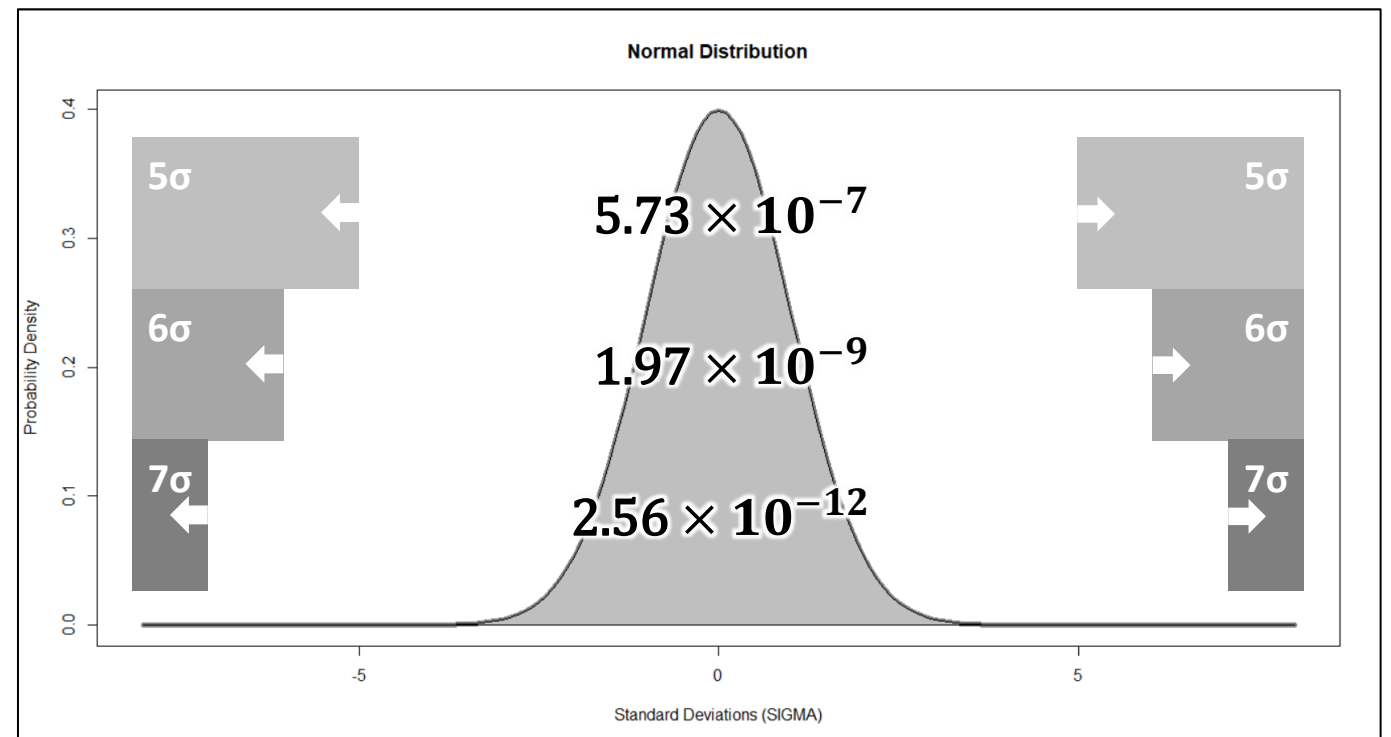
- Monte Carlo analysis of errors allows for many “runs” in very little time.
  - 100hops & 100,000 executes in <30 seconds
  - Calculating hops takes <15 seconds; rest of time spent generating plots
  - Add approx. 10 seconds to generate additional detailed plots if desired
- Next step: determine if the results are useful.
  - Compare to previous Time Series Simulation

# Comparison with Time Series Simulations

# Values to Compare Against Time Series $\max |DTE|$

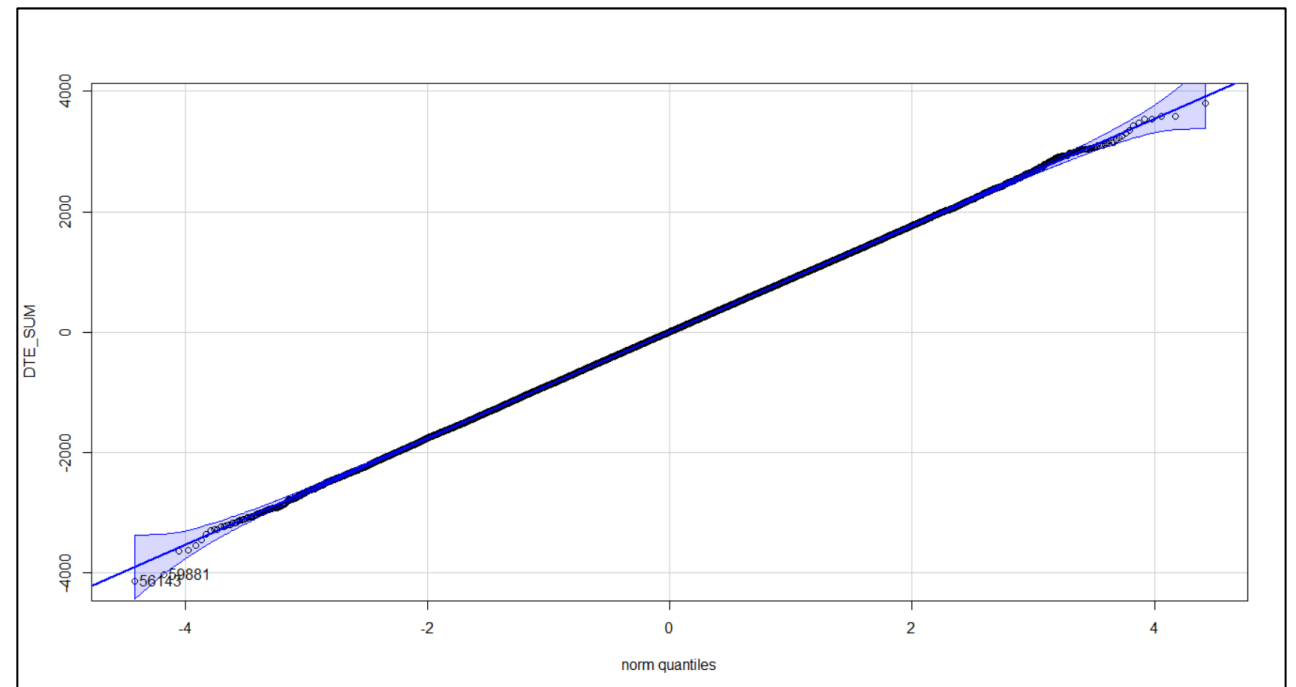
- Maximum Absolute Value of Dynamic Time Error ( **$\max |DTE|$** )
- A multiple of SIGMA ( $\sigma$ ) for DTE at hop 100, based on probability of exceeding it...\*

\* Only valid if data forms a normal (Gaussian) distribution



# Dynamic Time Error – Normal Distribution?

- Use of SIGMA to calculate probability of exceeding a value is only valid if the data forms a normal distribution.
- Quantile-Quantile Plot of DTE at hop 100 (100,000 runs)
  - 802.1AS default parameters
  - Clock Drift:  $\pm 0.6$  ppm/s
  - TSGE & DTSE:  $\pm 4$ ns
  - Data should lie along a straight line (with some variance at extremes expected)
- Result: **YES**, data forms normal distribution.



# Which SIGMA?

- Probability of **|DTE| > ?-SIGMA** over a period of time?

125ms Sync Interval	
8	per second
480	per minute
28,800	per hour
691,200	per day
252,460,800	per year

? x SIGMA	Average Time Before Exceeding
5 $\sigma$	2.5 days
6 $\sigma$	2 years
7 $\sigma$	1,548 years

- Conclusion: use 7 $\sigma$ 
  - Revisit if we can't achieve goals using 7 $\sigma$
  - Lower multiple (6 $\sigma$ ?) would be appropriate for constant time error
  - Lower multiple for dynamic time error might be justified due to combination with constant time error



# Enough runs for measurement of SIGMA?

- Increasing number of runs; track max|DTE| and  $7\sigma$ 
  - Same seed value...but structure of model means first 100 runs when analysing 1,000 runs are not the same as when analysing 100 runs.

Runs	max DTE  (ns)	$7\sigma$ of DTE (ns at hop 100)
100	2,400	6,230
1,000	3,710	6,380
10,000	3,610	6,100
100,000	4,140	6,190
1,000,000	4,380	6,190

- 100,000 runs is a good compromise between speed and accuracy
  - Give up very little in terms of accuracy & runs in

# Custom Script to Match Time Series Simulation

- The Time Series Simulation includes two factors that must be specifically modelled differently than the main model.
- Dynamic Time Error is +8ns or -8ns with 50% probability of either.
  - 50% chance of either extreme is not realistic. Not recommended for main model.
- mNRR is determined by calculating NRR using most recent and  $N^{\text{th}}$  prior pDelayResponse messages (included in the main model via mNRRsmoothingN) **and then** taking median value of previous N calculations (not included in the main model).
  - N is an odd number; values of 11 and 7 have been used.
  - Assuming clocks drift linearly, this will result in the  $\left(\frac{N+1}{2}\right)^{\text{th}}$  previous value being used; e.g. if N=11, 6<sup>th</sup> previous value.
    - This results in an additional clock drift between effective measurement and mNRR of  $\left(\frac{N+1}{2} - 1\right) = \left(\frac{N-1}{2}\right)$ , i.e. if 6<sup>th</sup> previous value is used, the effective measurement point is pushed back by 5x pDelayInterval.
  - This has no effect on  $mNRR_{\text{errorTS}}$  as there is no averaging, but increases  $mNRR_{\text{errorCD}}$  by an additional factor of N-1 (as original mNRR smoothing is an effective delay of  $pDelayInterval/2$  and  $\left(\frac{N-1}{2}\right) \times 2 = N - 1$ .
    - Modelled by changing the effect of mNRRsmoothingN on mNRRerrorCD from...
      - \* mNRRsmoothingN
      - ...to...
      - \*  $((mNRRsmoothingN * 2) - 1)$
- Note: taking the median of previous N calculations only has a negative effect; it only adds an additional source of error and mitigates no existing error. Therefore, not recommended for main model (or use in practical systems).

# Comparison with Time Series Simulation

Case	residenceTime (ms)	TSGE ( $\pm$ ns)	DTSE ( $\pm$ ns)	Temp Factor	mNRR Smoothing	Time Series max DTE  @100 hops (ns)	% Diff 100% Temp $\rightarrow$ 10% Temp	Monte Carlo max DTE  @100 hops (ns)	Monte Carlo max7sigma @100 hops (ns)	TS $\rightarrow$ MC max DTE	TS $\rightarrow$ MC 7Sigma
<b>Single Replication</b>											
1	1	4	8	100%	No	2717		1715	2729	-36.9%	0.4%
2	1	2	8	100%	No	2891		1666	2649	-42.4%	-8.4%
3	4	4	8	100%	No	6023		5967	8983	-0.9%	49.1%
4	4	2	8	100%	No	6155		5848	8722	-5.0%	41.7%
5	10	4	8	100%	No	13618		14470	21722	6.3%	59.5%
6	10	2	8	100%	No	13252		14212	21089	7.2%	59.1%
7	1	4	8	10%	No	3058	13%	1715	2729	-43.9%	-10.8%
8	1	2	8	10%	No	2777	-4%	1666	2649	-40.0%	-4.6%
9	4	4	8	10%	No	6341	5%	5967	8983	-5.9%	41.7%
10	4	2	8	10%	No	6045	-2%	5848	8722	-3.3%	44.3%
11	10	4	8	10%	No	13942	2%	14470	21722	3.8%	55.8%
12	10	2	8	10%	No	12766	-4%	14212	21089	11.3%	65.2%
13	1	0	0	100%	No	32		13	19	-59.4%	-40.6%
14	1	0	8	100%	No	2841		1860	2630	-34.5%	-7.4%
15	1	4	0	100%	No	733		458	759	-37.5%	3.5%
16	1	4	8	100%	Yes	579		711	1080	22.8%	86.5%
17	1	2	8	100%	Yes	547		670	1049	22.5%	91.7%
18	4	4	8	100%	Yes	658		962	1466	46.2%	122.8%
19	4	2	8	100%	Yes	627		919	1426	46.6%	127.4%
20	10	4	8	100%	Yes	909		1653	2555	81.8%	181.1%
21	10	2	8	100%	Yes	856		1607	2489	87.7%	190.8%
22	1	4	8	10%	Yes	584	1%	711	1080	21.8%	84.9%
23	1	2	8	10%	Yes	601	10%	670	1049	11.5%	74.5%
24	4	4	8	10%	Yes	690	5%	962	1466	39.4%	112.5%
25	4	2	8	10%	Yes	787	26%	919	1426	16.8%	81.2%
26	10	4	8	10%	Yes	1441	59%	1653	2555	14.7%	77.3%
27	10	2	8	10%	Yes	1376	61%	1607	2489	16.8%	80.9%
<b>300 Replications</b>											
16 (28)	1	4	8	100%	Yes	815	40.8%	711	1080	-12.7%	32.5%
18 (29)	4	4	8	100%	Yes	1121	78.8%	962	1466	-14.2%	30.8%
22 (30)	1	4	8	10%	Yes	784	34.2%	711	1080	-9.3%	37.8%
27 (31)	10	2	8	10%	Yes	2202	60.0%	1607	2489	-27.0%	13.0%

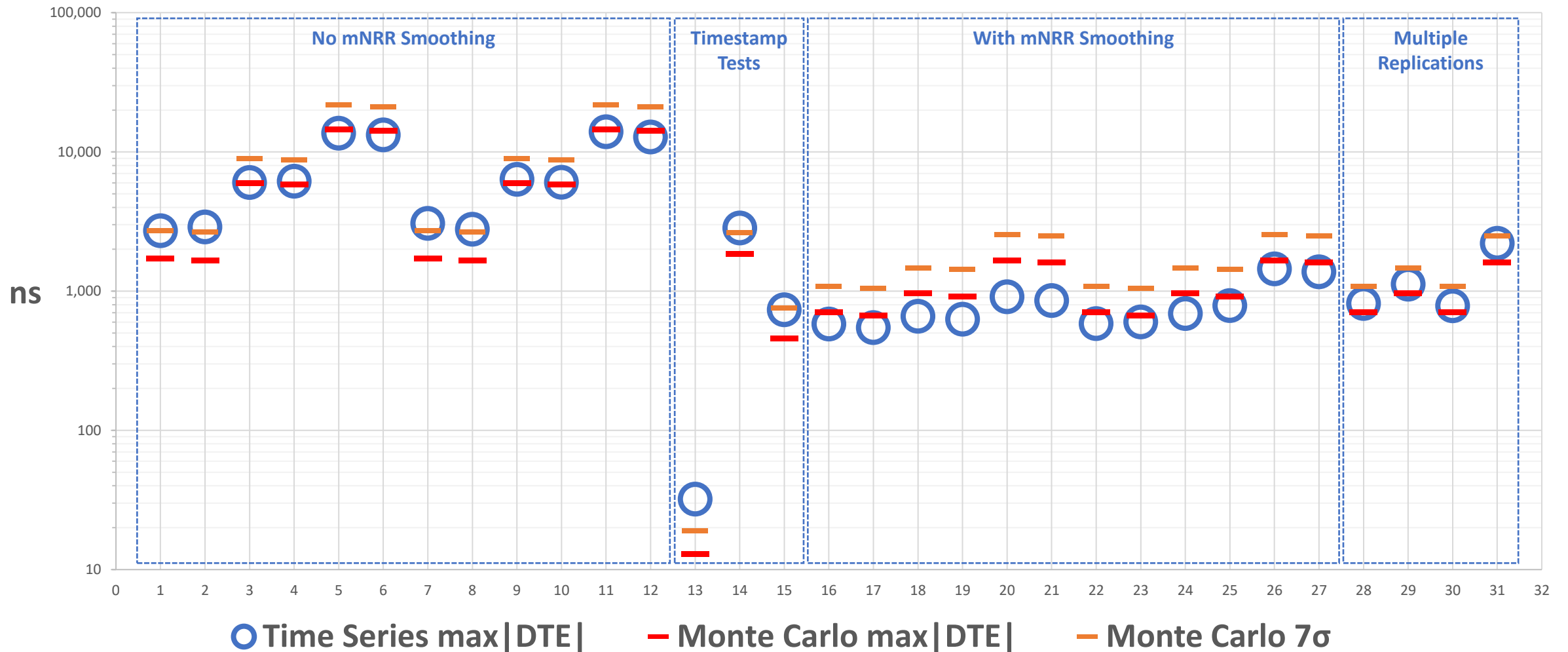
No mNRR Smoothing

Timestamp Tests

With mNRR Smoothing

Multiple Replications

# Comparison with Time Series Simulation



# Comparison with Time Series Simulation

- Monte Carlo results broadly align with Time Series results
- Where results deviate the most, they are still usefully close and the Monte Carlo results move in the same direction and by similar amounts as the Time Series results when input parameters change
- The closest matches are between Monte Carlo results and results from multiple replications of the Time Series simulation
- Monte Carlo analysis is definitely good enough for investigating approaches to minimising DTE

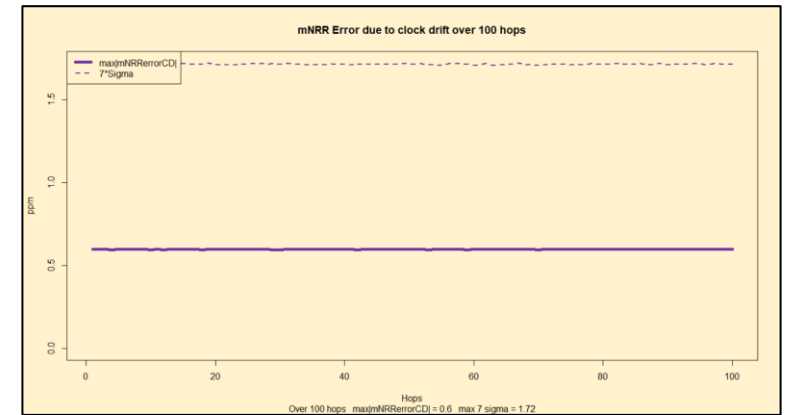
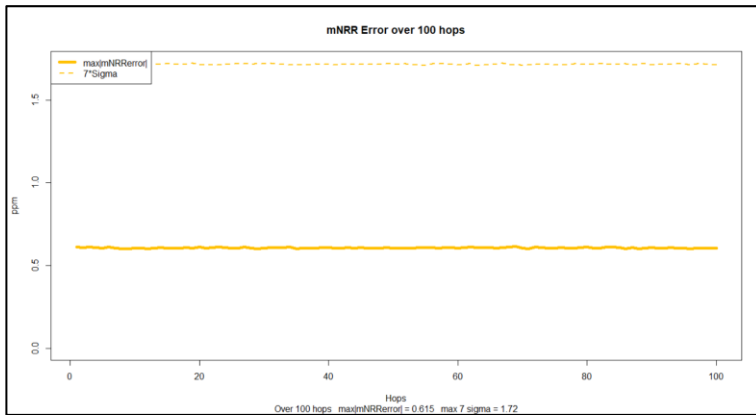
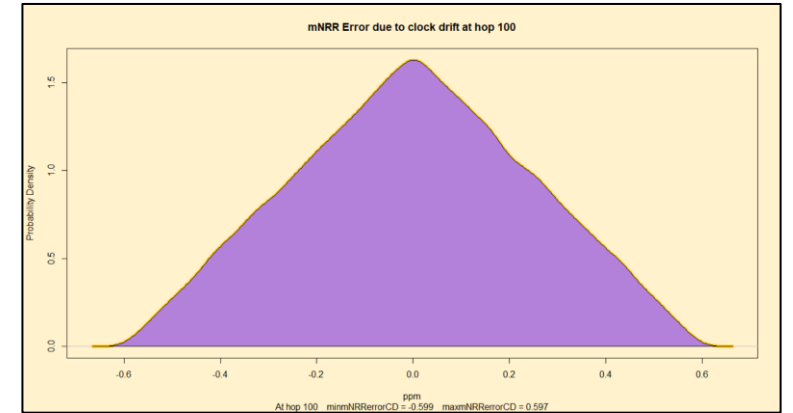
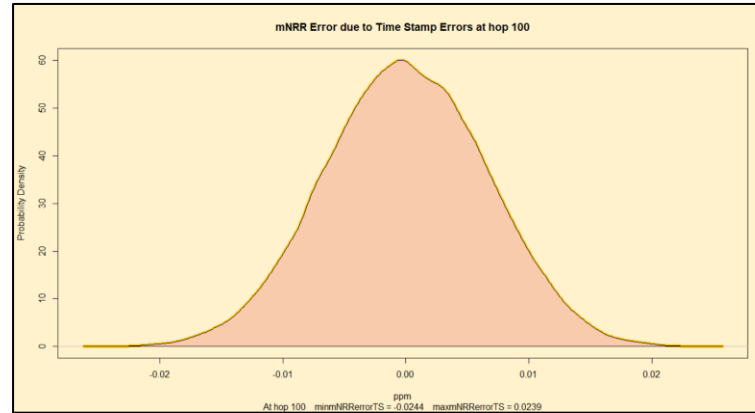
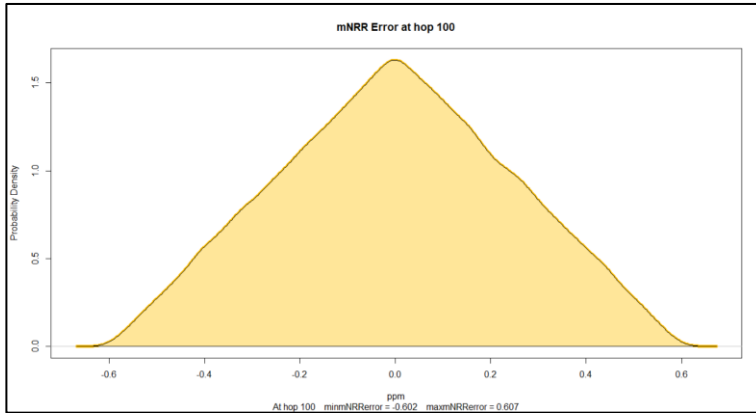
# Error Analysis

# Graphical Representations

- The Monte Carlo Analysis can generate **a lot** of data
- Prioritising what to data to look at and how to analyse it will help reach useful conclusions quickly
- With that in mind, here is an overview of the data that can be generated by RStudio...
  - Main Model  
(not the Time Series Match version)
  - 802.1AS Default Input Parameters
  - Clock Drift (inc. GM):  $\pm 0.6$  ppm/s
  - No correction factors

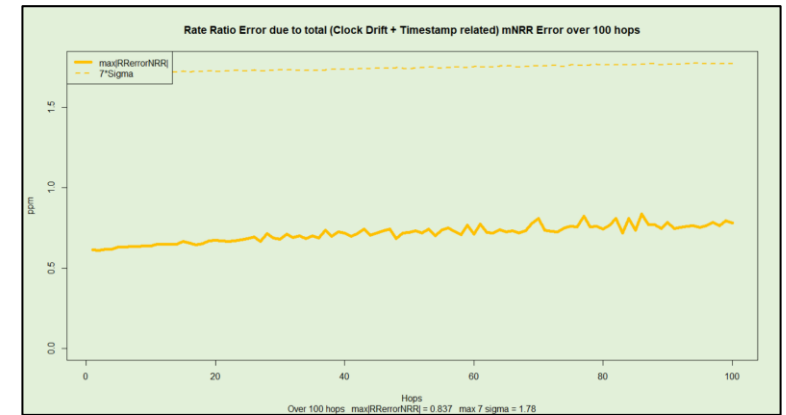
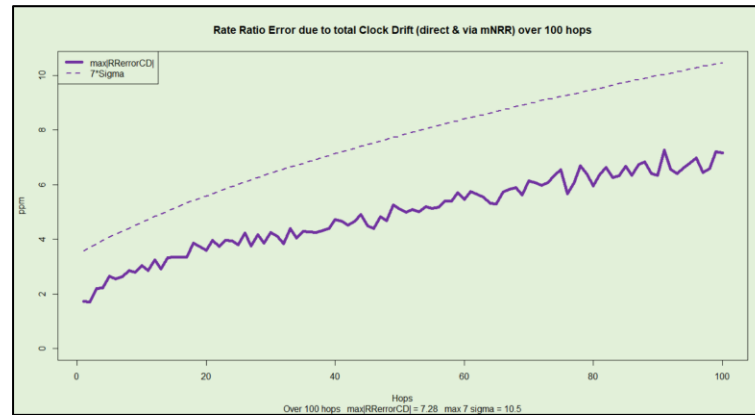
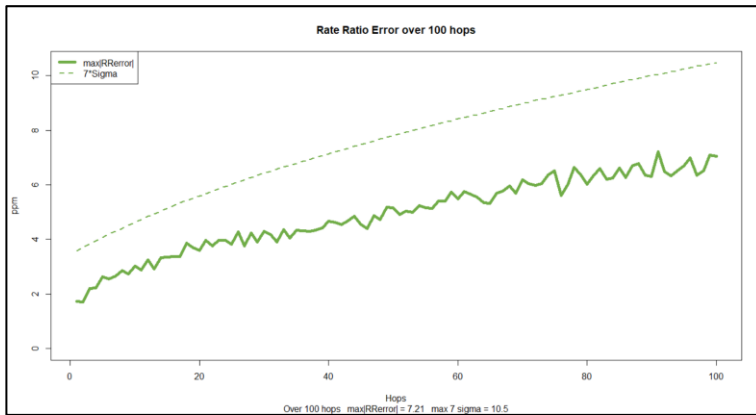
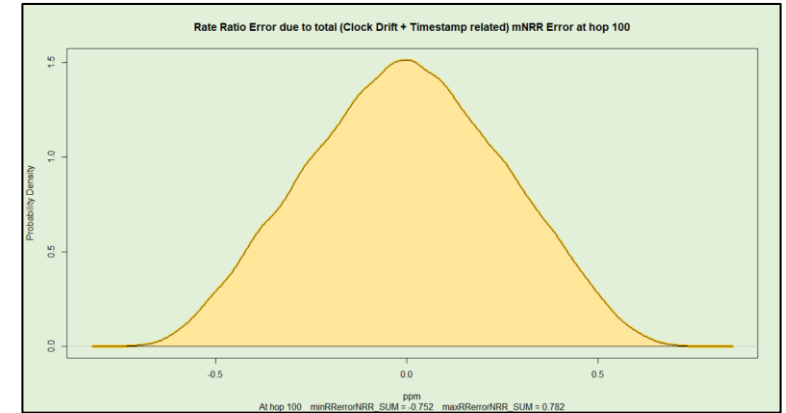
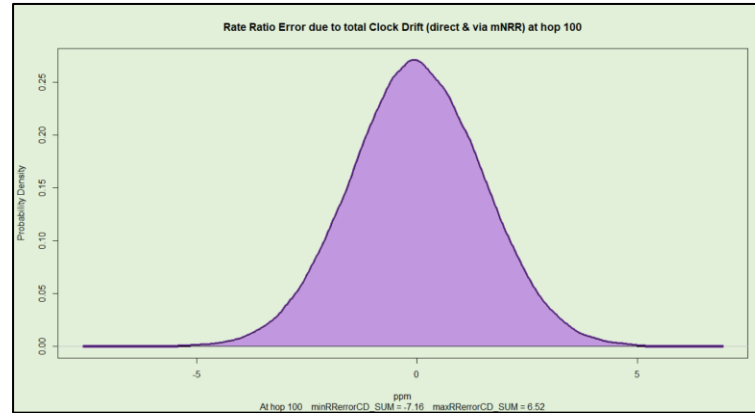
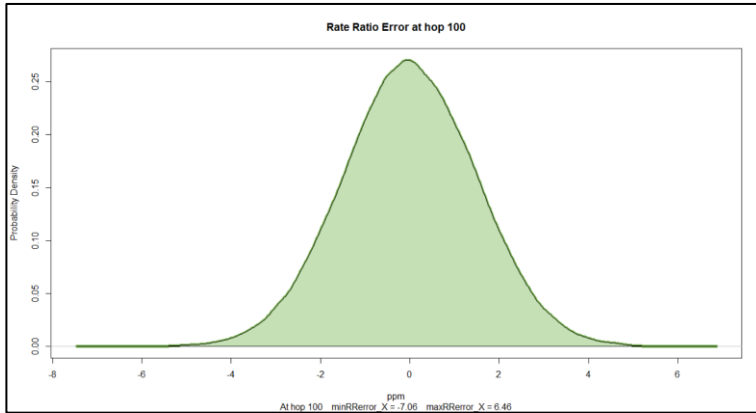
Input Errors		
GM Clock Drift Max	+0.6	ppm/s
GM Clock Drift Min	+0.6	ppm/s
Clock Drift (non-GM)	0.6	$\pm$ ppm/s
Timestamp Granularity TX	4	$\pm$ ns
Timestamp Granularity RX	4	$\pm$ ns
Dynamic Time Stamp Error TX	4	$\pm$ ns
Dynamic Time Stamp Error RX	4	$\pm$ ns
Input Parameters		
pDelay Interval	1000	ms
pDelay Response Time	10	ms
residenceTime	10	ms
Correction Factors		
Mean Link Delay	0	%
Drift Rate	0	%
pDelayResponse $\rightarrow$ Sync	0	%
mNRR Smoothing	1	
Configuration		
Hops	100	
Runs	100,000	

# mNRR Error

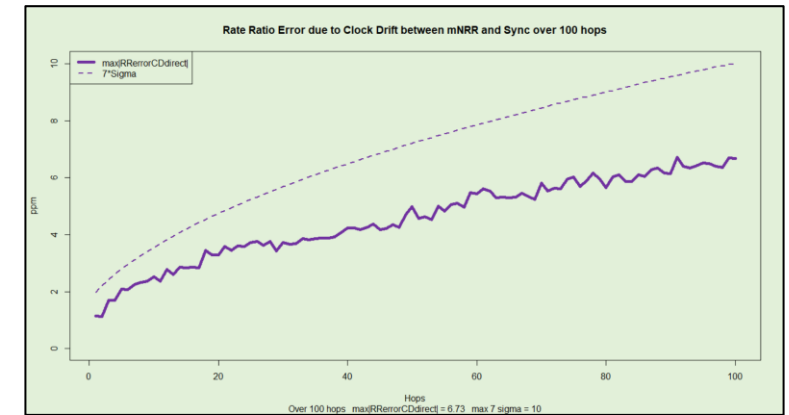
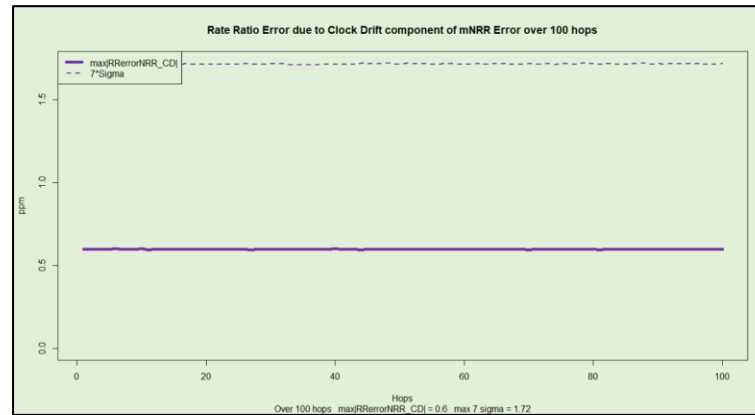
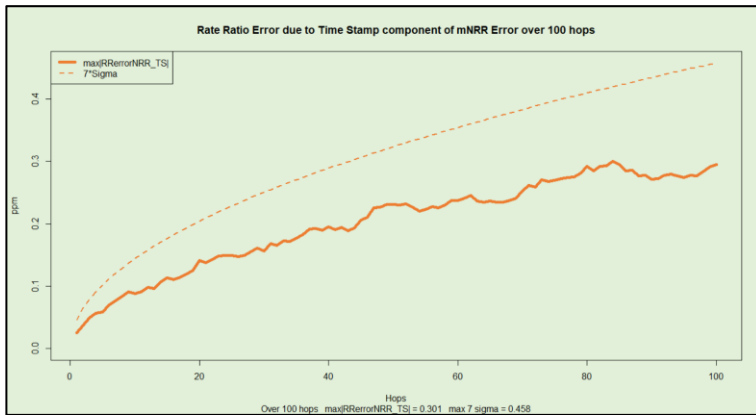
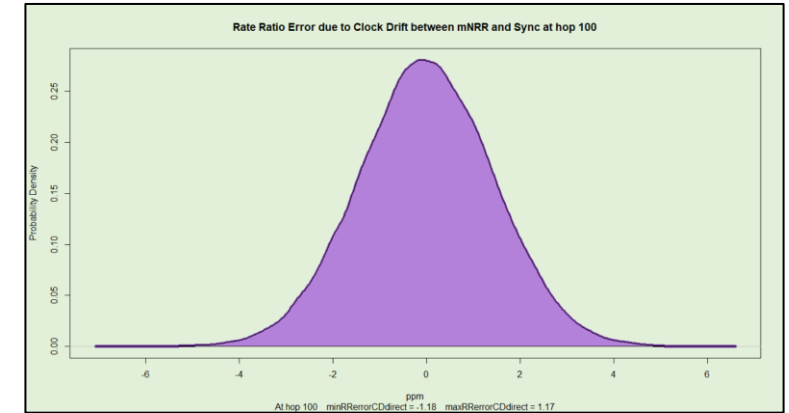
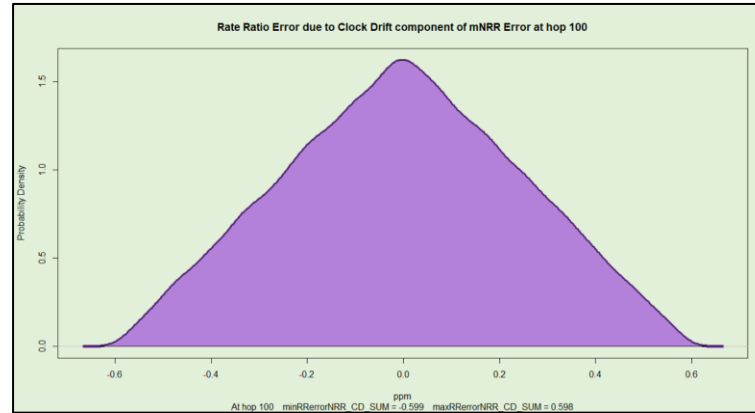
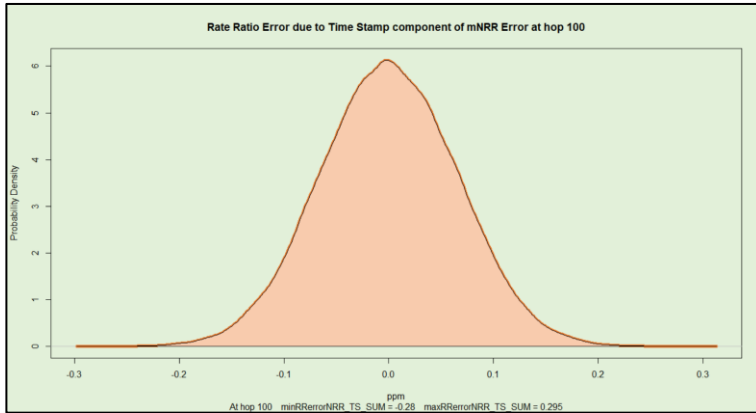




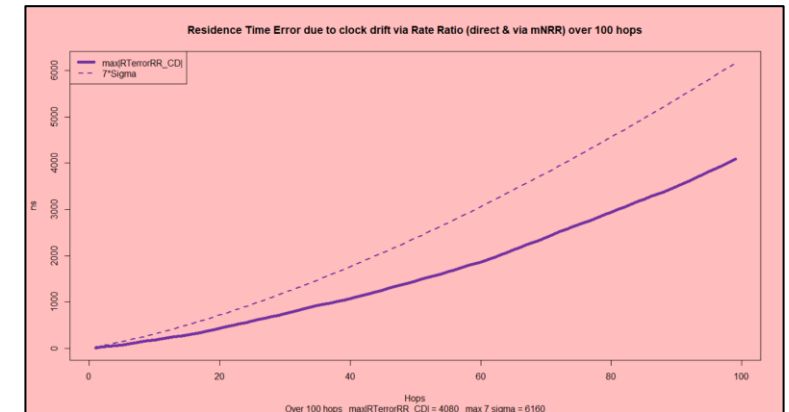
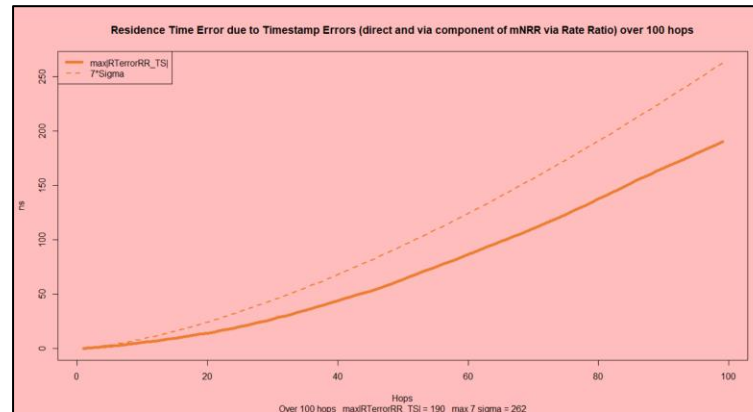
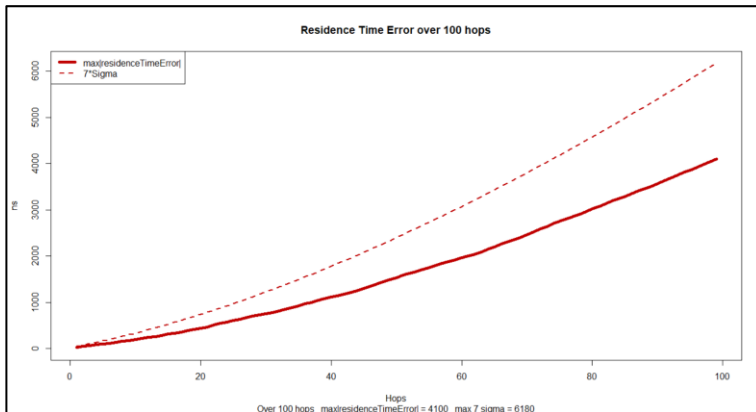
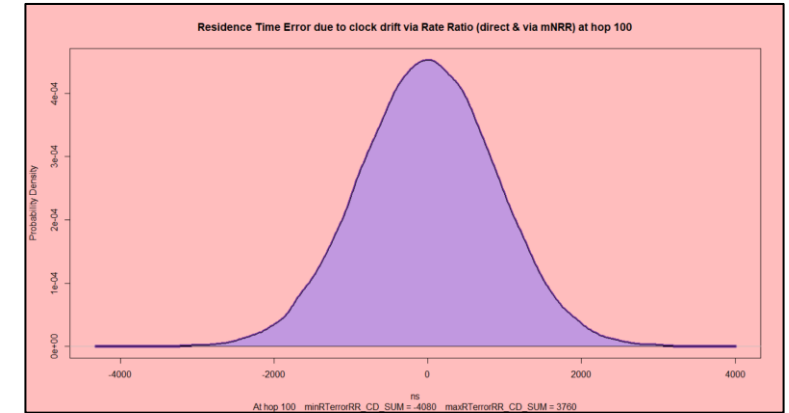
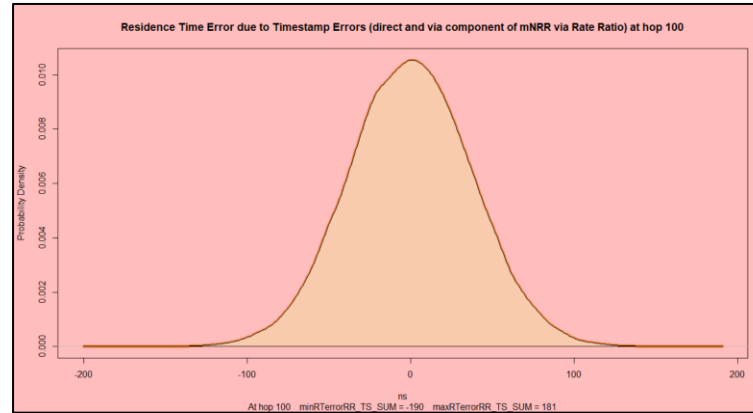
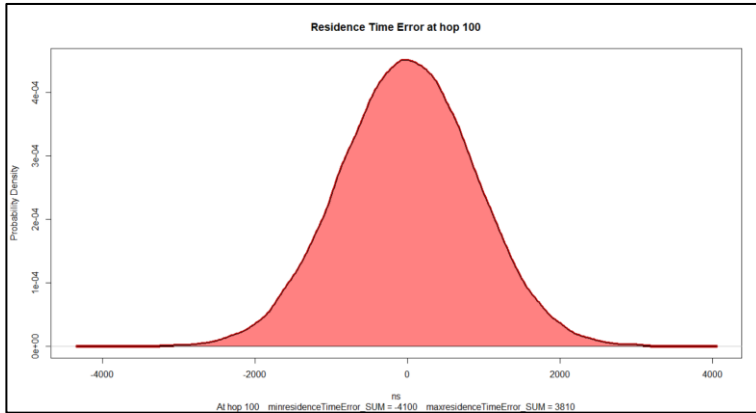
# Rate Ratio Error – Timestamp & Clock Drift



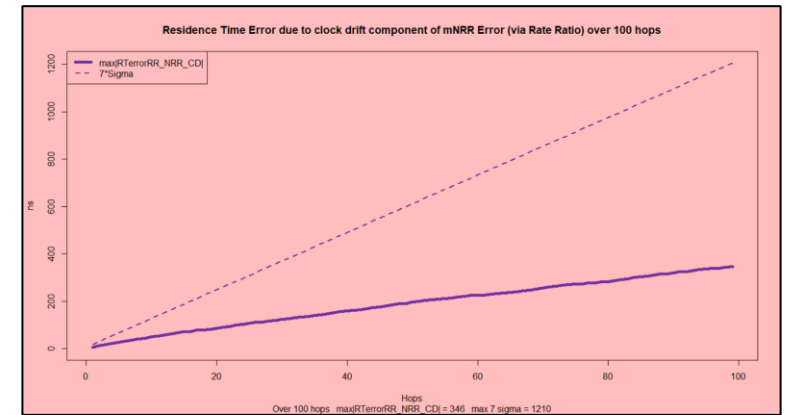
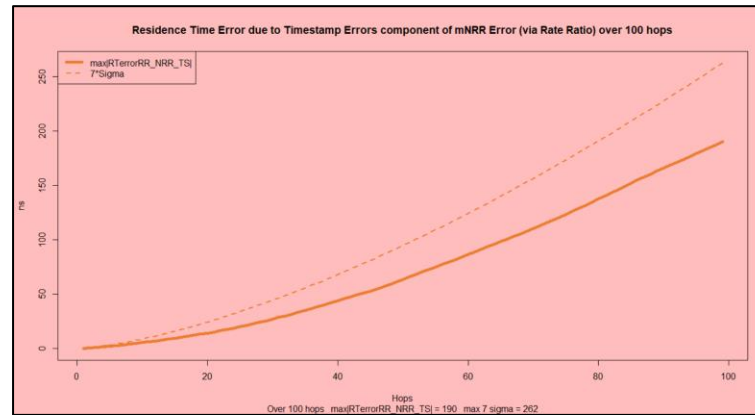
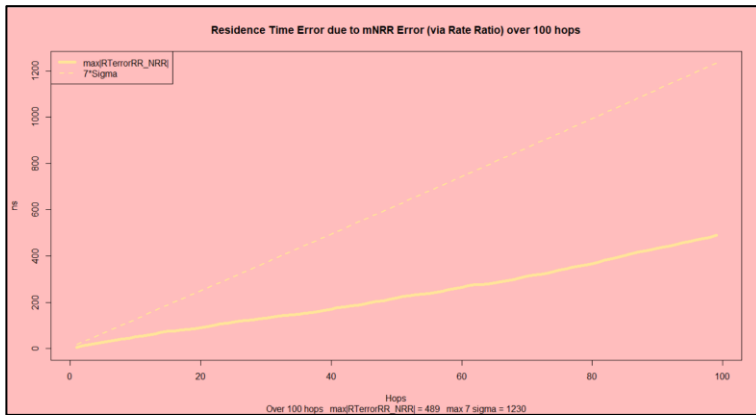
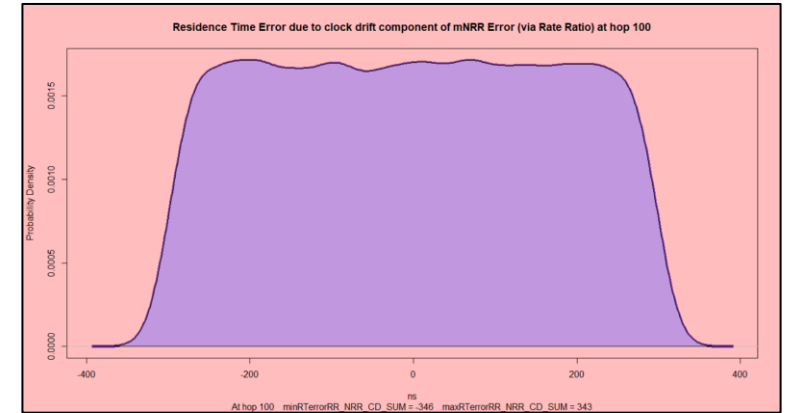
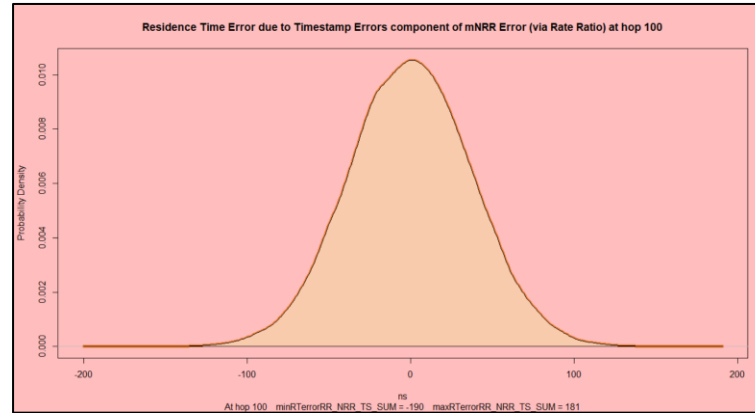
# Rate Ratio Error – mNRR & Direct Clock Drift



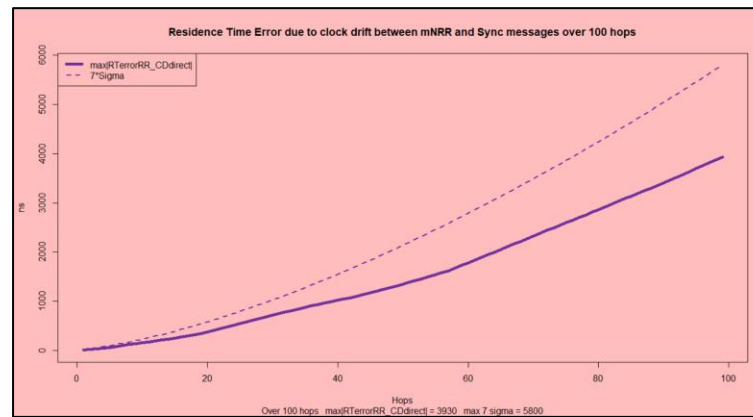
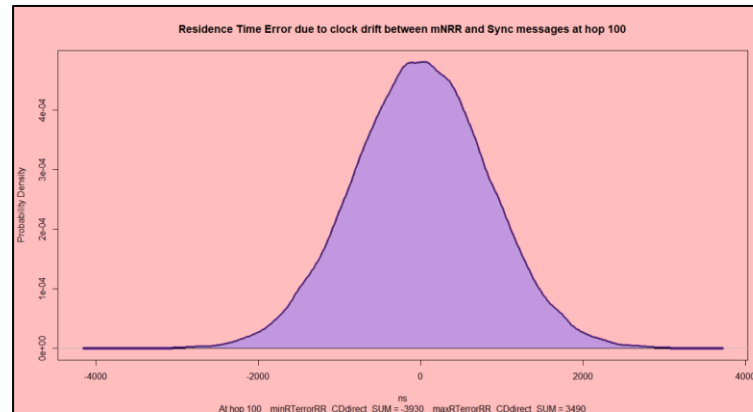
# Residence Time Error – Timestamp & Clock Drift



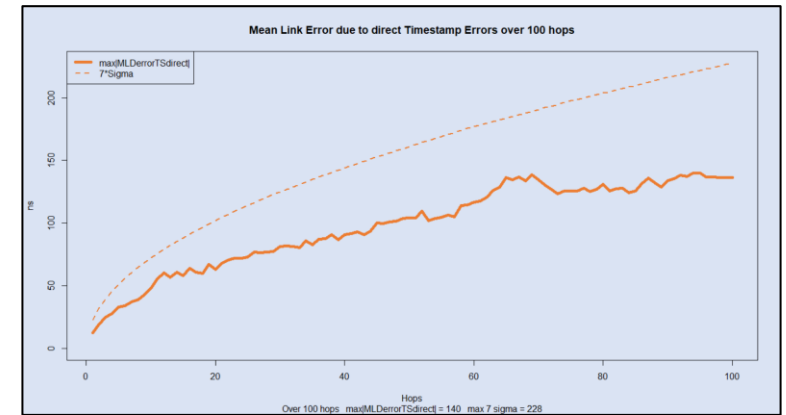
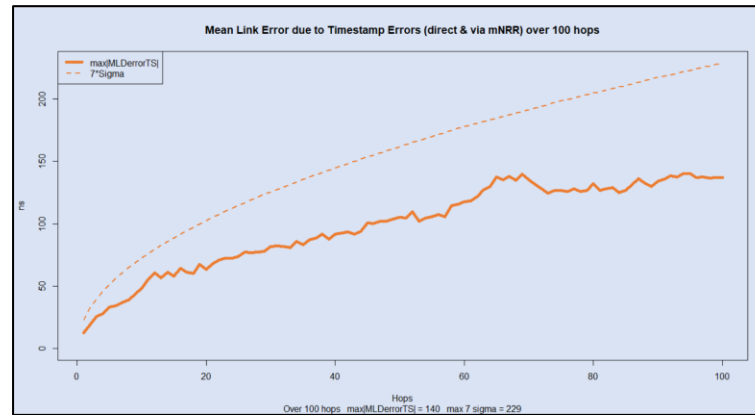
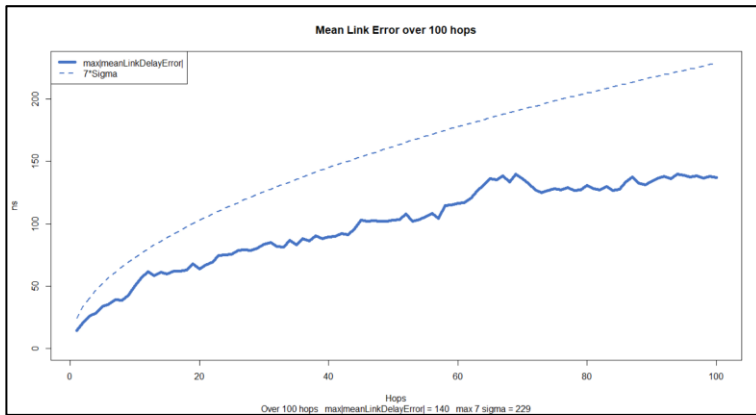
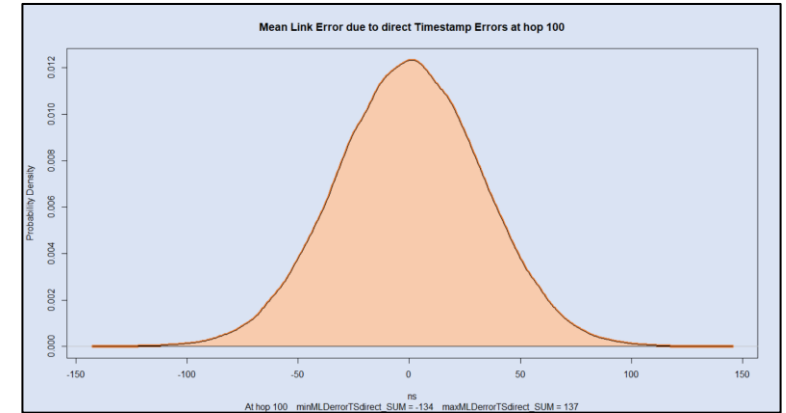
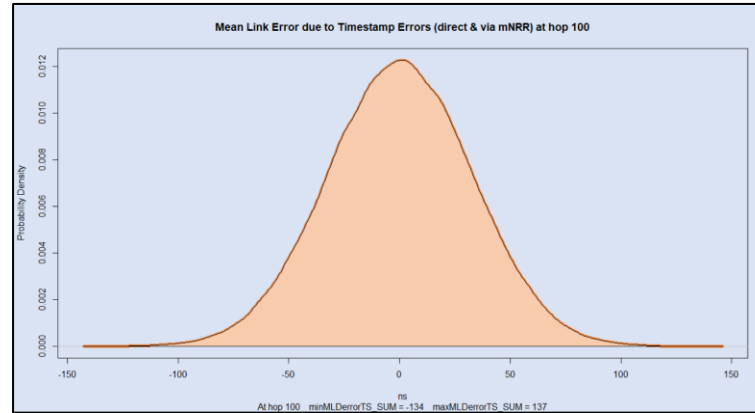
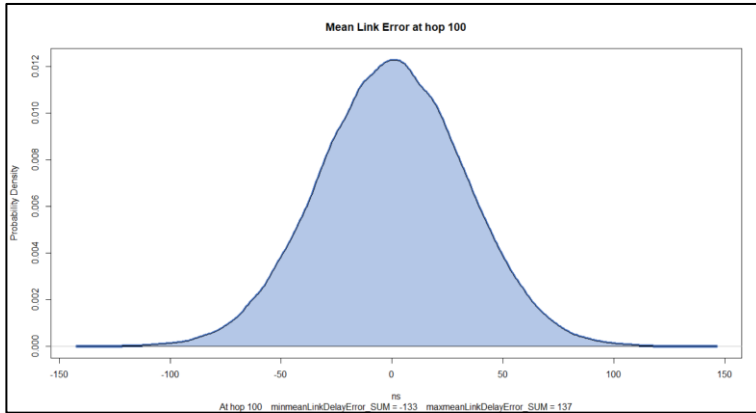
# Residence Time Error – mNRR



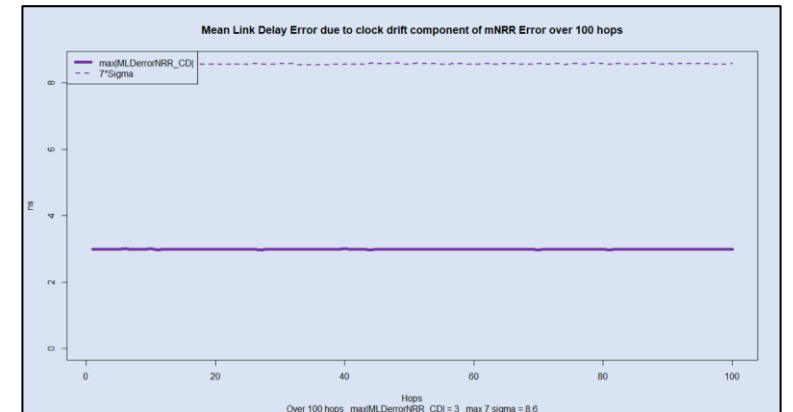
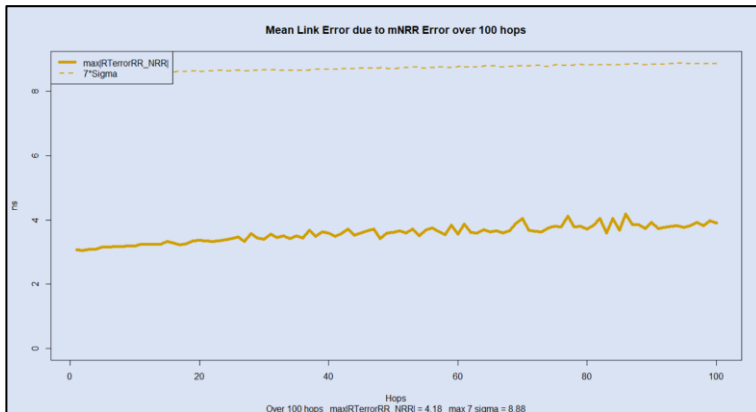
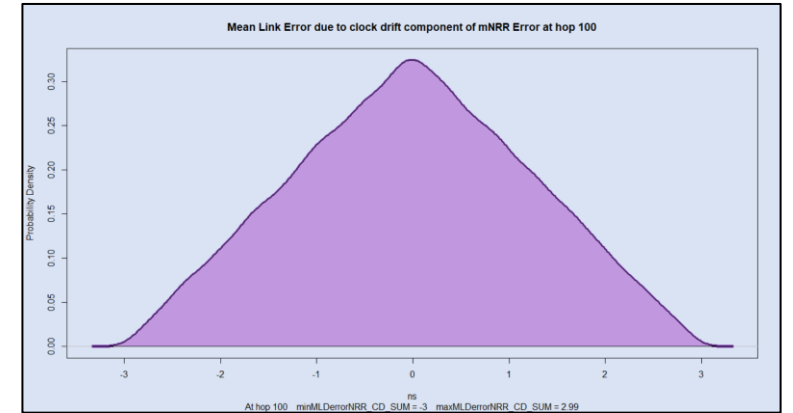
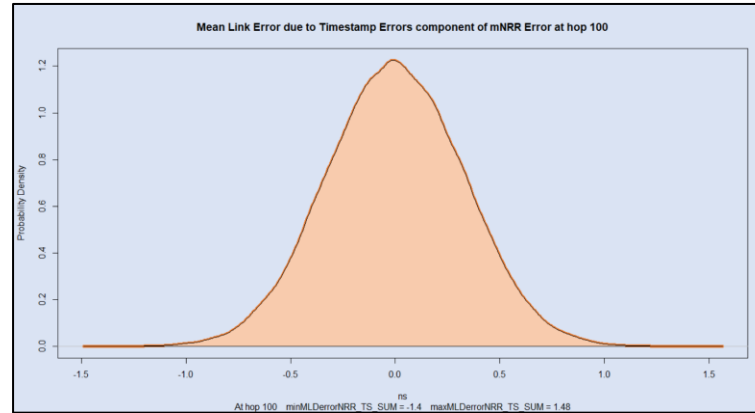
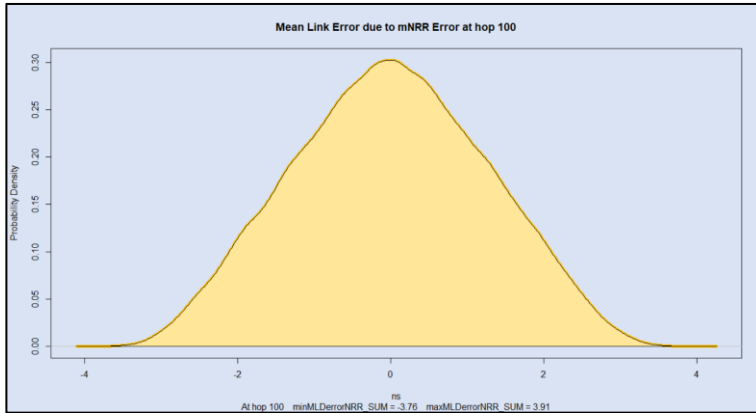
# Residence Time – Direct Clock Drift



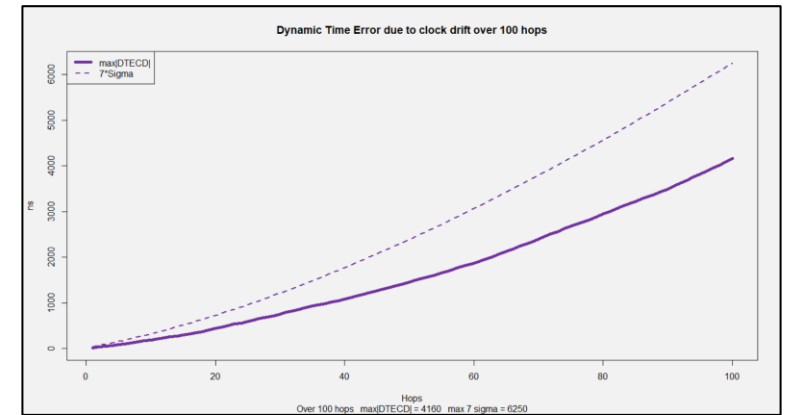
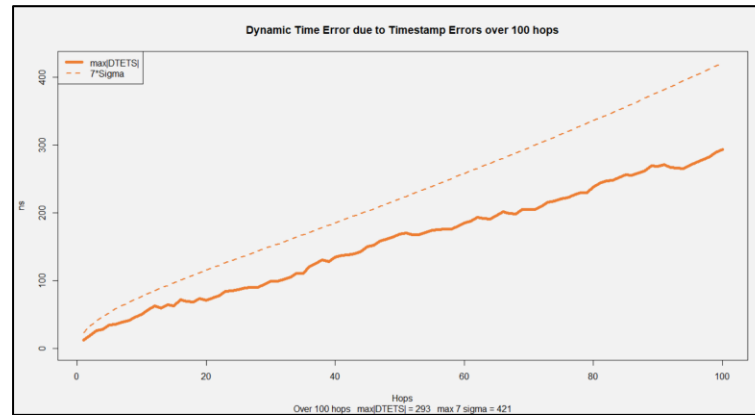
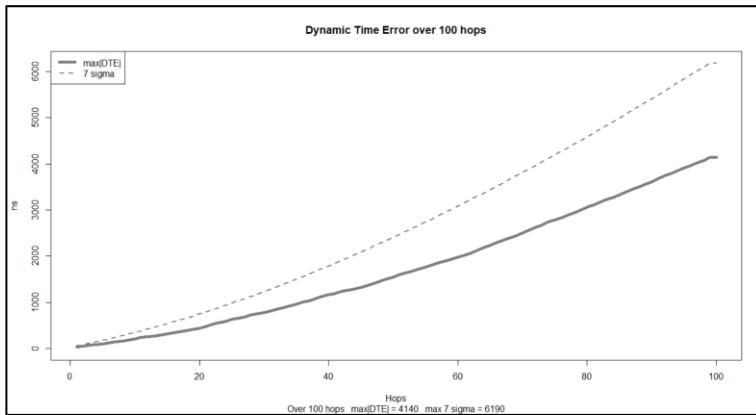
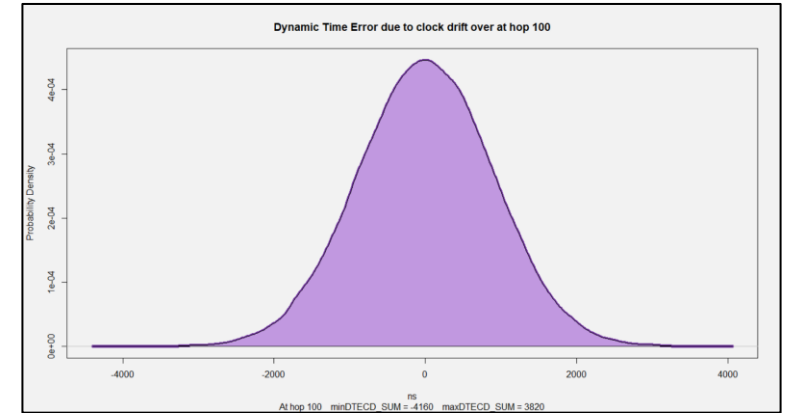
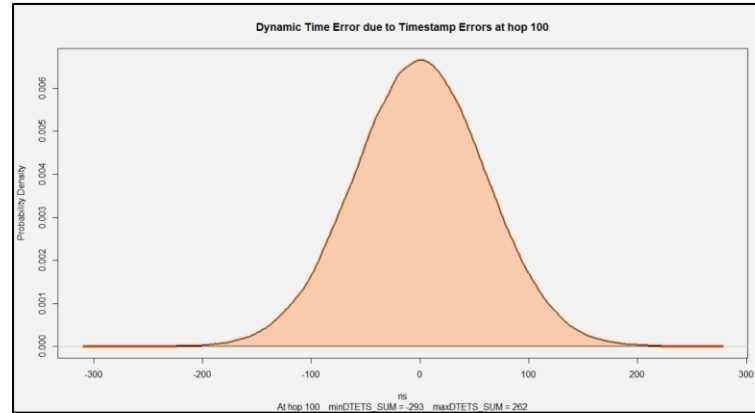
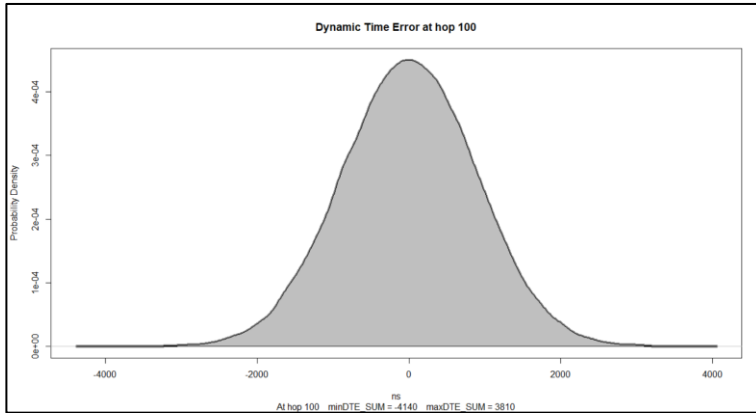
# Mean Link Delay Error – Total & Direct Timestamp Errors



# Mean Link Delay Error – mNRR Error

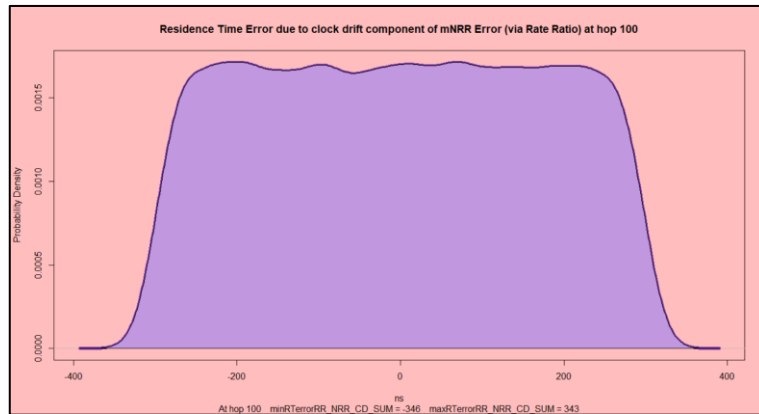


# Dynamic Time Error

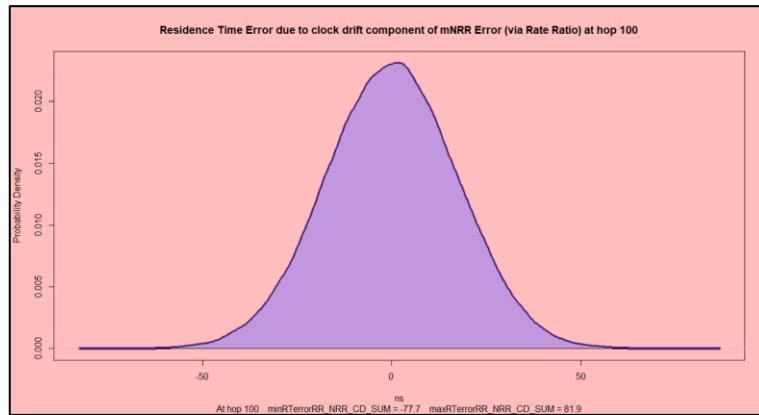
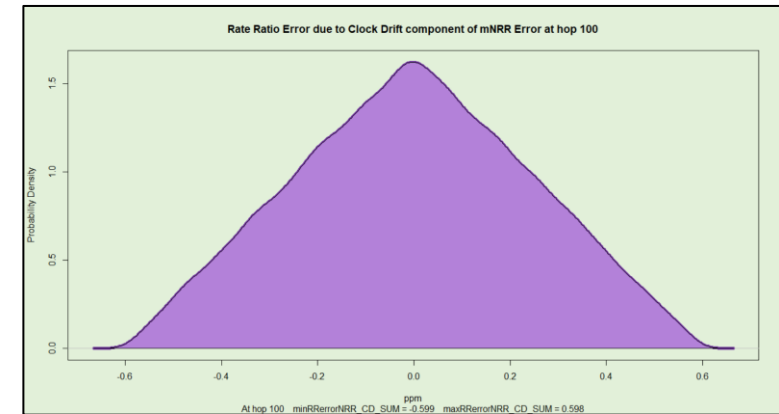




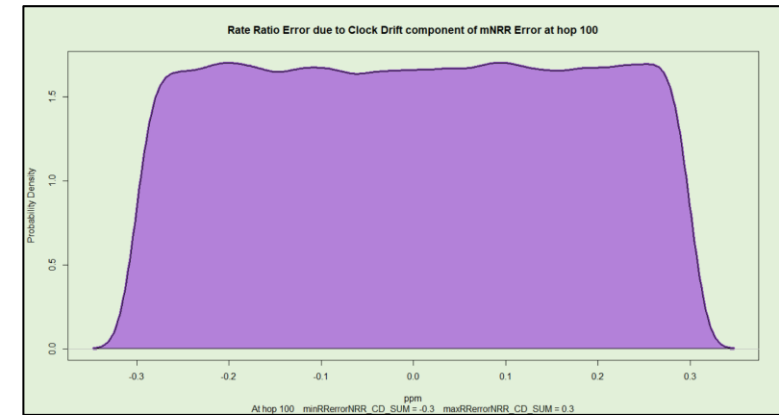
# Effect of GM Clock Drift on Residence Time Error and Rate Ratio Error



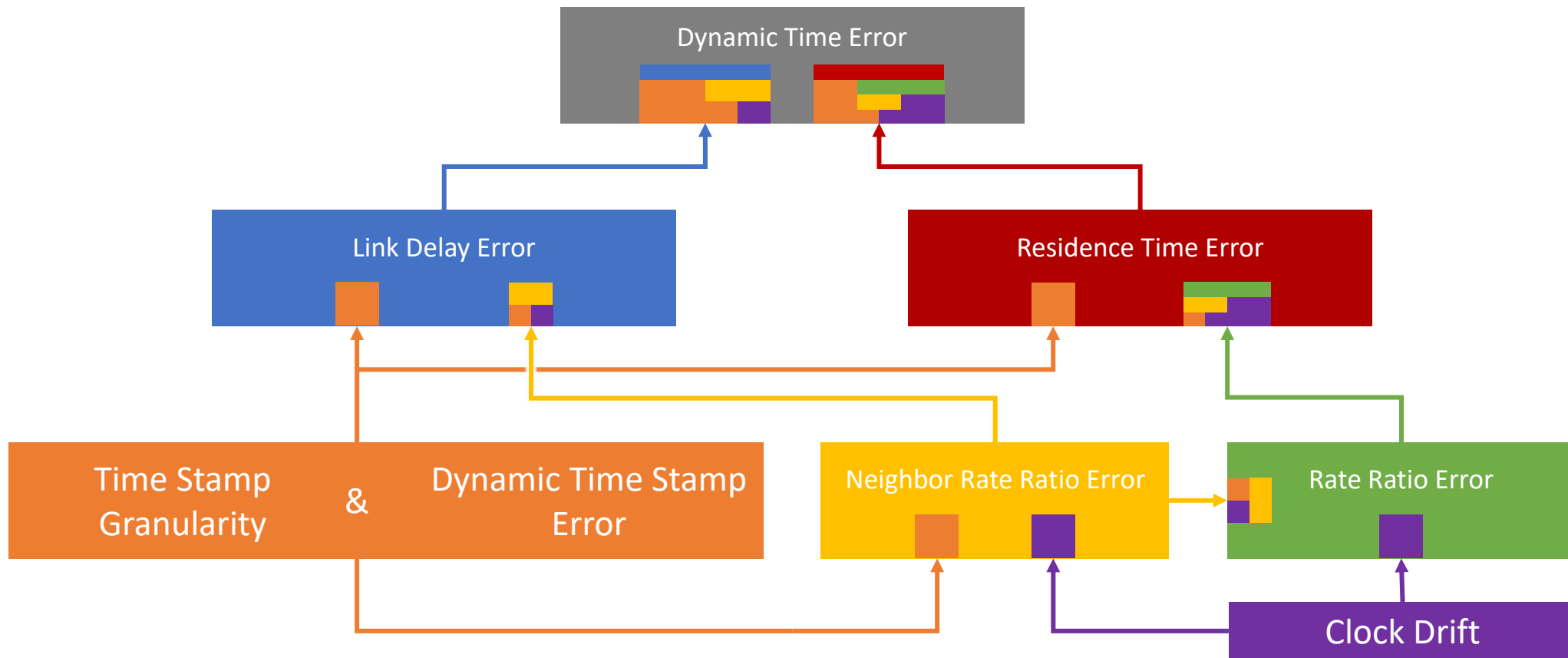
**GM Clock Drift  
±0.6 ppm/s**



**GM Clock Drift  
0 ppm/s**



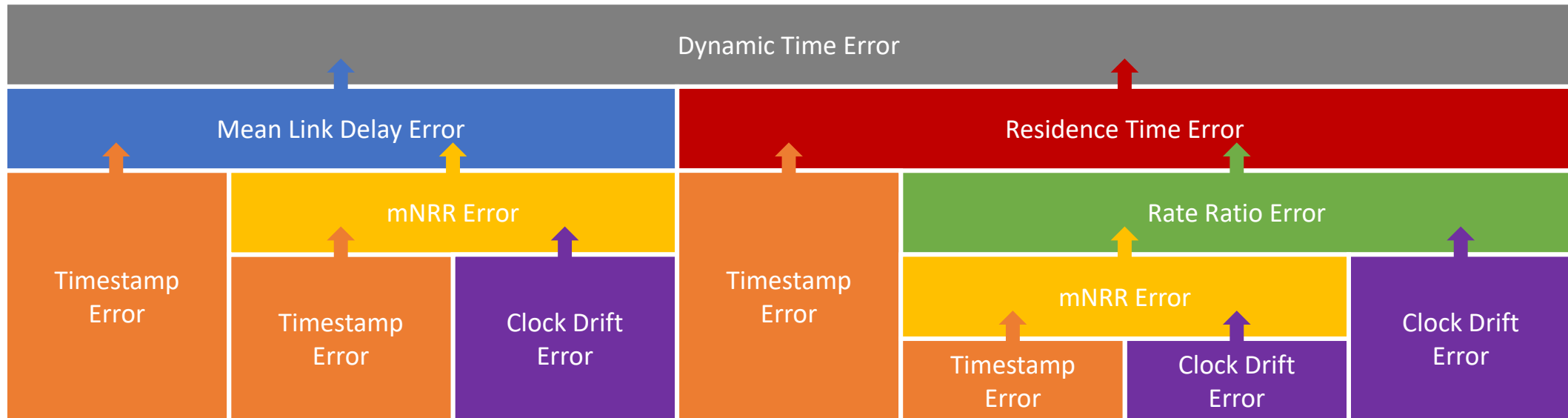
# Time Sync – How Errors Add Up



**All errors in this analysis are caused by either Clock Drift or Timestamp Errors**

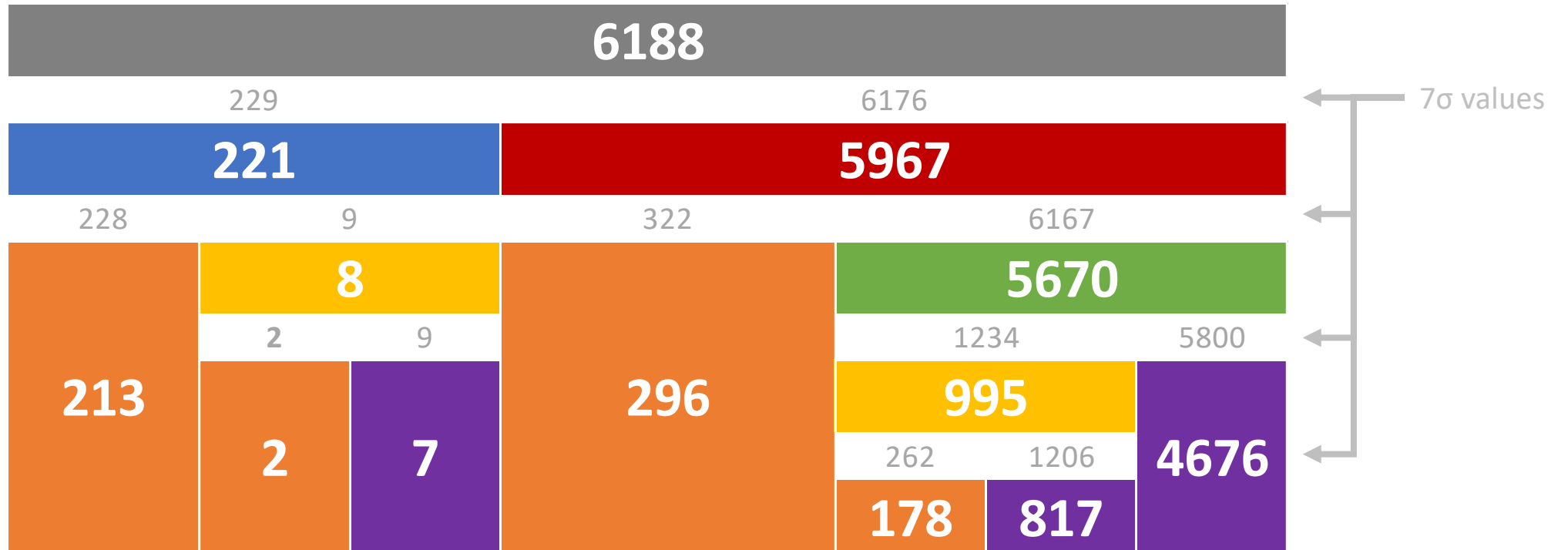
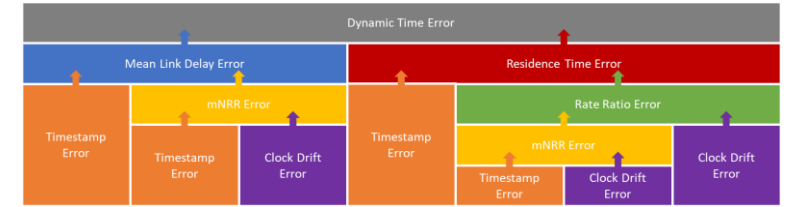
# Graphical Representation of Error Accumulation

- Each error breaks down into two parts

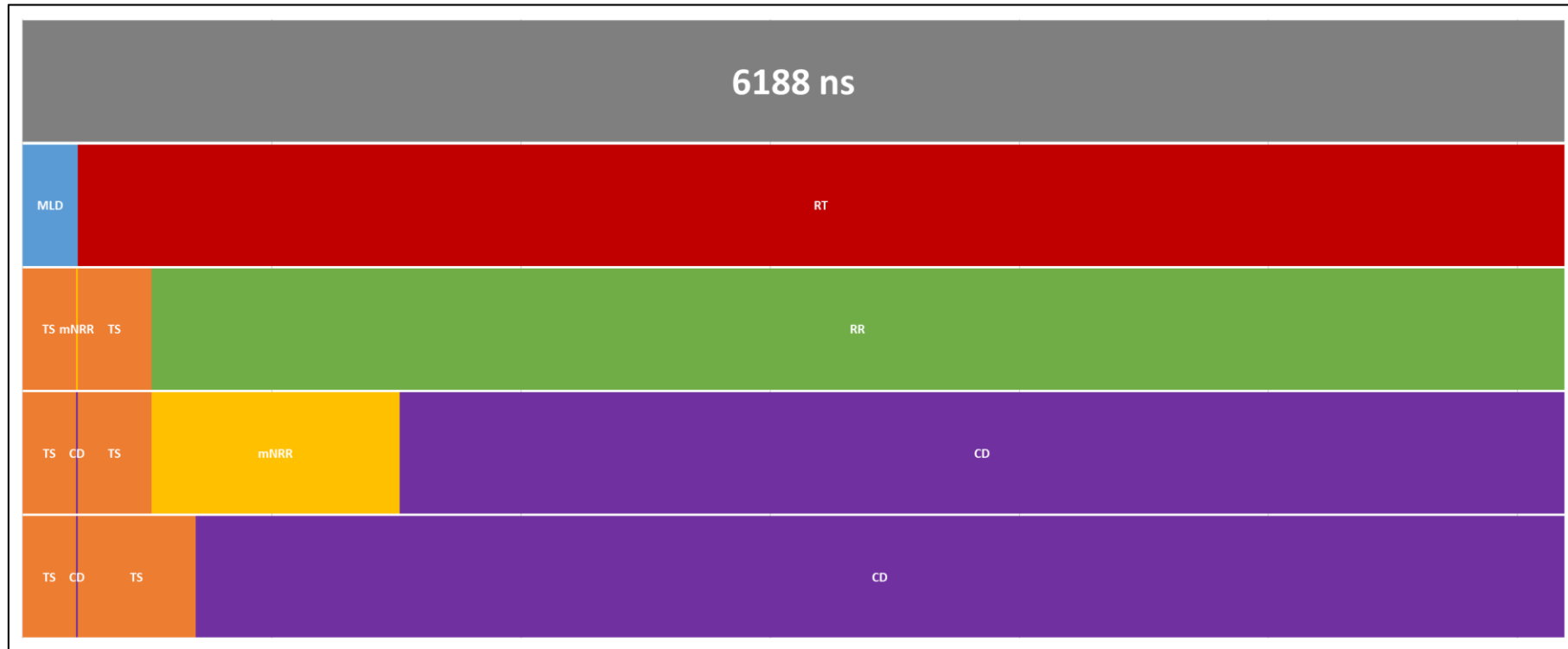
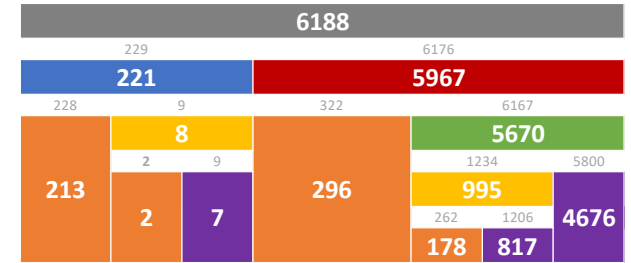


- The relative weight of each part can be judged by their  $7\sigma$  values

# Graphical Representation of Error Accumulation



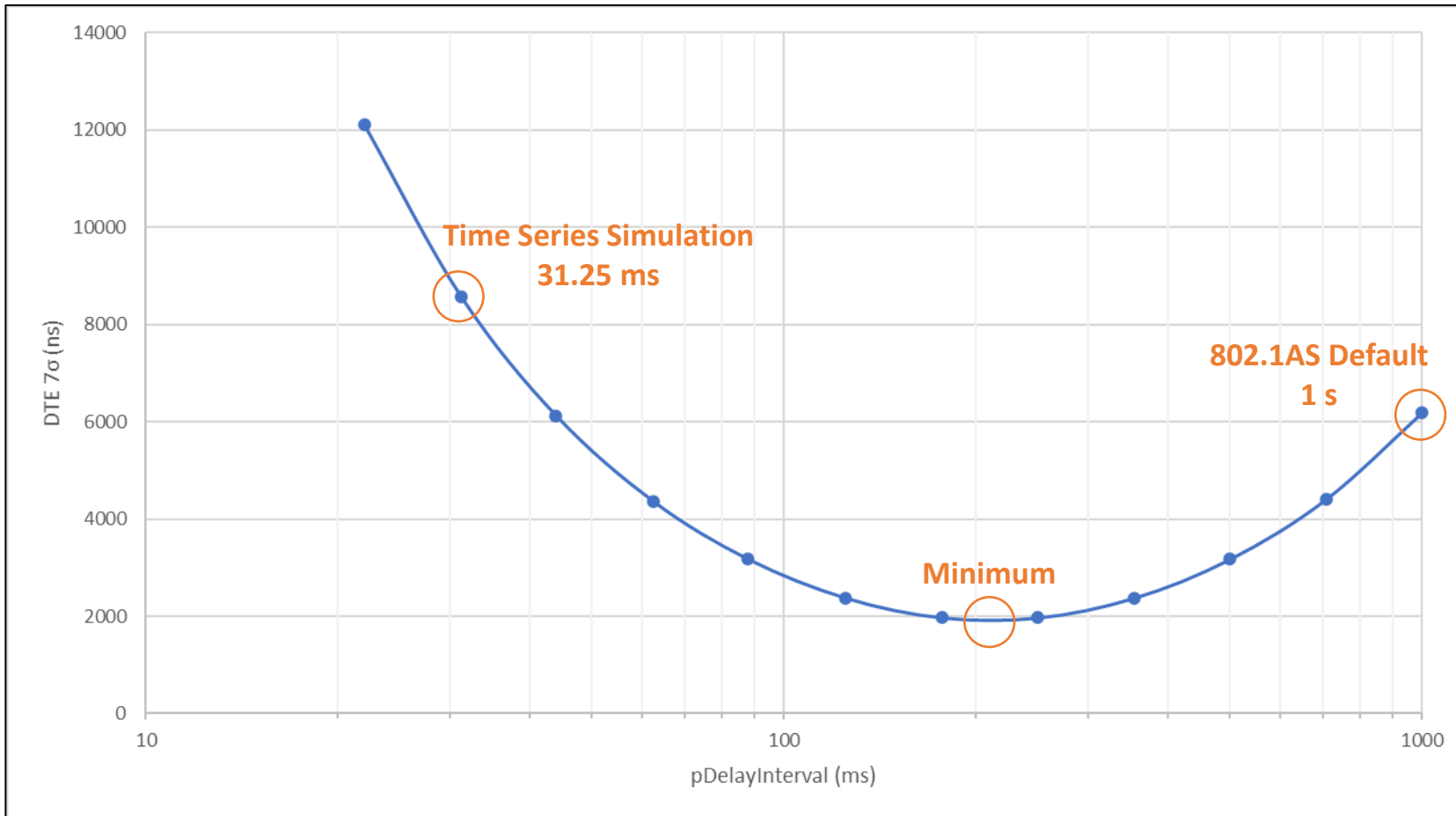
# Graphical Representation of Error Accumulation



# *pDelayInterval* Sensitivity Analysis

Plus a limited look at Timestamp & Clock Drift Sensitivity

# *pDelayInterval* Sensitivity Analysis



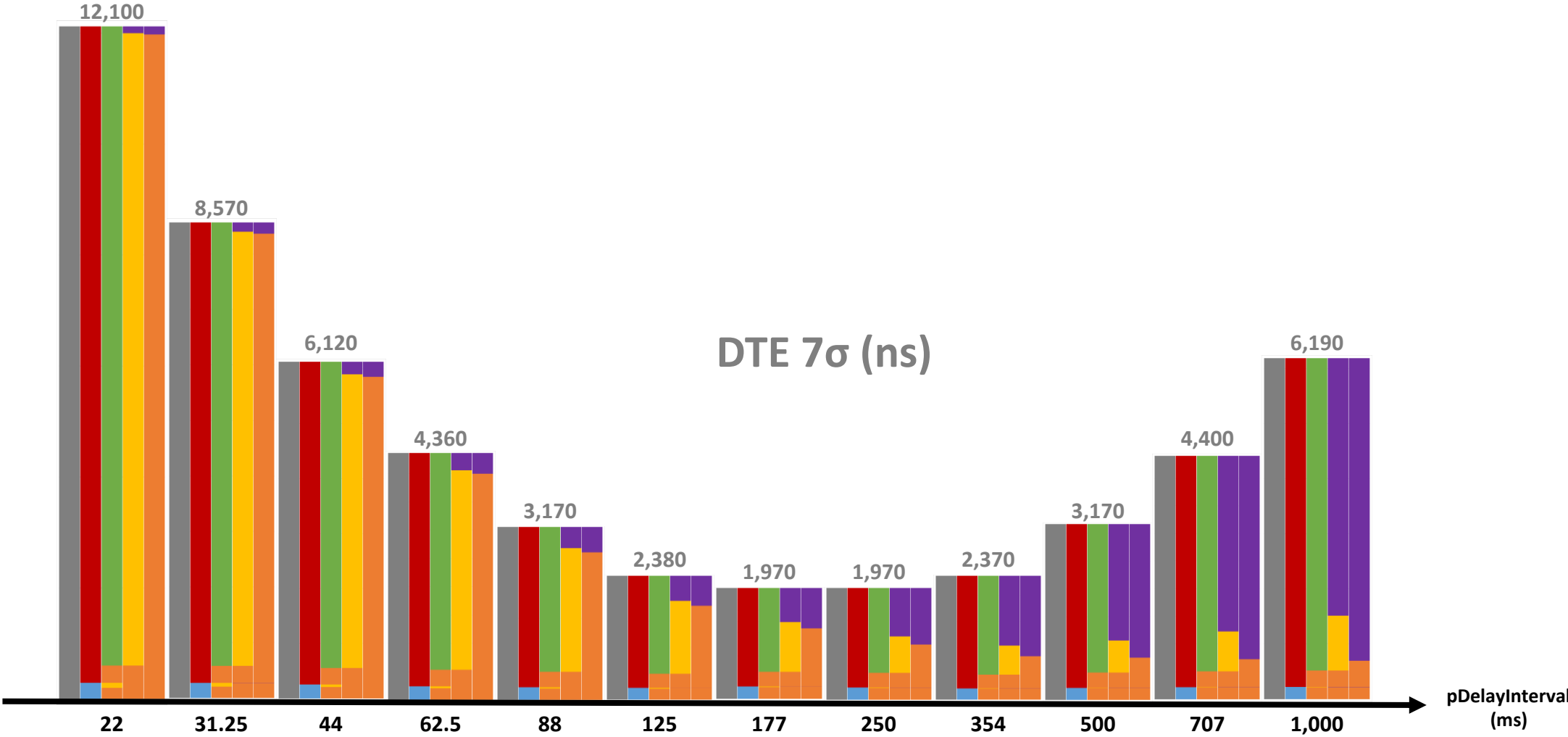
Input Errors		
GM Clock Drift Max	+0.3	ppm/s
GM Clock Drift Min	+0.3	ppm/s
Clock Drift (non-GM)	0.3	±ppm/s
Timestamp Granularity TX	4	±ns
Timestamp Granularity RX	4	±ns
Dynamic Time Stamp Error TX	4	±ns
Dynamic Time Stamp Error RX	4	±ns
Input Parameters		
pDelay Interval	Variable	ms
pDelay Response Time	10	ms
residenceTime	10	ms
Input Correction Factors		
Mean Link Delay	0	%
Drift Rate	0	%
pDelayResponse → Sync	0	%
mNRR Smoothing	1	
Configuration		
Hops	100	
Runs	100,000	

Vary This

**Minimum is at approx 210 ms...**

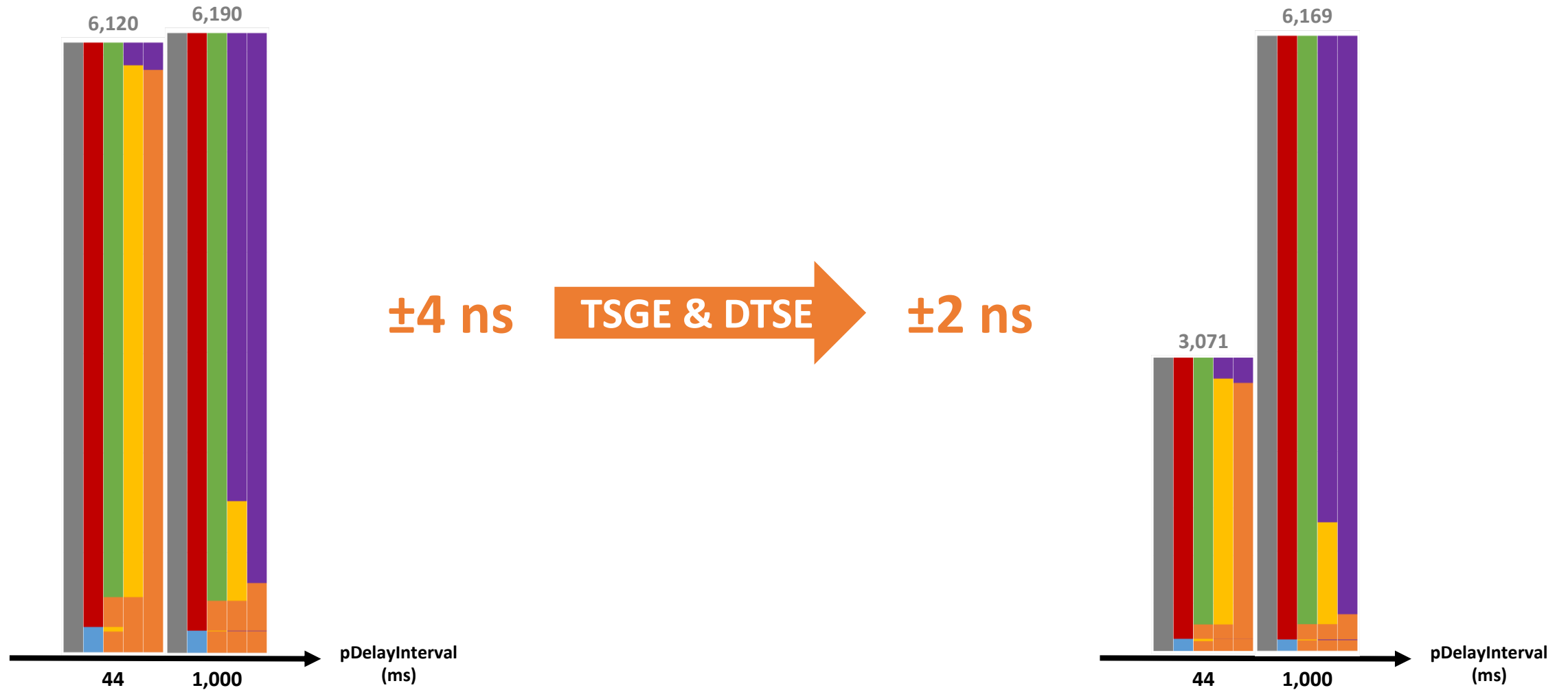
**...for this set of parameters.**

# *pDelayInterval* Sensitivity Analysis

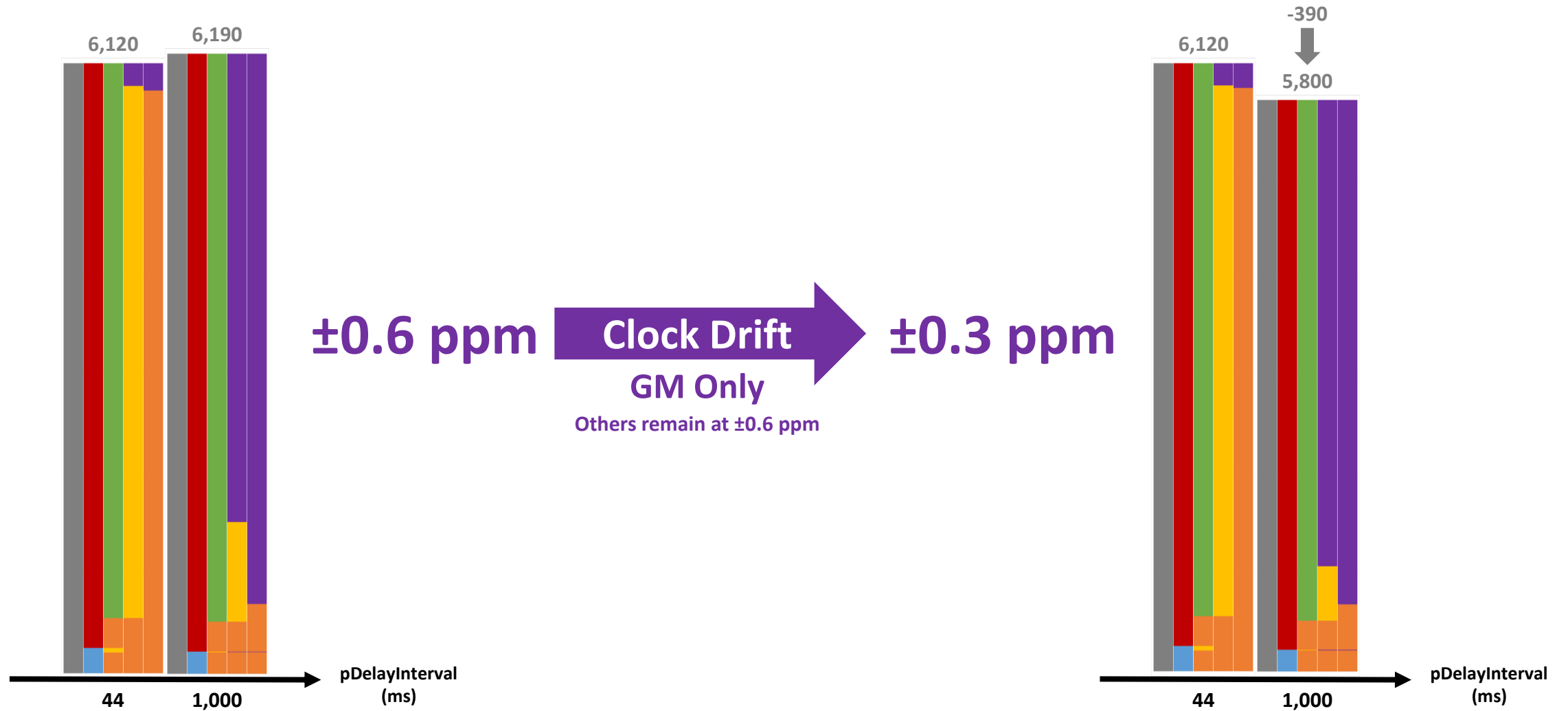




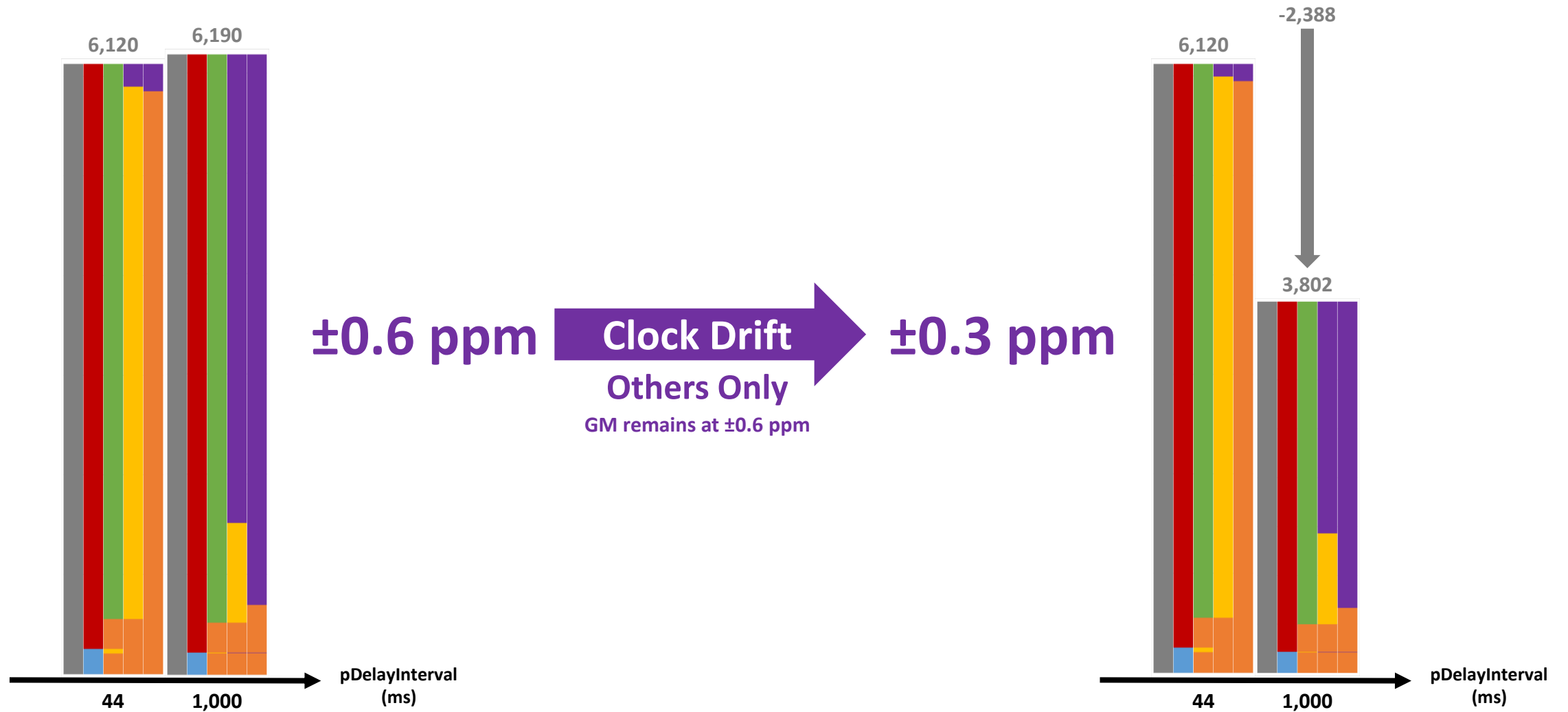
# Timestamp Errors Sensitivity



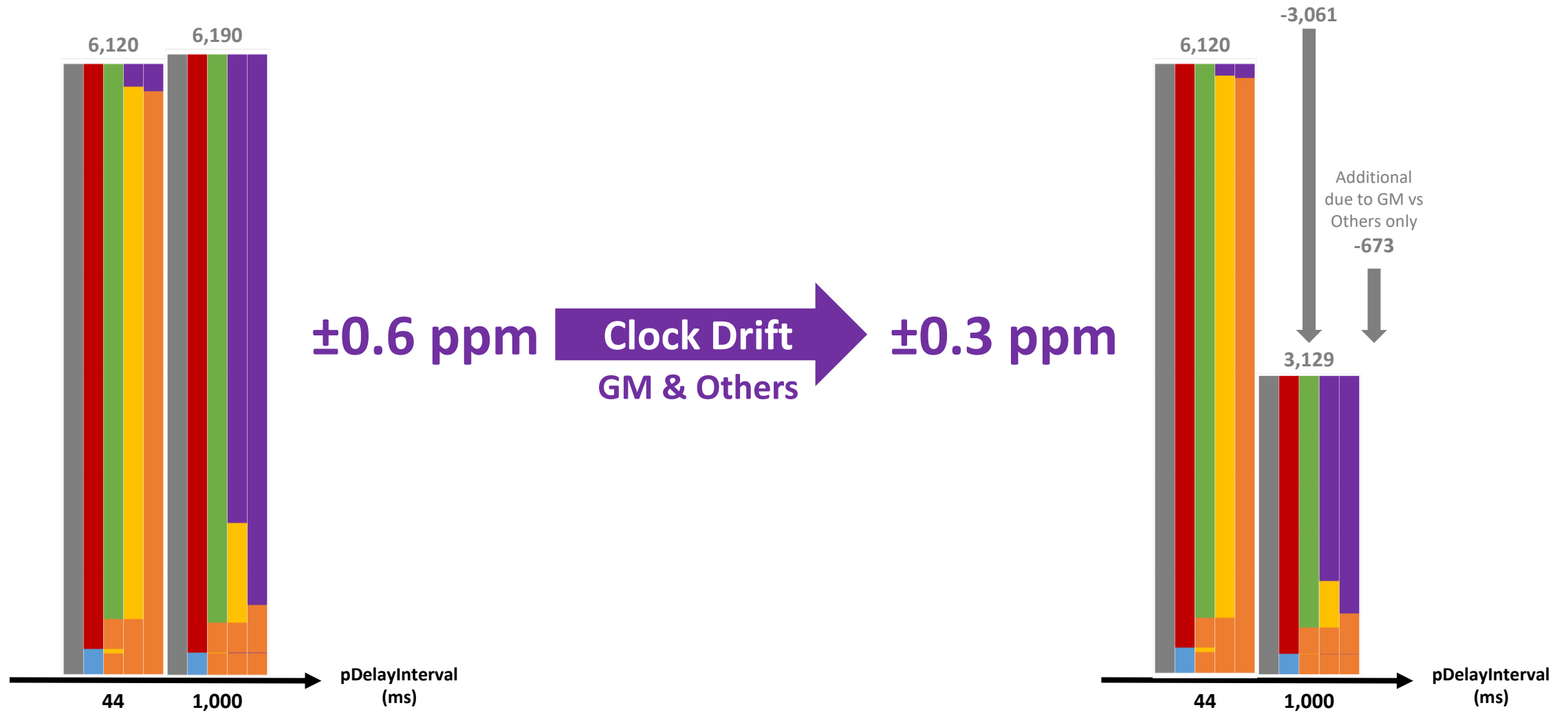
# Clock Drift Sensitivity



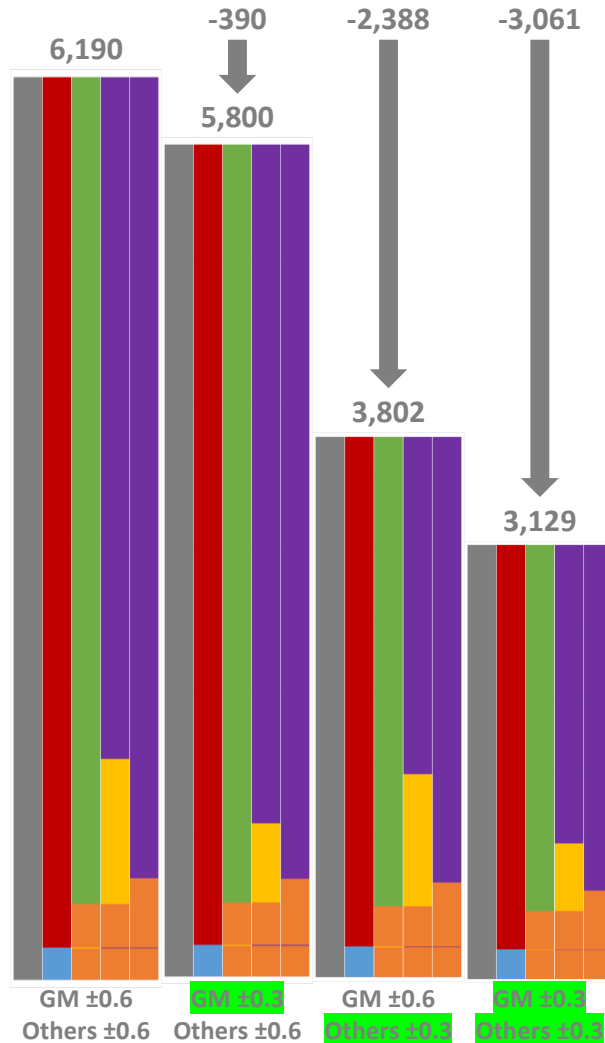
# Clock Drift Sensitivity



# Clock Drift Sensitivity

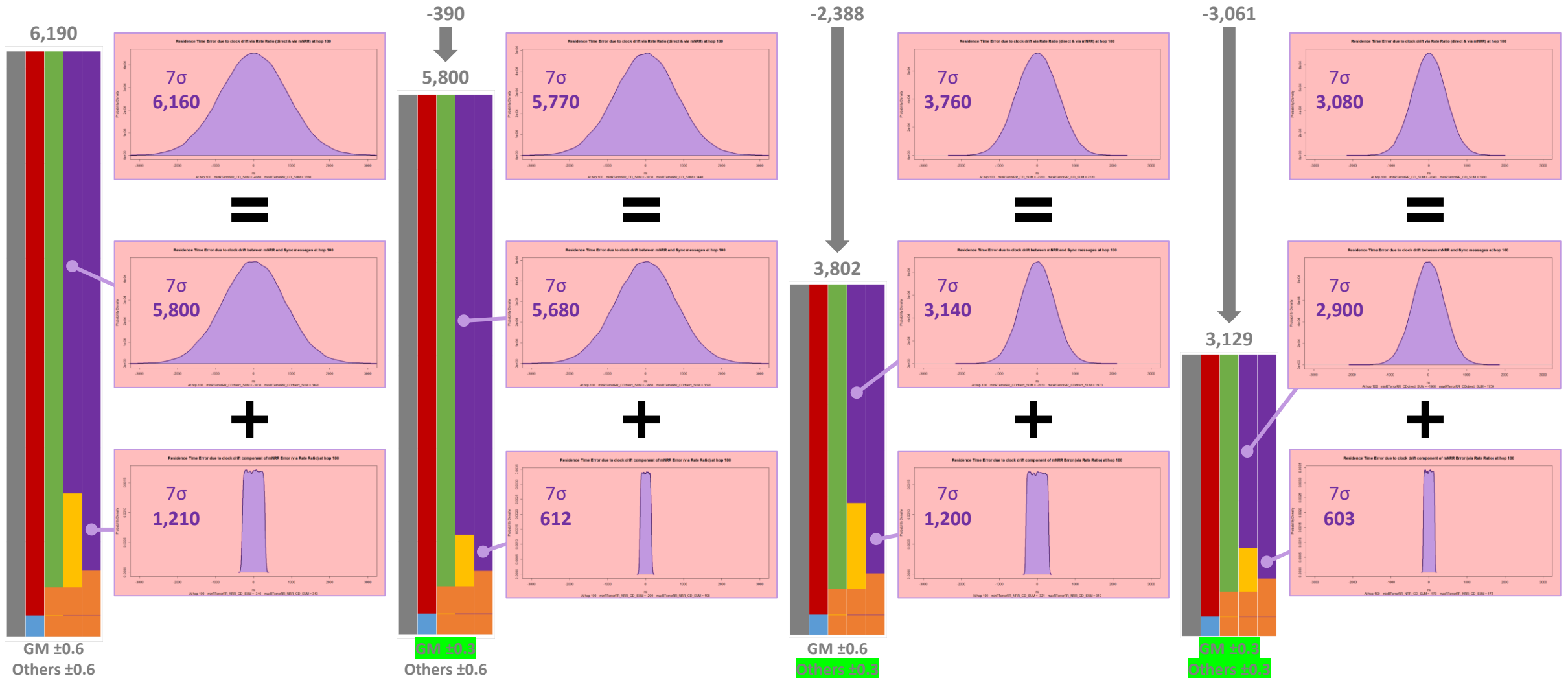


# Clock Drift Sensitivity

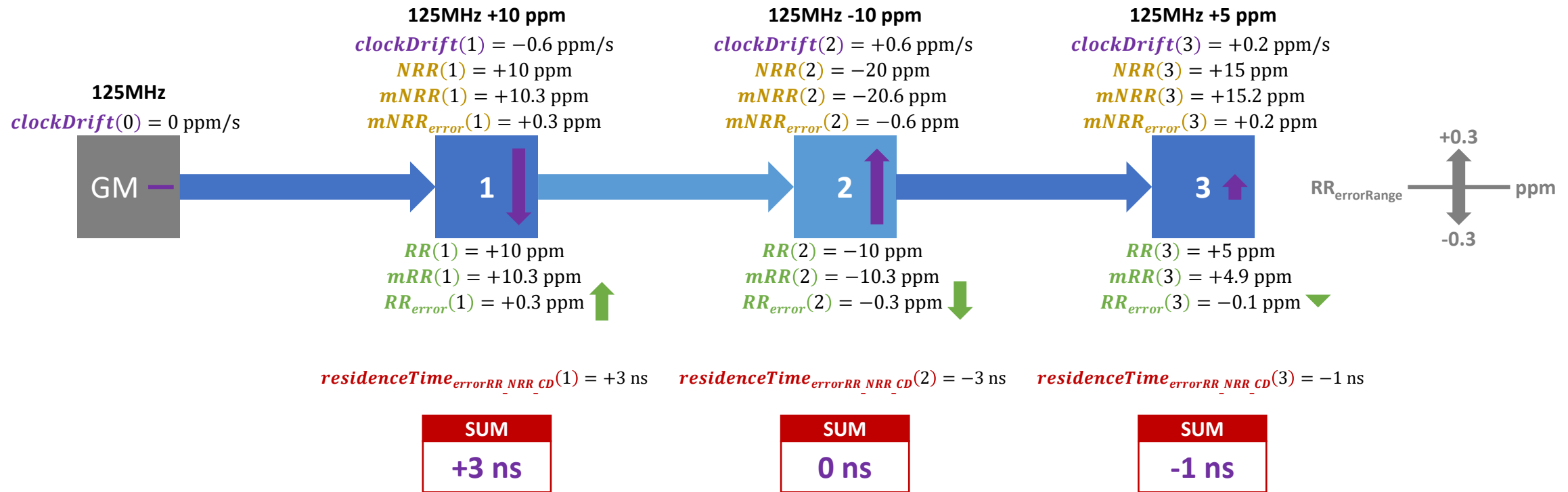


Input Errors		
GM Clock Drift Max	Variable	ppm/s
GM Clock Drift Min	Variable	ppm/s
Clock Drift (non-GM)	Variable	±ppm/s
Timestamp Granularity TX	4	±ns
Timestamp Granularity RX	4	±ns
Dynamic Time Stamp Error TX	4	±ns
Dynamic Time Stamp Error RX	4	±ns
Input Parameters		
pDelay Interval	1000	ms
pDelay Response Time	10	ms
residenceTime	10	ms
Input Correction Factors		
Mean Link Delay	0	%
Drift Rate	0	%
pDelayResponse → Sync	0	%
mNRR Smoothing	1	
Configuration		
Hops	100	
Runs	100,000	

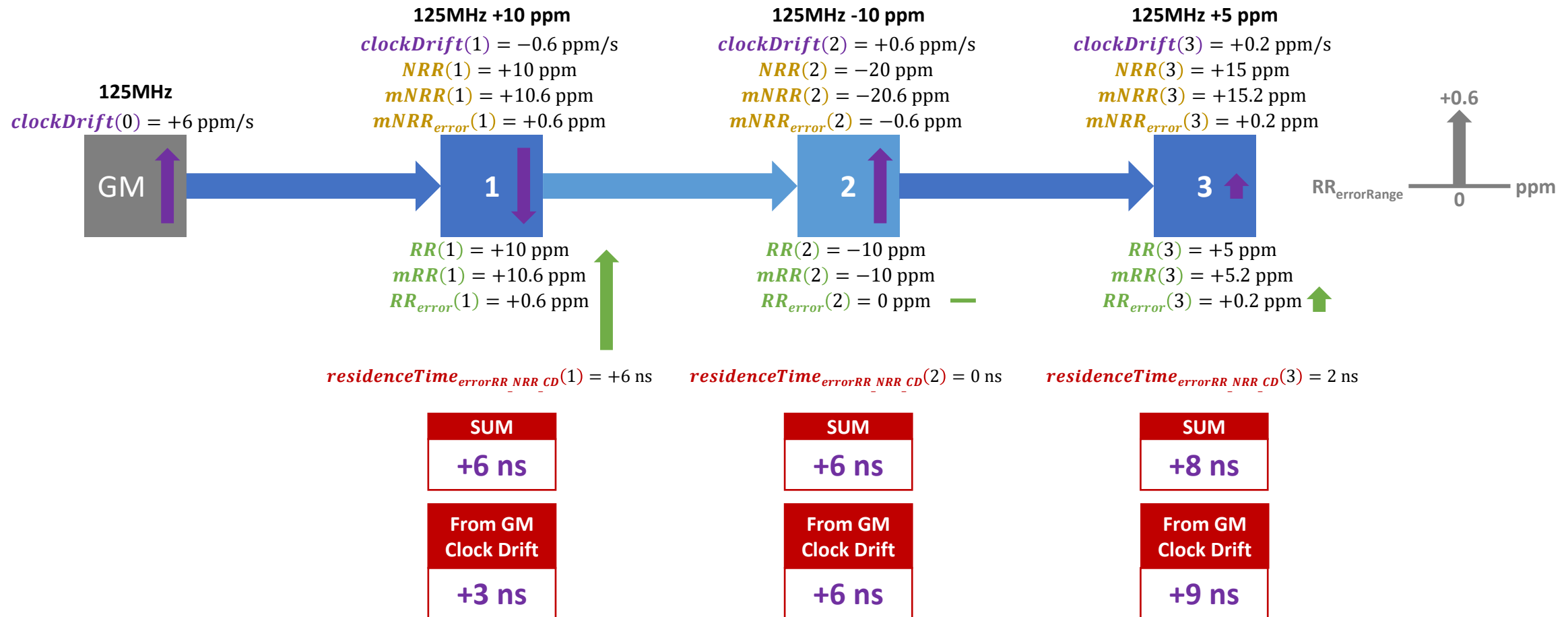
# Clock Drift Sensitivity



# How *residenceTime<sub>errorRR\_NRR\_CD</sub>* Accumulates

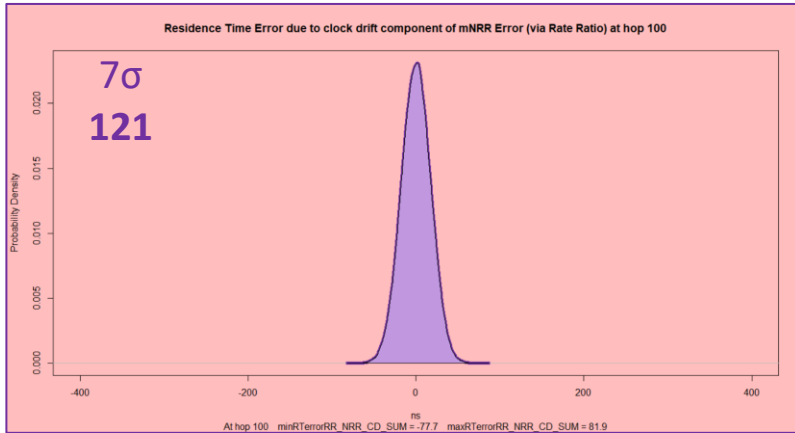


# How *residenceTime<sub>errorRR\_NRR\_CD</sub>* Accumulates

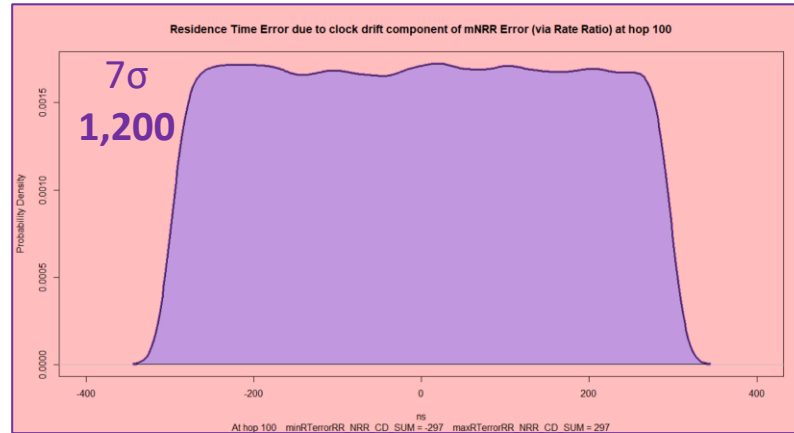




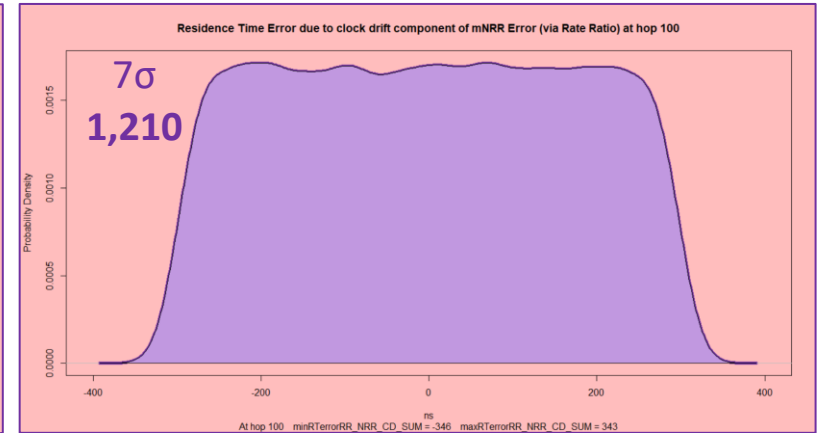
# *residenceTime*<sub>errorRR\_NRR\_CD</sub> at Hop 100



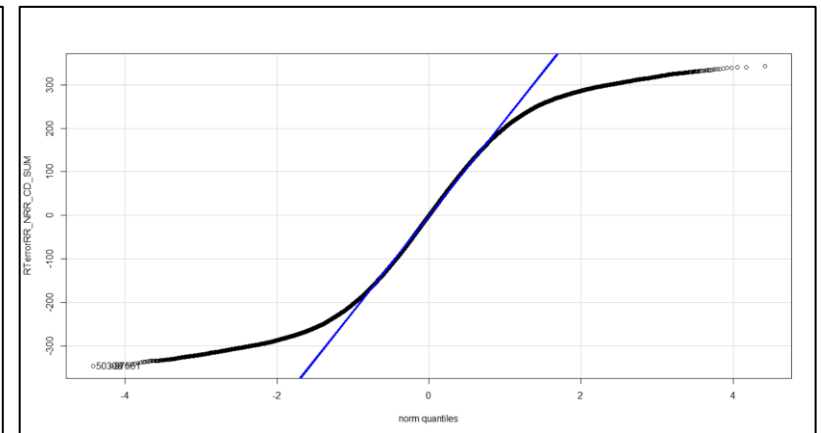
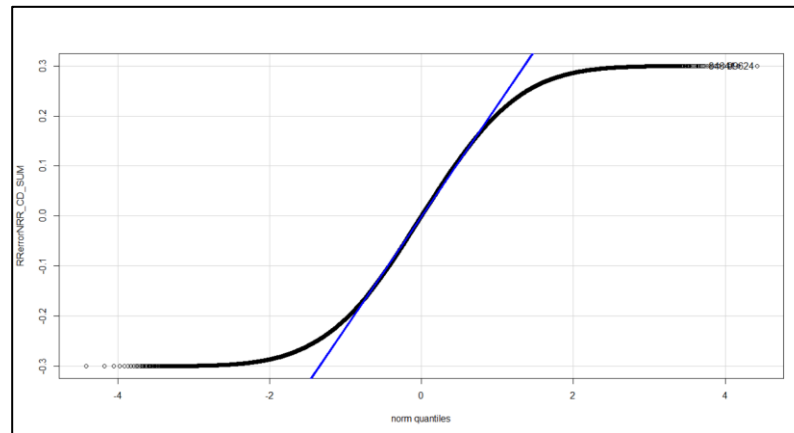
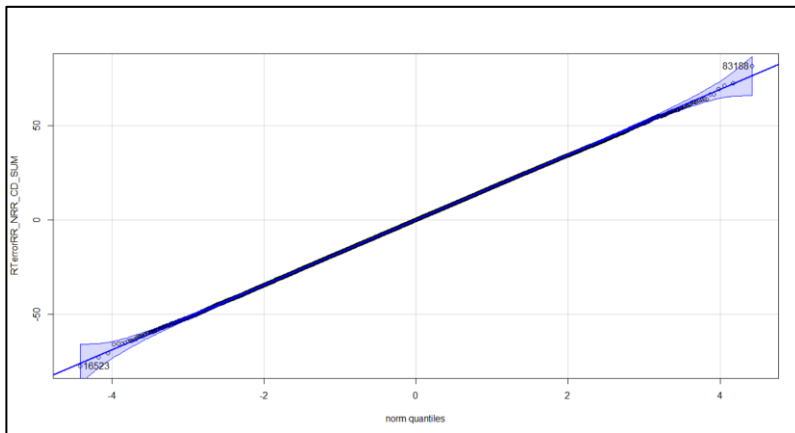
$clockDrift_{GM} = 0$  ppm/s  
 $clockDrift = \pm 0.6$  ppm/s



$clockDrift_{GM} = \pm 0.6$  ppm/s  
 $clockDrift = 0$  ppm/s



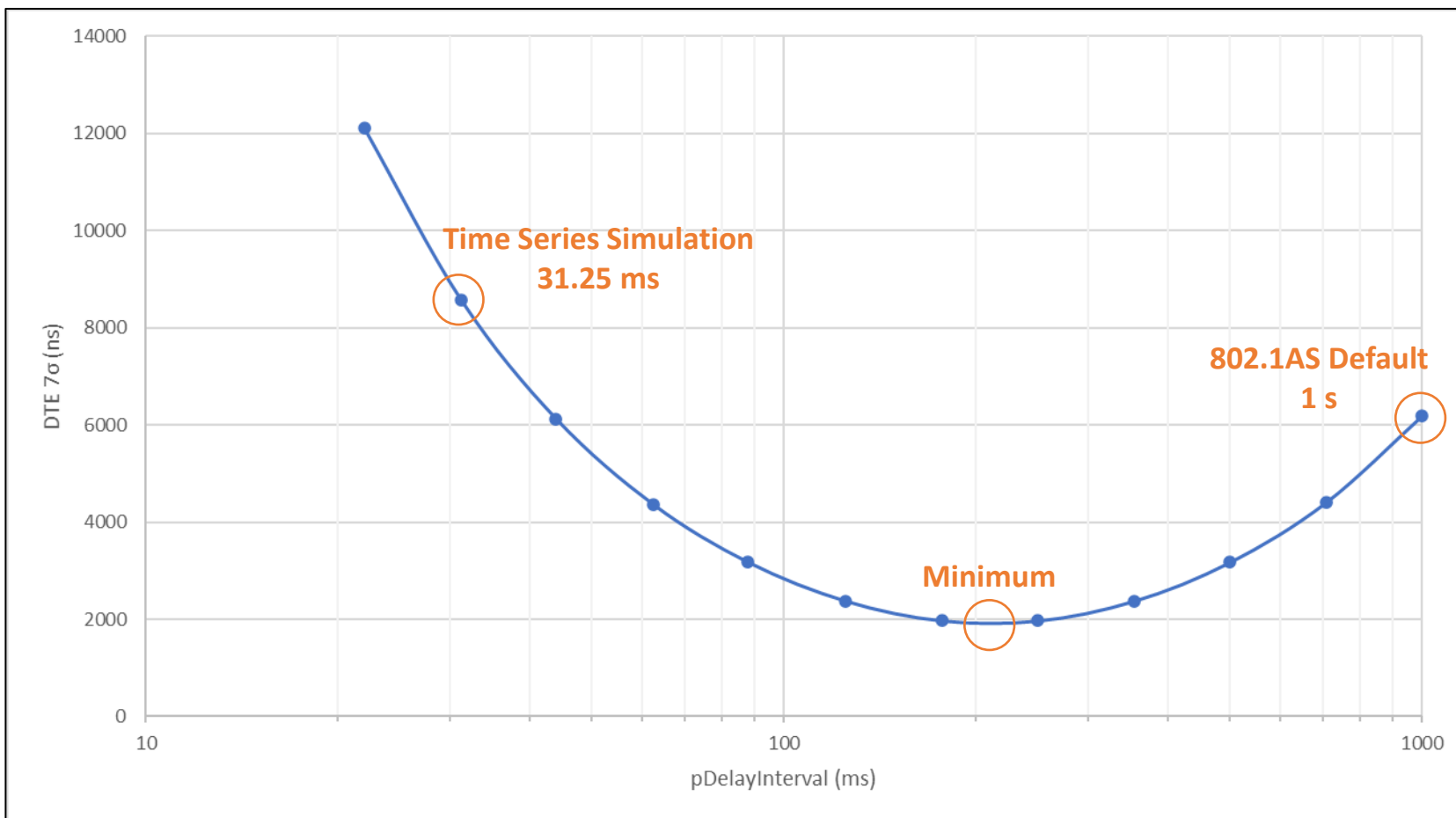
$clockDrift_{GM} = \pm 0.6$  ppm/s  
 $clockDrift = \pm 0.6$  ppm/s



# Timestamp Errors & Clock Drift Sensitivity

- DTE sensitivity to Timestamp Errors and Clock Drift varies depending on input parameters (and error correction factors – see next section).
  - Mainly depends on  $pDelayInterval$  (and  $driftRate_{errorCorrection}$ ) which have a big effect on ratio of DTE errors due to Timestamp Errors and Clock Drift.
- DTE response to Timestamp Errors is as intuition might suggest
  - If DTE is sensitive to Timestamp Errors, then reducing Timestamp Errors results in a proportional drop in DTE.
- DTE response to Clock Drift Errors is not intuitive
  - Depends on ratio of errors that are via direct effect on Rate Ratio (due to delay between NRR measurement and use;  $RT_{errorRR\_CD}$ ) vs. via effect on mNRR ( $RT_{errorRR\_NRR\_CD}$  and, to a lesser extent  $MLD_{errorNRR\_CD}$ ).
  - $RT_{errorRR\_NRR\_CD}$  is noteworthy because  $clockDrift_{GM}$  can easily be the most important factor (far more significant than clock drift at every other node combined).
    - In the Monte Carlo analysis, the significance of  $clockDrift_{GM}$ , if modelled as a uniform distribution, can also result in  $RT_{errorRR\_NRR\_CD}$  having a non-Gaussian distribution, which should be considered when using related  $7\sigma$  values as part of the analysis.

# *pDelayInterval* Sensitivity Analysis

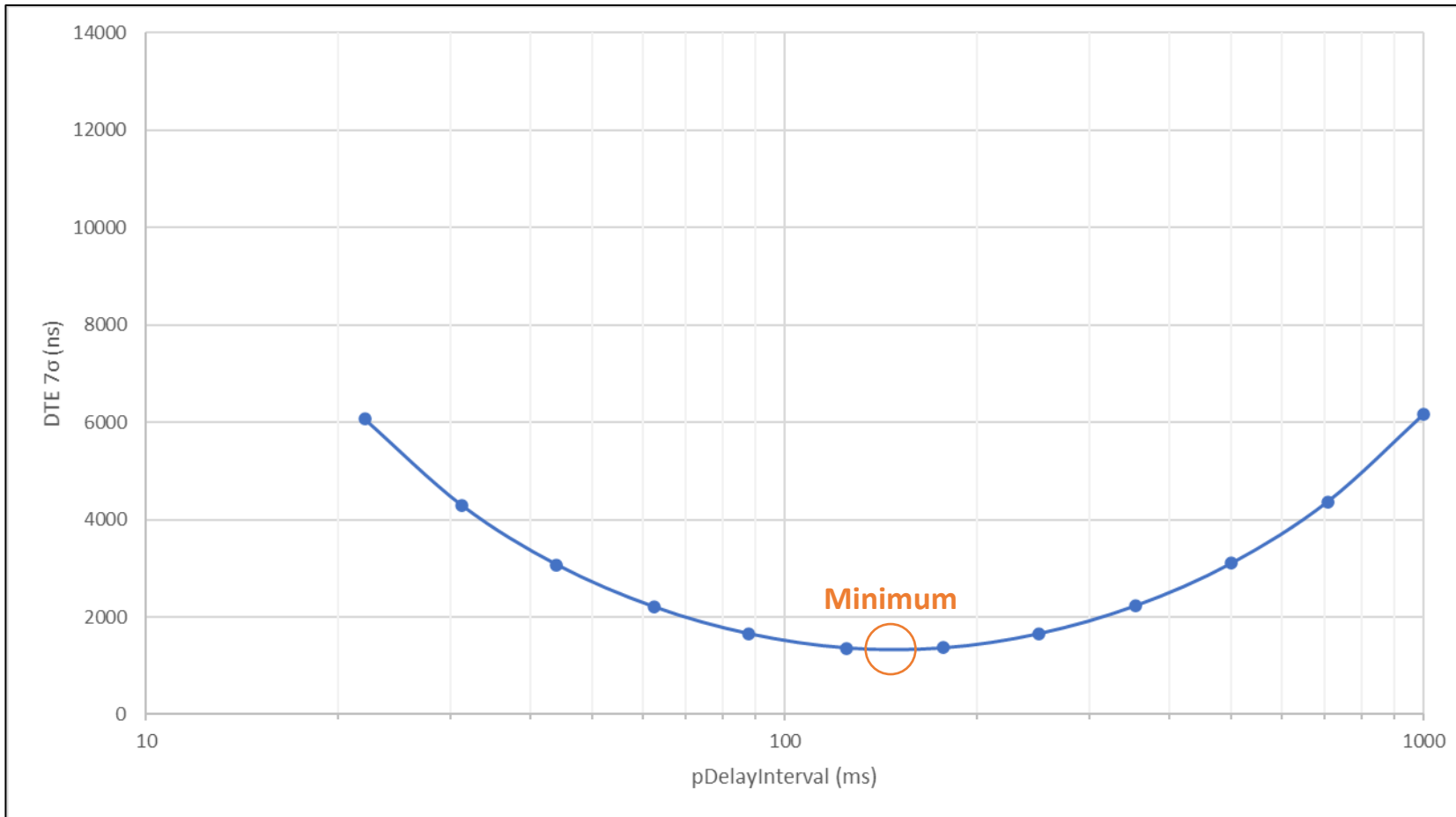


Input Errors		
GM Clock Drift Max	+0.6	ppm/s
GM Clock Drift Min	+0.6	ppm/s
Clock Drift (non-GM)	0.6	±ppm/s
Timestamp Granularity TX	4	±ns
Timestamp Granularity RX	4	±ns
Dynamic Time Stamp Error TX	4	±ns
Dynamic Time Stamp Error RX	4	±ns
Input Parameters		
pDelay Interval	Variable	ms
pDelay Response Time	10	ms
residenceTime	10	ms
Input Correction Factors		
Mean Link Delay	0	%
Drift Rate	0	%
pDelayResponse → Sync	0	%
mNRR Smoothing	1	
Configuration		
Hops	100	
Runs	100,000	

**Minimum is at approx 210 ms...**

**...for this set of parameters.**

# *pDelayInterval* Sensitivity Analysis with Lower Timestamp Error

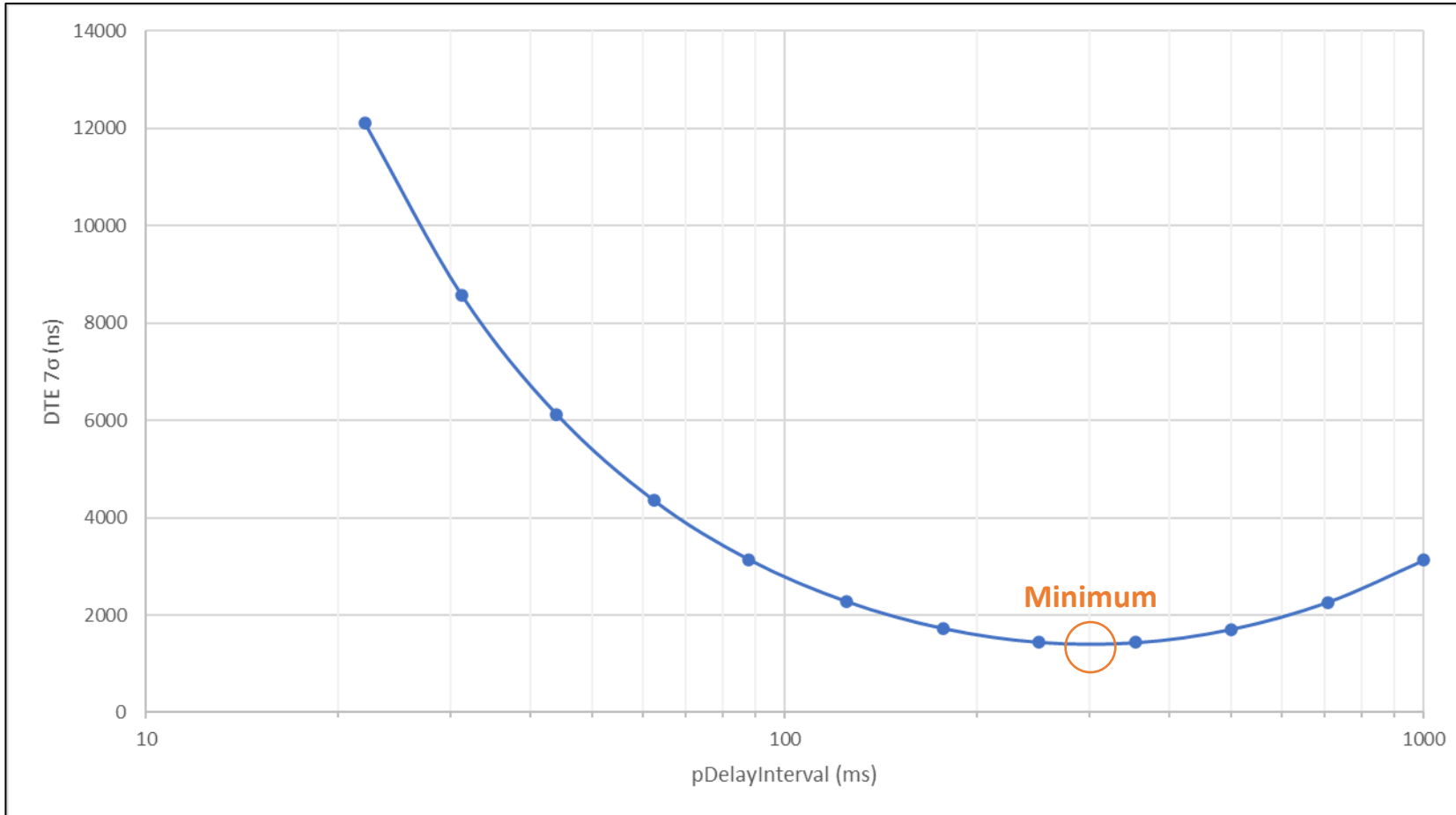


Input Errors		
GM Clock Drift Max	+0.6	ppm/s
GM Clock Drift Min	+0.6	ppm/s
Clock Drift (non-GM)	0.6	±ppm/s
Timestamp Granularity TX	2	±ns
Timestamp Granularity RX	2	±ns
Dynamic Time Stamp Error TX	2	±ns
Dynamic Time Stamp Error RX	2	±ns
Input Parameters		
pDelay Interval	Variable	ms
pDelay Response Time	10	ms
residenceTime	10	ms
Input Correction Factors		
Mean Link Delay	0	%
Drift Rate	0	%
pDelayResponse → Sync	0	%
mNRR Smoothing	1	
Configuration		
Hops	100	
Runs	100,000	

**Minimum is at approx 150ms...**

**...for this set of parameters.**

# *pDelayInterval* Sensitivity Analysis with Lower Clock Drift



Input Errors		
GM Clock Drift Max	+0.3	ppm/s
GM Clock Drift Min	+0.3	ppm/s
Clock Drift (non-GM)	0.3	±ppm/s
Timestamp Granularity TX	4	±ns
Timestamp Granularity RX	4	±ns
Dynamic Time Stamp Error TX	4	±ns
Dynamic Time Stamp Error RX	4	±ns
Input Parameters		
pDelay Interval	Variable	ms
pDelay Response Time	10	ms
residenceTime	10	ms
Input Correction Factors		
Mean Link Delay	0	%
Drift Rate	0	%
pDelayResponse → Sync	0	%
mNRR Smoothing	1	
Configuration		
Hops	100	
Runs	100,000	

**Minimum is at approx 300ms...**

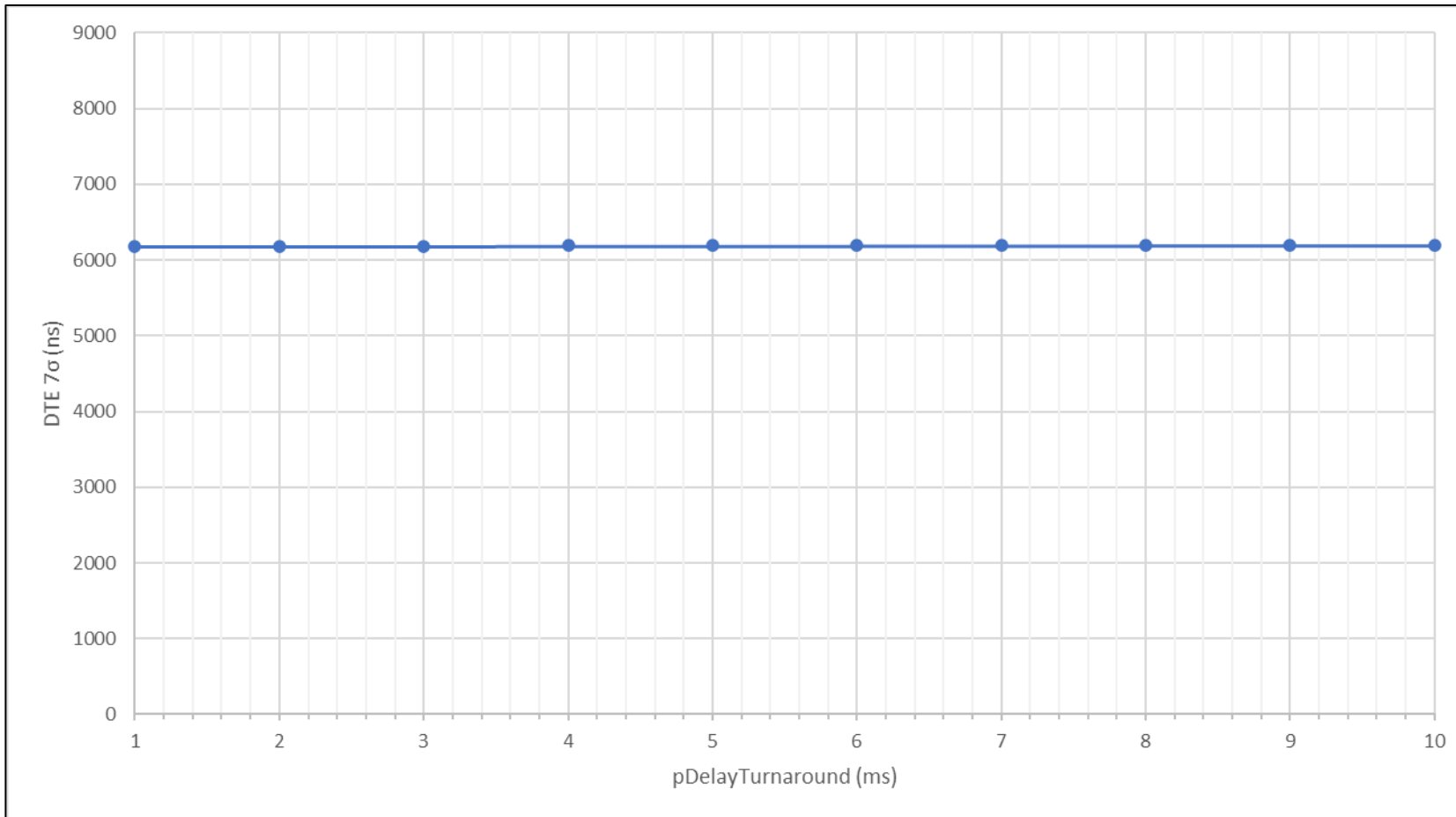
**...for this set of parameters.**

# *pDelayInterval* Sensitivity - Conclusions

- Choice of *pDelayInterval* can have a large impact on DTE.
  - Also on which components contribute most to DTE. Low *pDelayInterval* favours increased contribution from Timestamp Errors; high *pDelayInterval* favours increased contribution from Clock Drift related errors.
- pDelay interval can be optimised but the optimal choice depends on other parameters and sources of error.
- Monte Carlo Analysis is an effective tool for investigating this further.

# *pDelayTurnaround* Sensitivity Analysis

# *pDelayTurnaround* Sensitivity – 1 s pDelay Interval

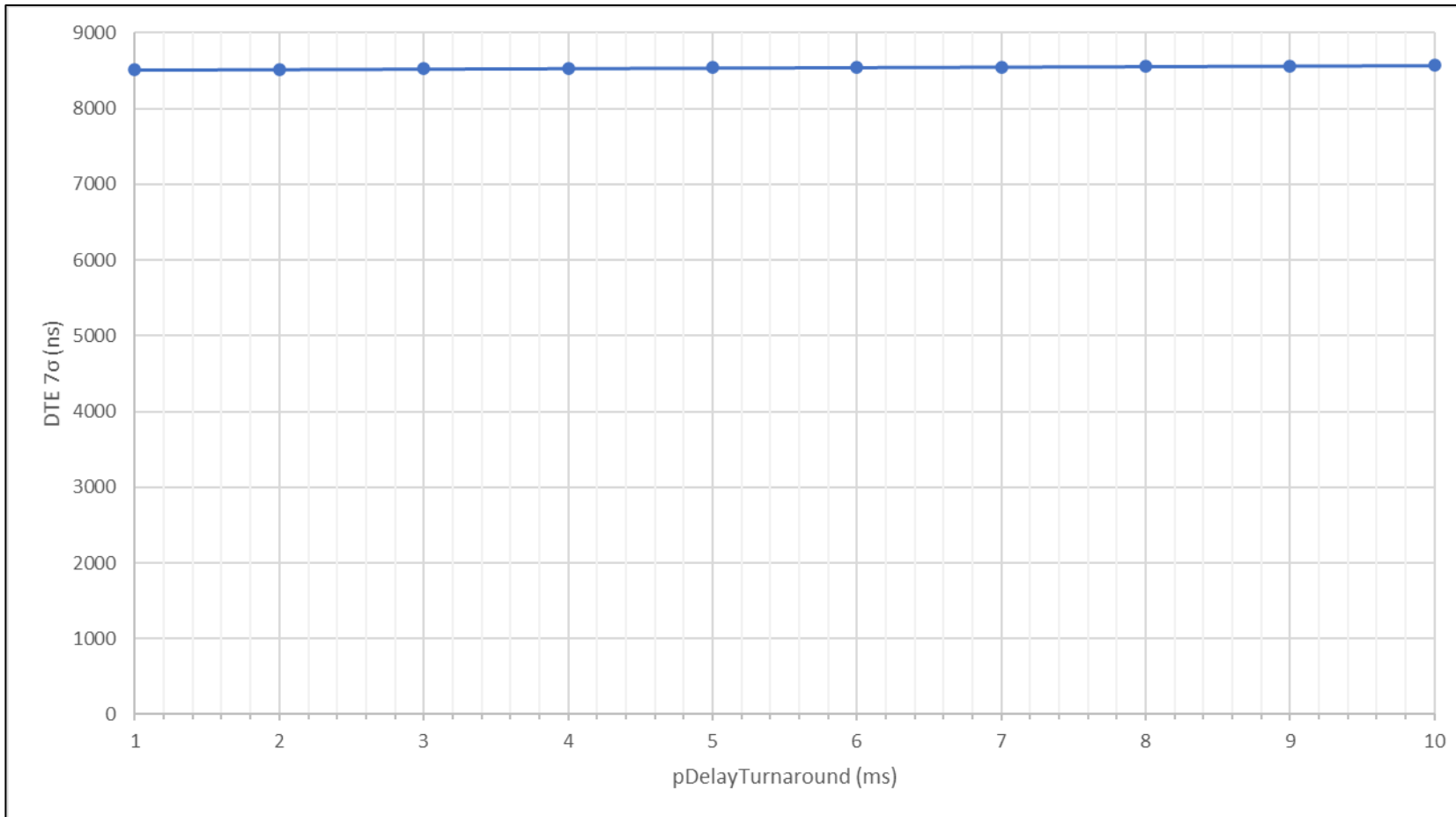


Input Errors		
GM Clock Drift Max	+0.6	ppm/s
GM Clock Drift Min	+0.6	ppm/s
Clock Drift (non-GM)	0.6	±ppm/s
Timestamp Granularity TX	4	±ns
Timestamp Granularity RX	4	±ns
Dynamic Time Stamp Error TX	4	±ns
Dynamic Time Stamp Error RX	4	±ns
Input Parameters		
pDelay Interval	1000	ms
pDelay Response Time	Variable	ms
residenceTime	10	ms
Input Correction Factors		
Mean Link Delay	0	%
Drift Rate	0	%
pDelayResponse → Sync	0	%
mNRR Smoothing	1	
Configuration		
Hops	100	
Runs	100,000	

**DTE is not sensitive to  
pDelayTurnaround when  
pDelayInterval is high.**



# *pDelayTurnaround* Sensitivity – 31.25 ms pDelay Interval



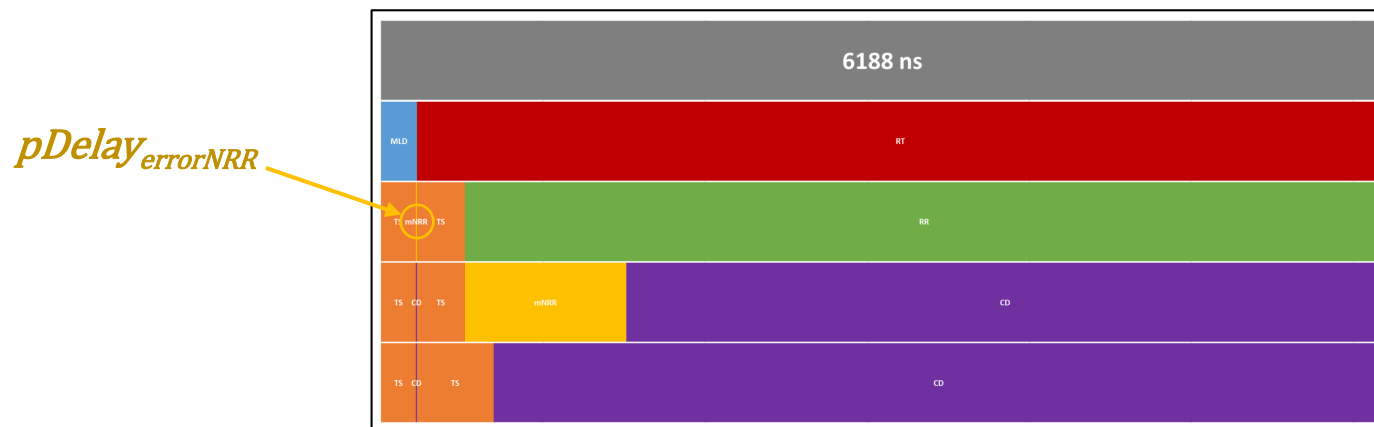
Input Errors		
GM Clock Drift Max	+0.6	ppm/s
GM Clock Drift Min	+0.6	ppm/s
Clock Drift (non-GM)	0.6	±ppm/s
Timestamp Granularity TX	4	±ns
Timestamp Granularity RX	4	±ns
Dynamic Time Stamp Error TX	4	±ns
Dynamic Time Stamp Error RX	4	±ns
Input Parameters		
pDelay Interval	<b>31.25</b>	ms
pDelay Response Time	Variable	ms
residenceTime	10	ms
Input Correction Factors		
Mean Link Delay	0	%
Drift Rate	0	%
pDelayResponse → Sync	0	%
mNRR Smoothing	1	
Configuration		
Hops	100	
Runs	100,000	

**And DTE is not sensitive to pDelayTurnaround when pDelayInterval is low.**

# *pDelayTurnaround* Sensitivity - Conclusions

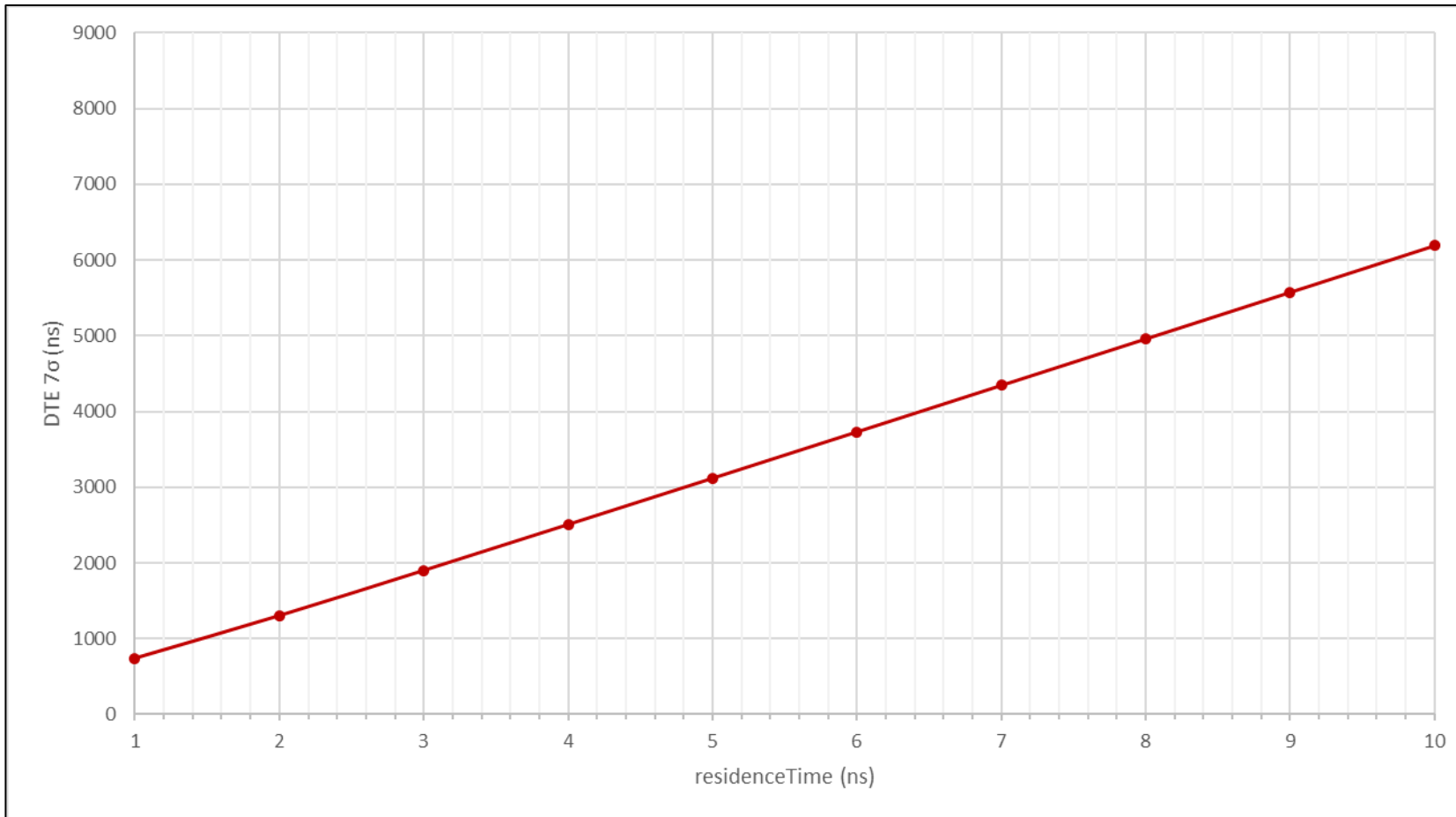
- DTE is, in general, not sensitive to *pDelayTurnaround*.
- This is not surprising as the only error where *pDelayTurnaround* plays a role is  $pDelay_{errorNRR}$ , which is a very small part of DTE.

$$pDelay_{errorNRR} = mNRR_{error} \left( \frac{pDelayTurnaround}{2} \right)$$



# *residenceTime* Sensitivity Analysis

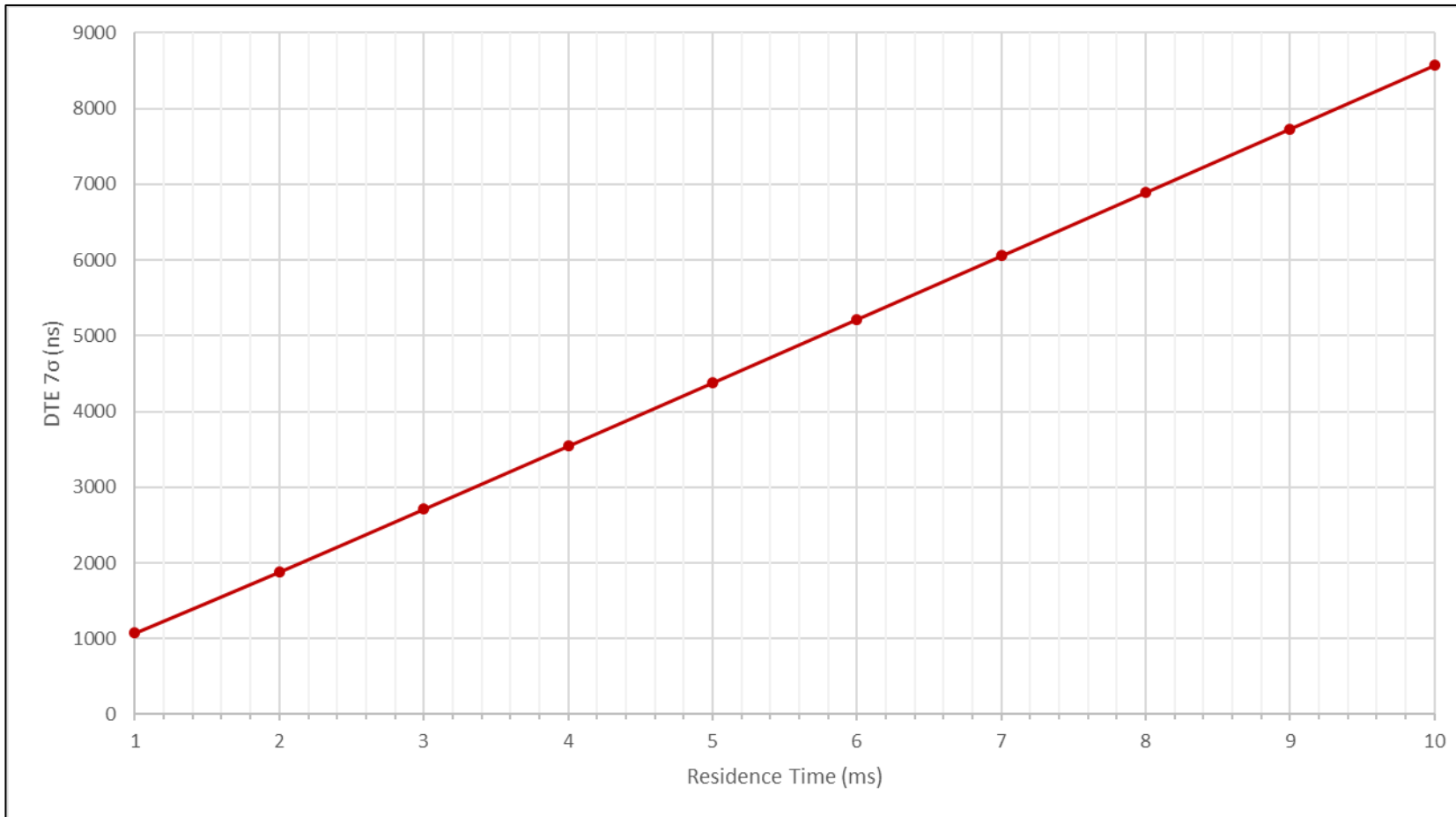
# *residenceTime* Sensitivity – 1 s pDelay Interval



Input Errors		
GM Clock Drift Max	+0.6	ppm/s
GM Clock Drift Min	+0.6	ppm/s
Clock Drift (non-GM)	0.6	±ppm/s
Timestamp Granularity TX	4	±ns
Timestamp Granularity RX	4	±ns
Dynamic Time Stamp Error TX	4	±ns
Dynamic Time Stamp Error RX	4	±ns
Input Parameters		
pDelay Interval	<b>1000</b>	ms
pDelay Response Time	10	ms
residenceTime	<b>Variable</b>	ms
Input Correction Factors		
Mean Link Delay	0	%
Drift Rate	0	%
pDelayResponse → Sync	0	%
mNRR Smoothing	1	
Configuration		
Hops	100	
Runs	100,000	

**Lower Residence Time is better.**

# *residenceTime* Sensitivity – 31.25 ms pDelay Interval



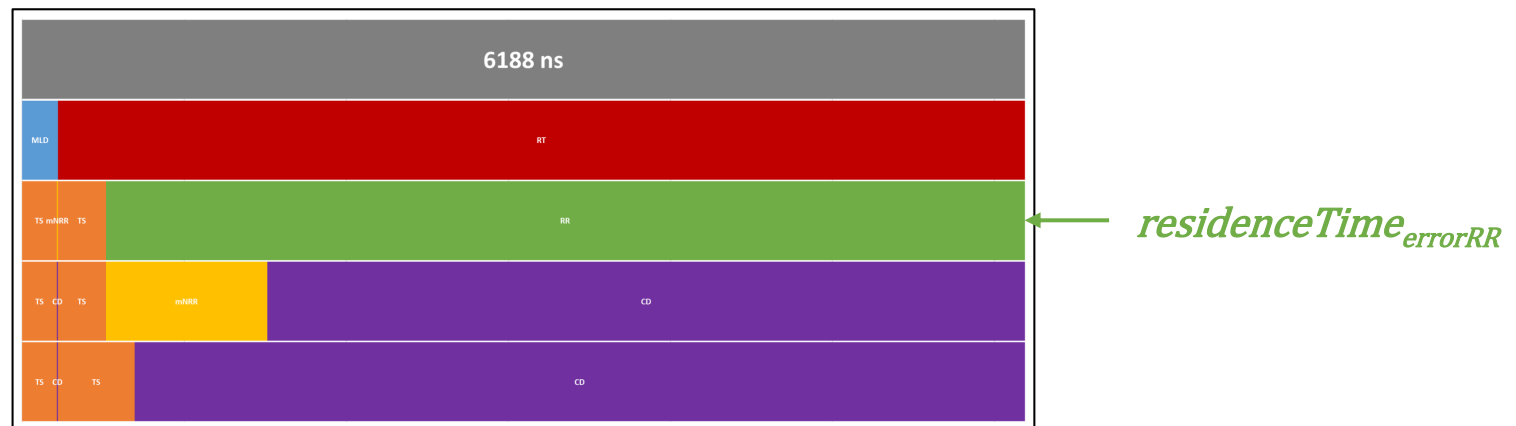
Input Errors		
GM Clock Drift Max	+0.6	ppm/s
GM Clock Drift Min	+0.6	ppm/s
Clock Drift (non-GM)	0.6	±ppm/s
Timestamp Granularity TX	4	±ns
Timestamp Granularity RX	4	±ns
Dynamic Time Stamp Error TX	4	±ns
Dynamic Time Stamp Error RX	4	±ns
Input Parameters		
pDelay Interval	<b>31.25</b>	ms
pDelay Response Time	10	ms
residenceTime	<b>Variable</b>	ms
Input Correction Factors		
Mean Link Delay	0	%
Drift Rate	0	%
pDelayResponse → Sync	0	%
mNRR Smoothing	1	
Configuration		
Hops	100	
Runs	100,000	

**Lower Residence Time is better...**  
**...proportional to the size of**  
*residenceTime<sub>errorRR</sub>*

# *residenceTime* Sensitivity - Conclusions

- DTE is often highly sensitive to *residenceTime*.
- This is not surprising as  $RT_{errorRR}$ , which can be a large part of DTE, is proportional to *residenceTime*.

$$residenceTime_{errorRR} = RR_{error} \times (residenceTime)$$



# Reducing Dynamic Time Error

Parameters & Correction Factors

# Approaches to Reducing Dynamic Time Error

- Address Sources of Error
  - Reduce Timestamp Error
  - Reduce Clock Drift
    - Reduce GM Clock Drift specifically
  - Align pDelay messaging just ahead of Sync messaging
- Adjust Parameters
  - Reduce Residence Time
  - Optimise pDelayInterval
- Algorithmically
  - mNRR smoothing (use Nth prior pDelay message's timestamp)
  - Average Mean Link Delay Error
  - Measure and compensate for Clock Drift



# Approaches to Reducing Dynamic Time Error

## Address Sources of Error

Reduce Timestamp Error

Reduce Clock Drift

Align pDelay messaging just ahead of Sync messaging

## Alter Parameters

Reduce Residence Time

Optimise pDelayInterval

## Algorithmic Improvements

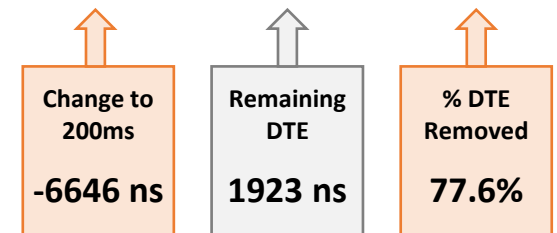
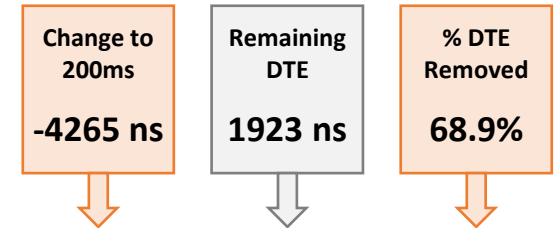
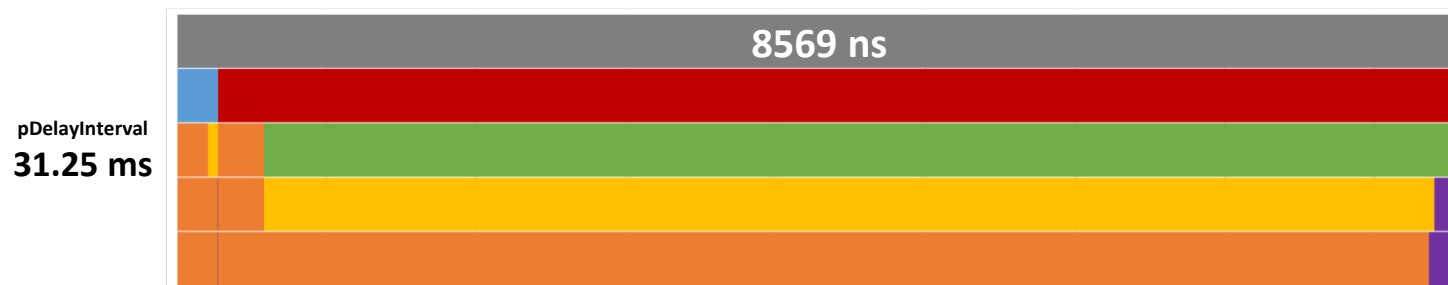
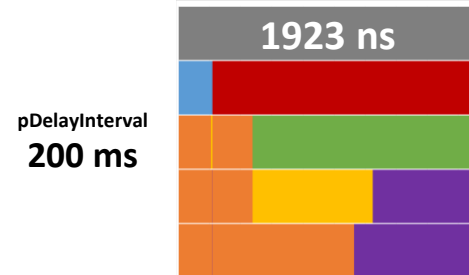
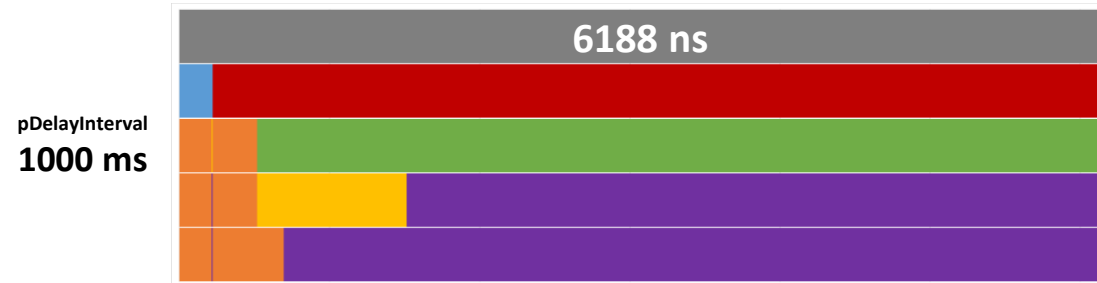
mNRR Smoothing (use  $n^{\text{th}}$  previous pDelay message's timestamp)

Average Mean Link Delay

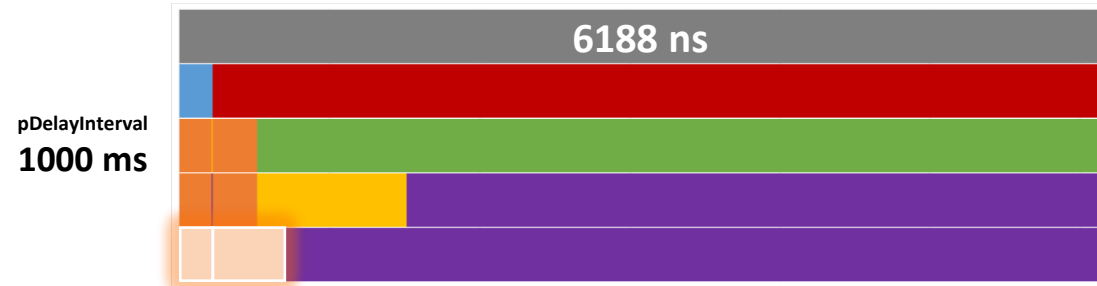
Measure and Compensate for Clock Drift

- Affect different error paths
  - Different % of DTE
- Have different costs and tradeoffs
- Have different likely effectiveness
- Can be combined...which means they will interact with each other

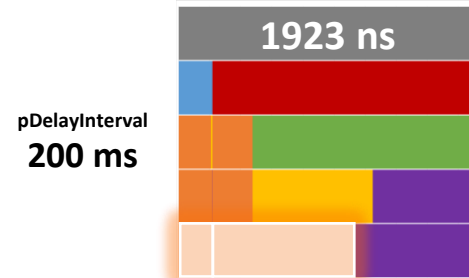
# Different Error Paths – Optimise pDelay Interval



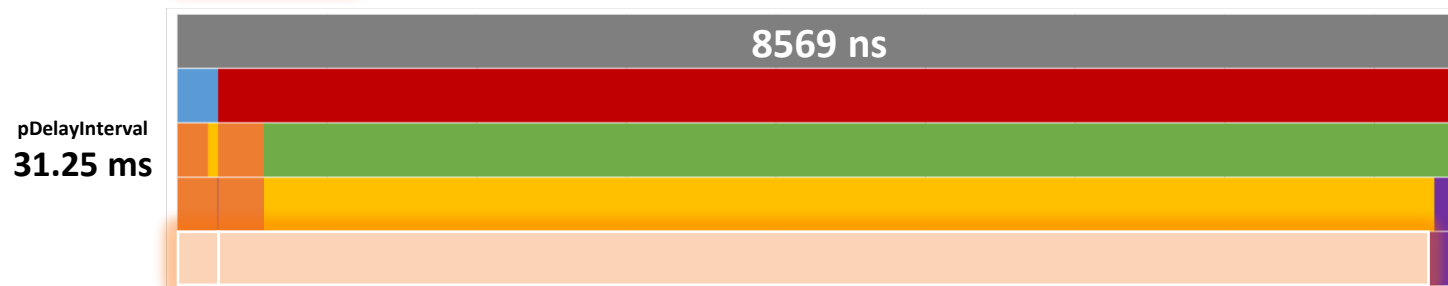
# Different Error Paths – Reduce Timestamp Errors



If 100% Successful	Remaining DTE	% DTE Removed
-10 ns	6178 ns	0.2%

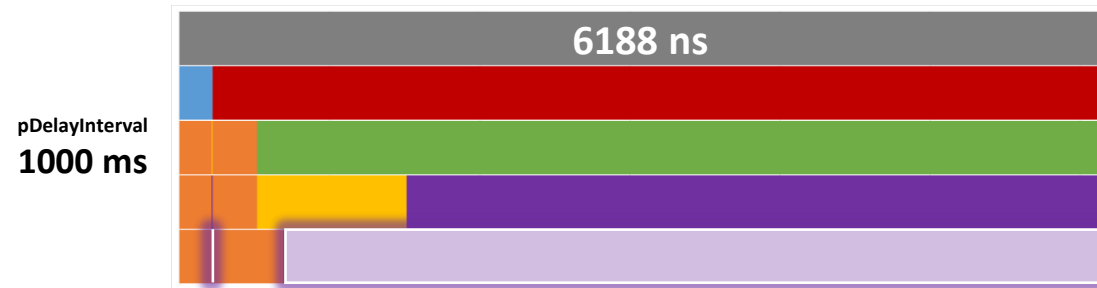


If 100% Successful	Remaining DTE	% DTE Removed
-687 ns	1236 ns	35.7%

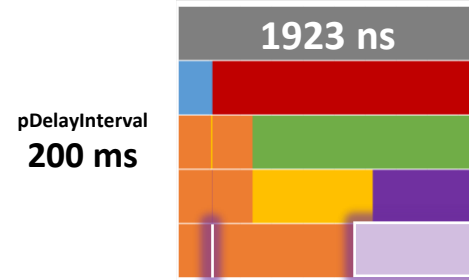


If 100% Successful	Remaining DTE	% DTE Removed
-8376 ns	193 ns	97.7%

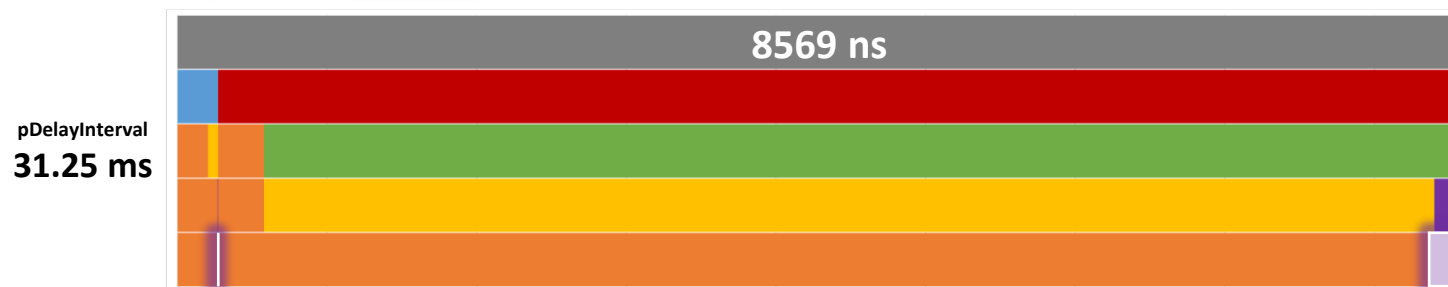
# Different Error Paths – Reduce Only GM Clock Drift



If 100% Successful	Remaining DTE	% DTE Removed
-521 ns	5667 ns	8.4%

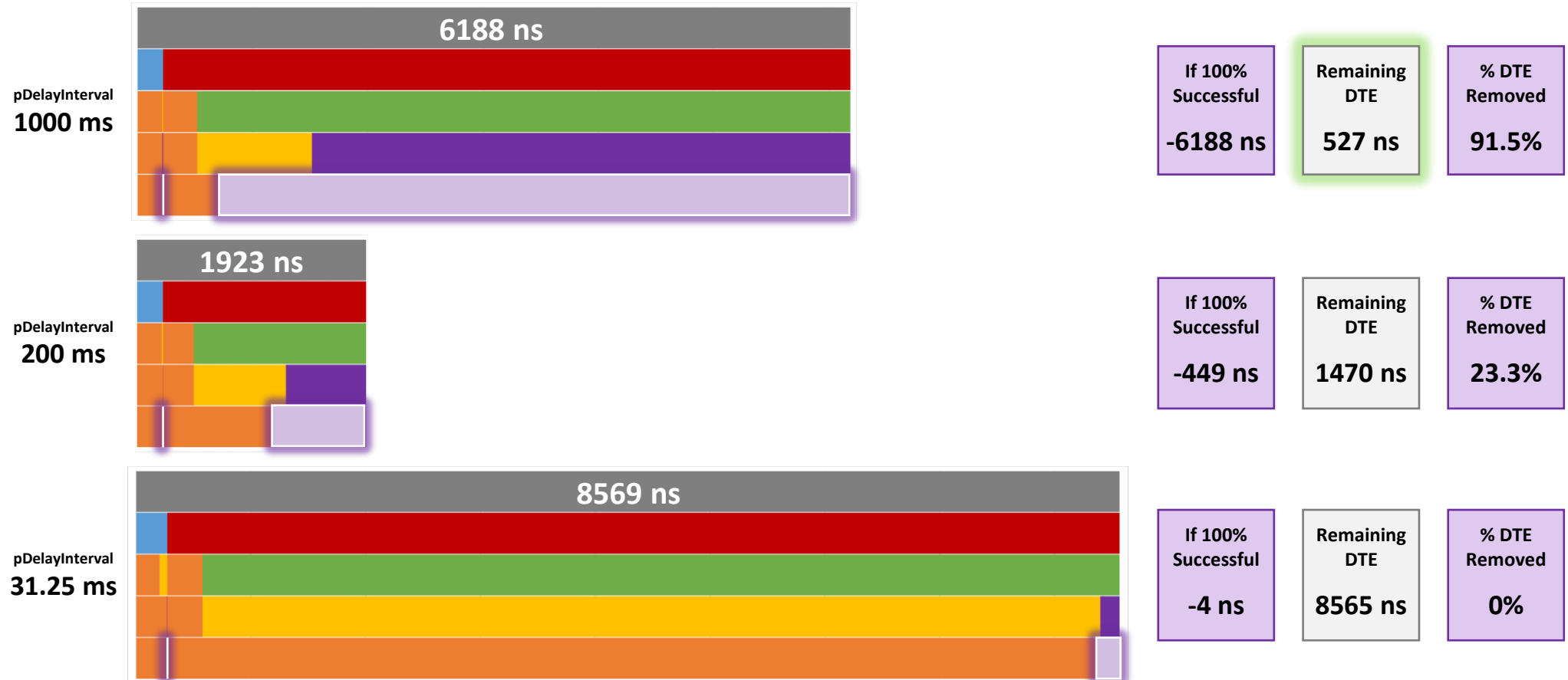


If 100% Successful	Remaining DTE	% DTE Removed
-65 ns	1858 ns	3.4%

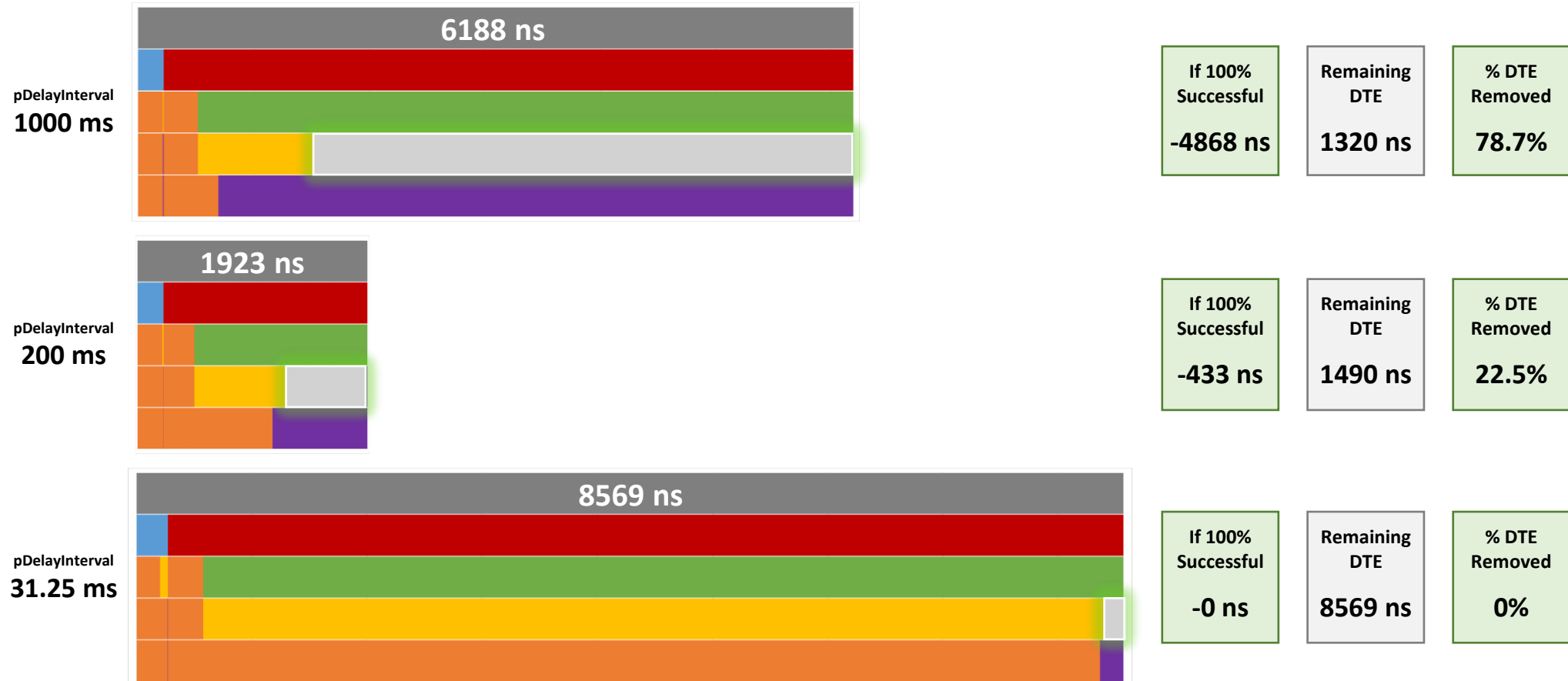


If 100% Successful	Remaining DTE	% DTE Removed
-1 ns	8568 ns	0%

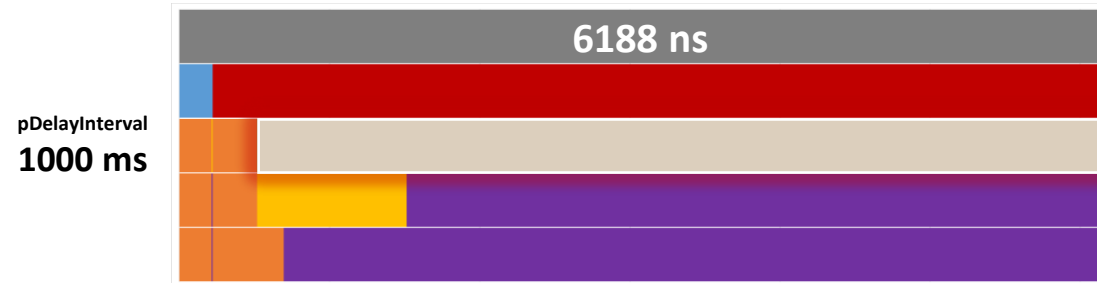
# Different Error Paths – Reduce All Clock Drift



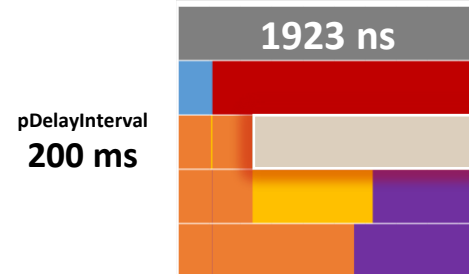
# Different Error Paths – Align pDelay and Sync Messaging



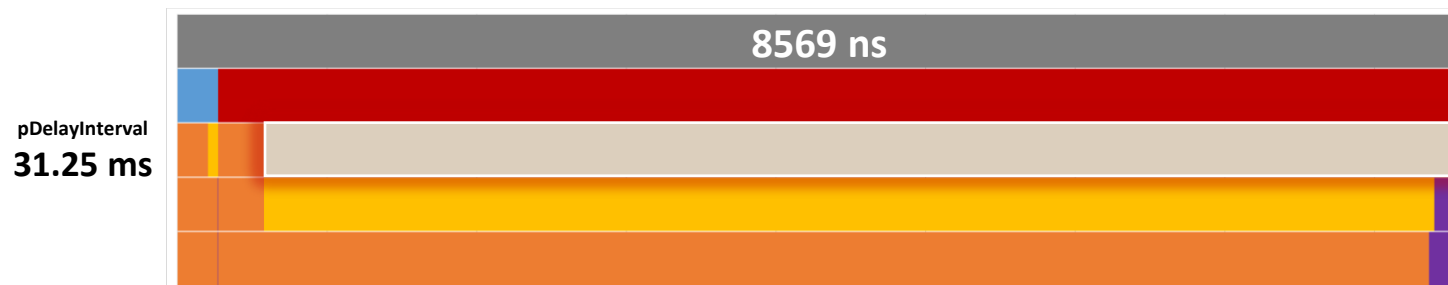
# Different Error Paths – Reduce Residence Time



If 100% Successful	Remaining DTE	% DTE Removed
-5793 ns	395 ns	93.6%

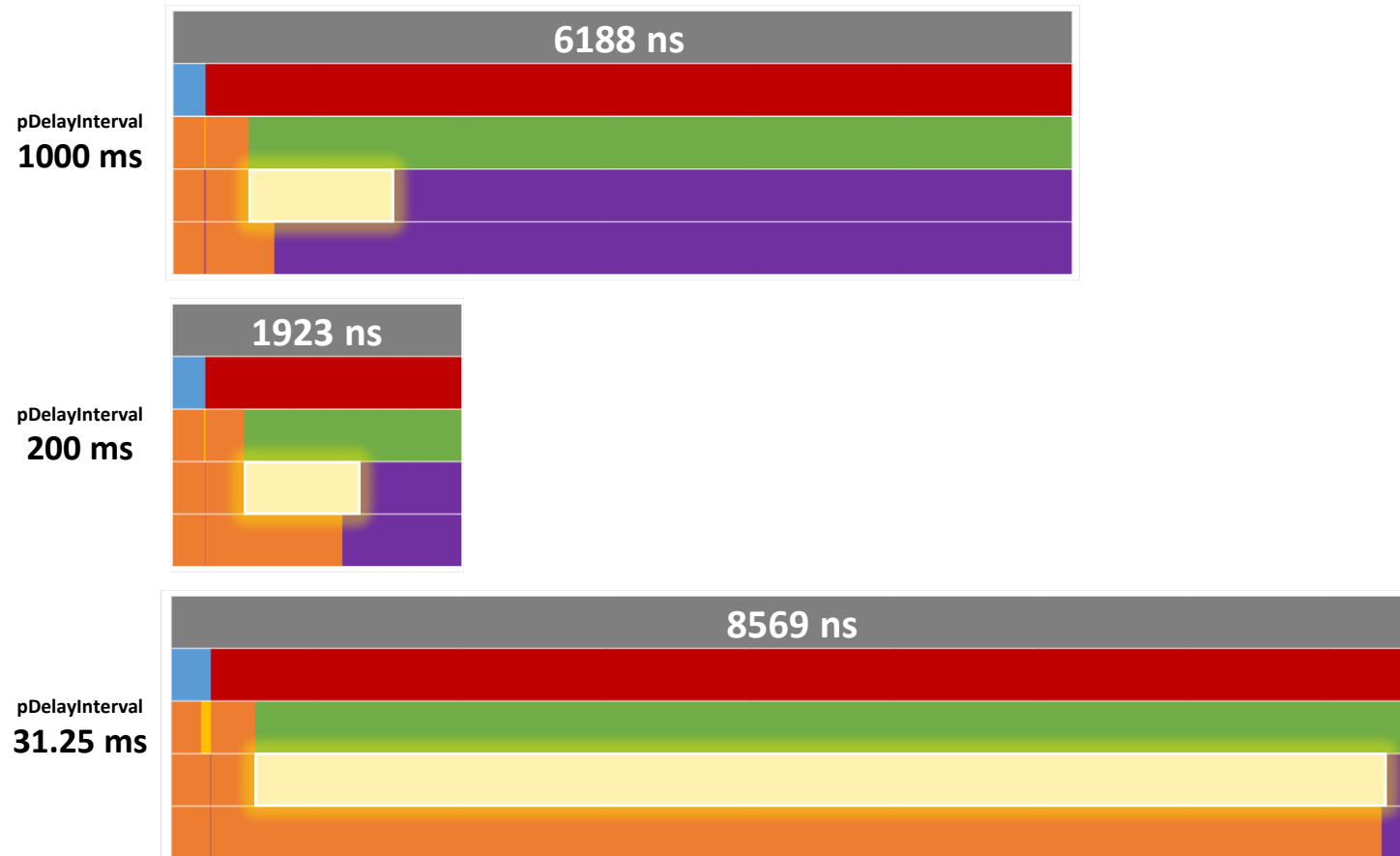


If 100% Successful	Remaining DTE	% DTE Removed
-1526 ns	397 ns	79.4%



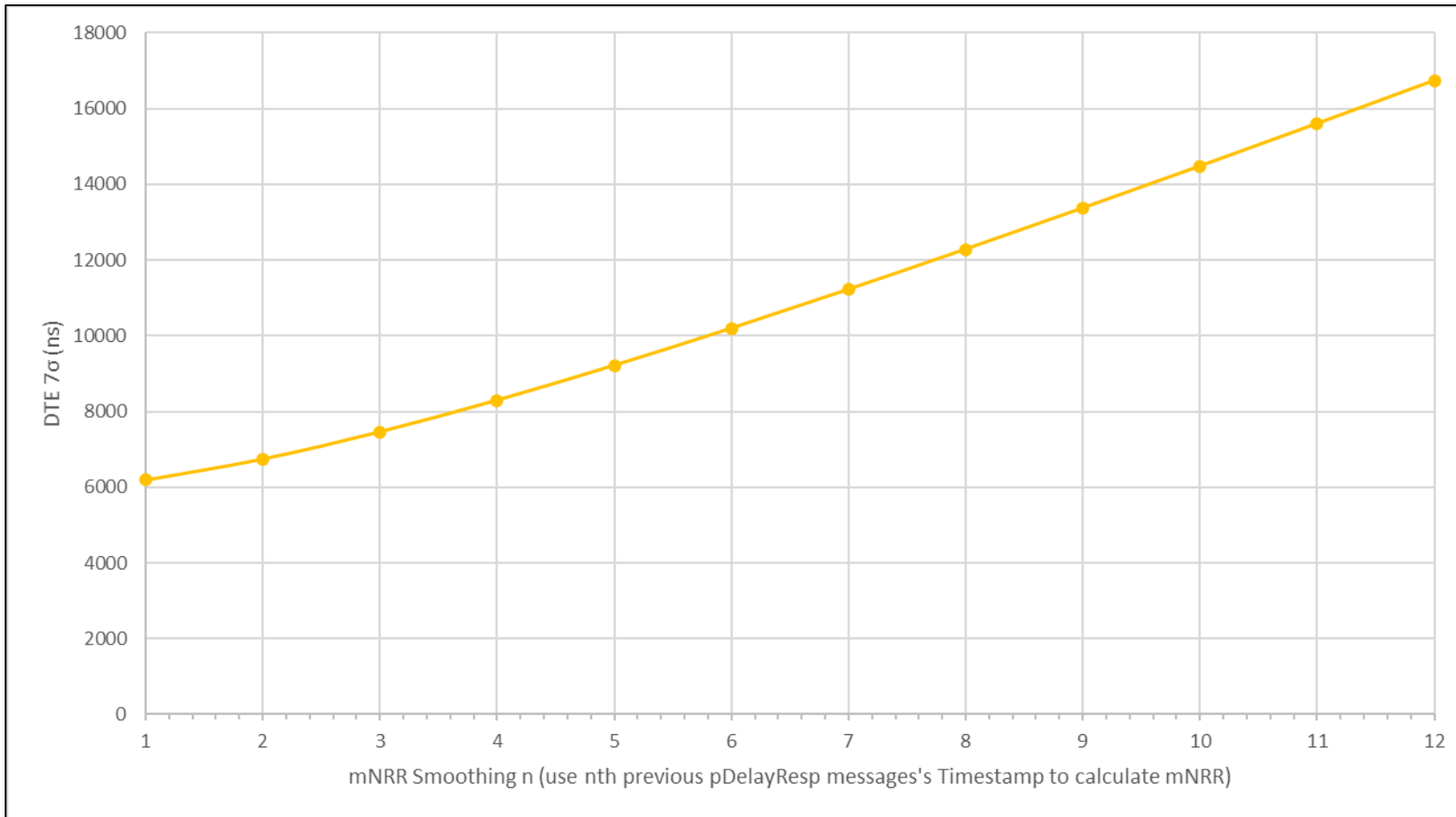
If 100% Successful	Remaining DTE	% DTE Removed
-8148 ns	421 ns	95.1%

# Different Error Paths – mNRR Smoothing





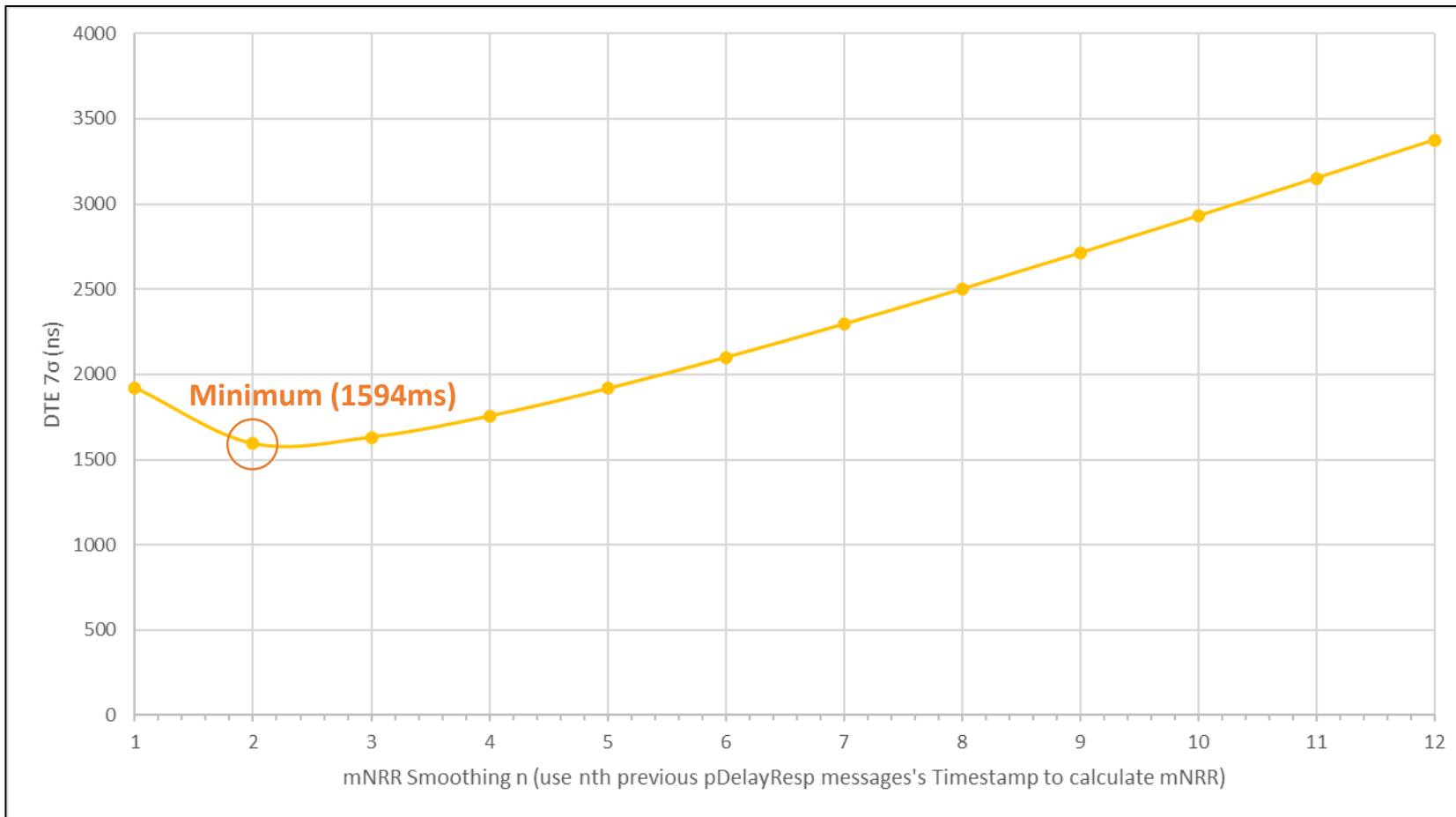
# Different Error Paths – mNRR Smoothing – 1s pDelay Interval



Input Errors		
GM Clock Drift Max	+0.6	ppm/s
GM Clock Drift Min	-0.6	ppm/s
Clock Drift (non-GM)	0.6	±ppm/s
Timestamp Granularity TX	4	±ns
Timestamp Granularity RX	4	±ns
Dynamic Time Stamp Error TX	4	±ns
Dynamic Time Stamp Error RX	4	±ns
Input Parameters		
pDelay Interval	1000	ms
pDelay Response Time	10	ms
residenceTime	10	ms
Input Correction Factors		
Mean Link Delay	0	%
Drift Rate	0	%
pDelayResponse → Sync	0	%
mNRR Smoothing	Variable	
Configuration		
Hops	100	
Runs	100,000	

**mNRR smoothing doesn't help  
when  $RT_{errorRR\_NRR}$  is already  
dominated by errors due to Clock  
Drift ( $RT_{errorRR\_NRR\_CD}$ )**

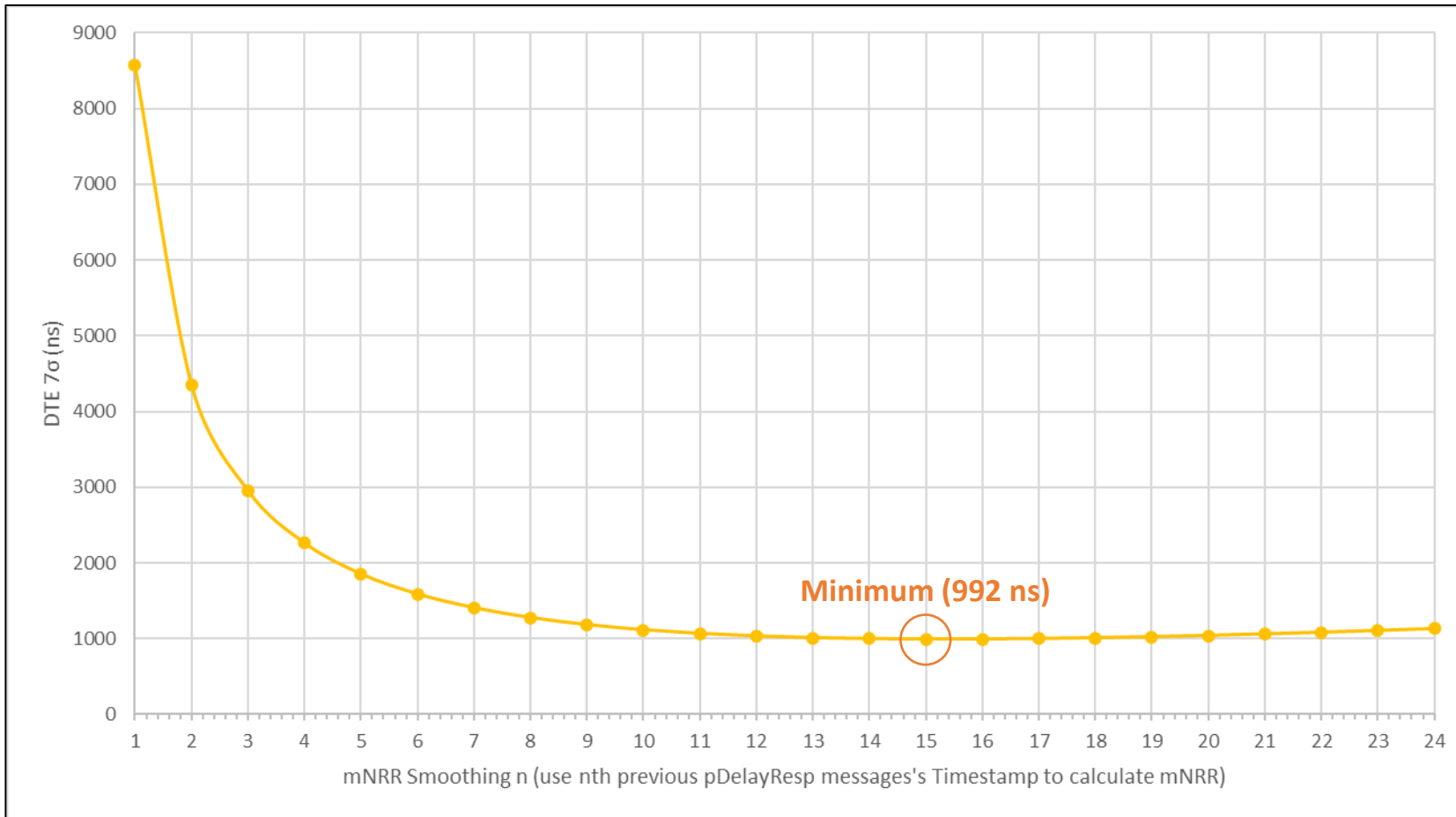
# Different Error Paths – mNRR Smoothing – 200ms pDelay Interval



Input Errors		
GM Clock Drift Max	+0.6	ppm/s
GM Clock Drift Min	-0.6	ppm/s
Clock Drift (non-GM)	0.6	±ppm/s
Timestamp Granularity TX	4	±ns
Timestamp Granularity RX	4	±ns
Dynamic Time Stamp Error TX	4	±ns
Dynamic Time Stamp Error RX	4	±ns
Input Parameters		
pDelay Interval	<b>31.25</b>	ms
pDelay Response Time	10	ms
residenceTime	10	ms
Input Correction Factors		
Mean Link Delay	0	%
Drift Rate	0	%
pDelayResponse → Sync	0	%
mNRR Smoothing	<b>Variable</b>	
Configuration		
Hops	100	
Runs	100,000	

**mNRR smoothing may help a bit when *pDelayInterval* is optimised (for these parameters at least) for low values of n, but as n rises the errors due to clock drift soon outweigh the benefits of reduced Timestamp-related errors**

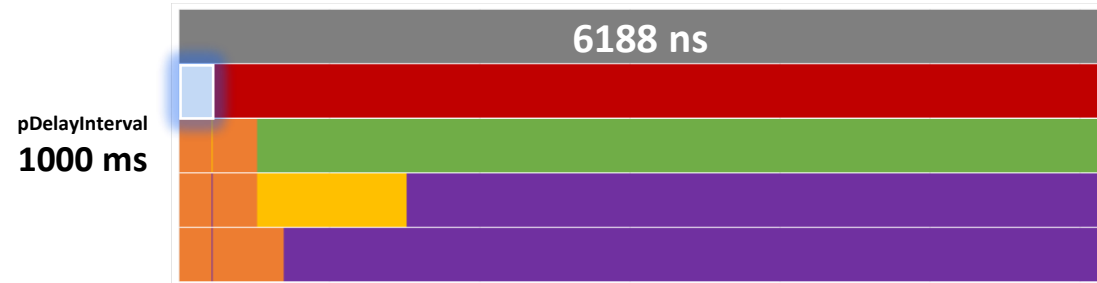
# Different Error Paths – mNRR Smoothing – 31.25ms pDelay Interval



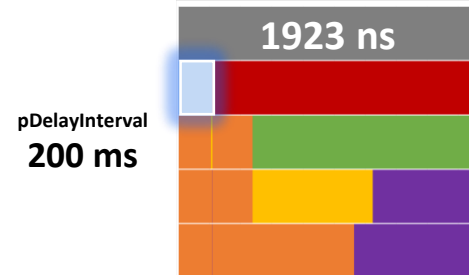
Input Errors		
GM Clock Drift Max	+0.6	ppm/s
GM Clock Drift Min	-0.6	ppm/s
Clock Drift (non-GM)	0.6	±ppm/s
Timestamp Granularity TX	4	±ns
Timestamp Granularity RX	4	±ns
Dynamic Time Stamp Error TX	4	±ns
Dynamic Time Stamp Error RX	4	±ns
Input Parameters		
pDelay Interval	31.25	ms
pDelay Response Time	10	ms
residenceTime	10	ms
Input Correction Factors		
Mean Link Delay	0	%
Drift Rate	0	%
pDelayResponse → Sync	0	%
mNRR Smoothing	Variable	
Configuration		
Hops	100	
Runs	100,000	

mNRR Smoothing helps a lot when *pDelayInterval* is short and Timestamp-related errors dominate  $RT_{errorRR\_NRR}$ . The short *pDelayInterval* limits  $RT_{errorRR\_CD}$  (which would rise if *pDelay* were increased).

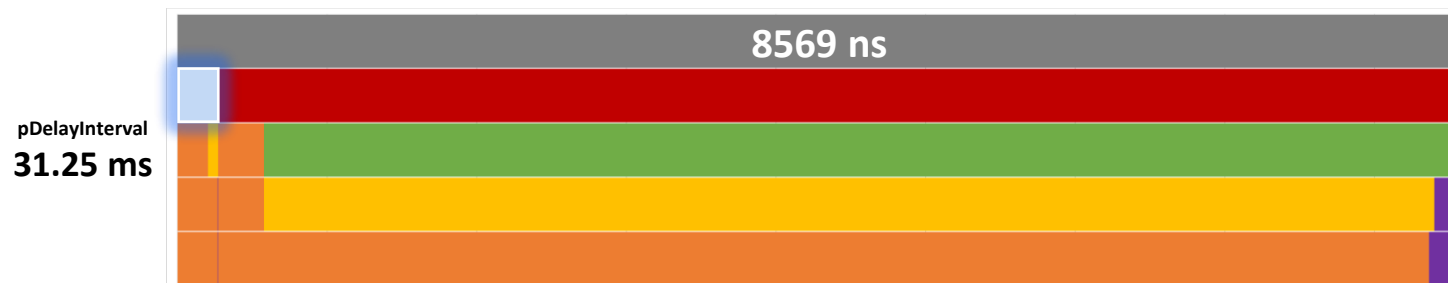
# Different Error Paths – Average Mean Link Delay



If 100% Successful	Remaining DTE	% DTE Removed
-12 ns	6176 ns	0.2%

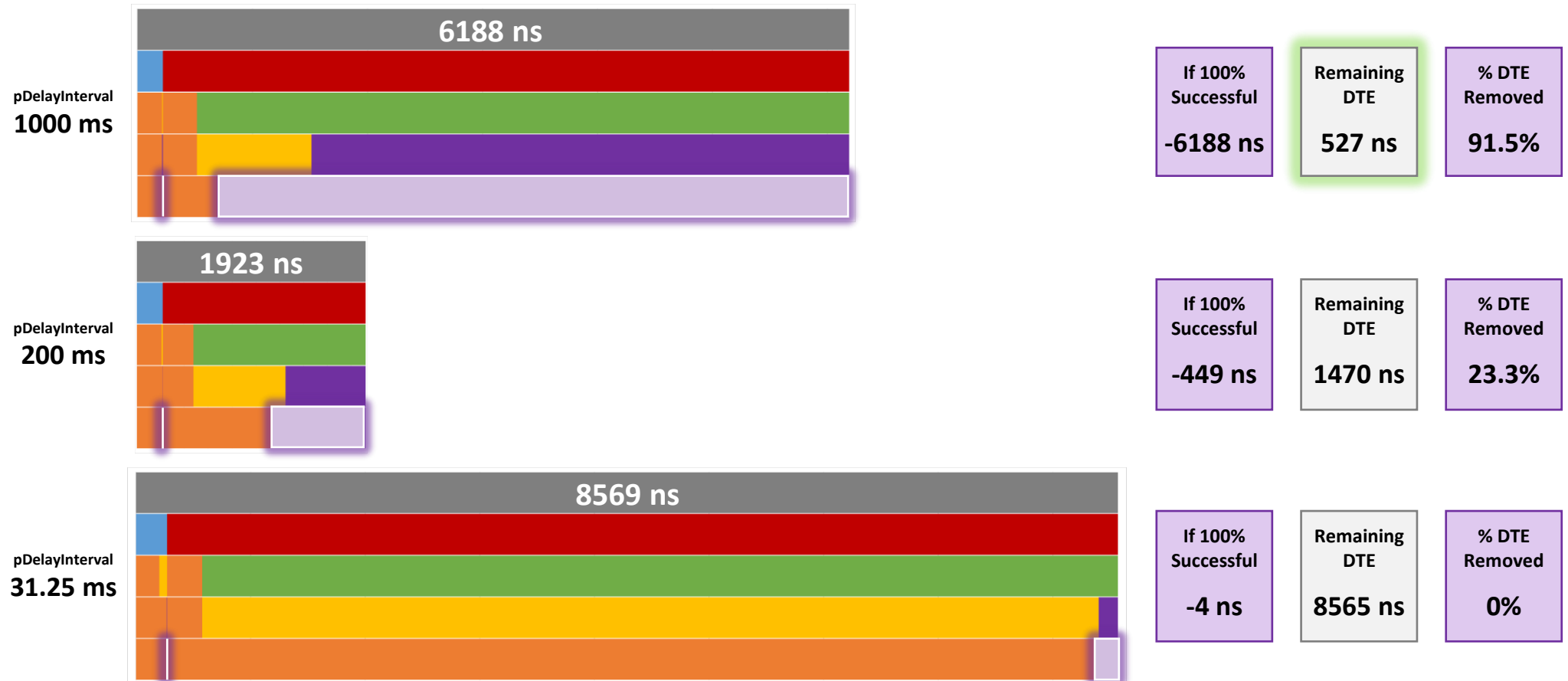


If 100% Successful	Remaining DTE	% DTE Removed
-92 ns	1831 ns	4.8%



If 100% Successful	Remaining DTE	% DTE Removed
-165 ns	8404 ns	1.9%

# Different Error Paths – Compensate for Clock Drift

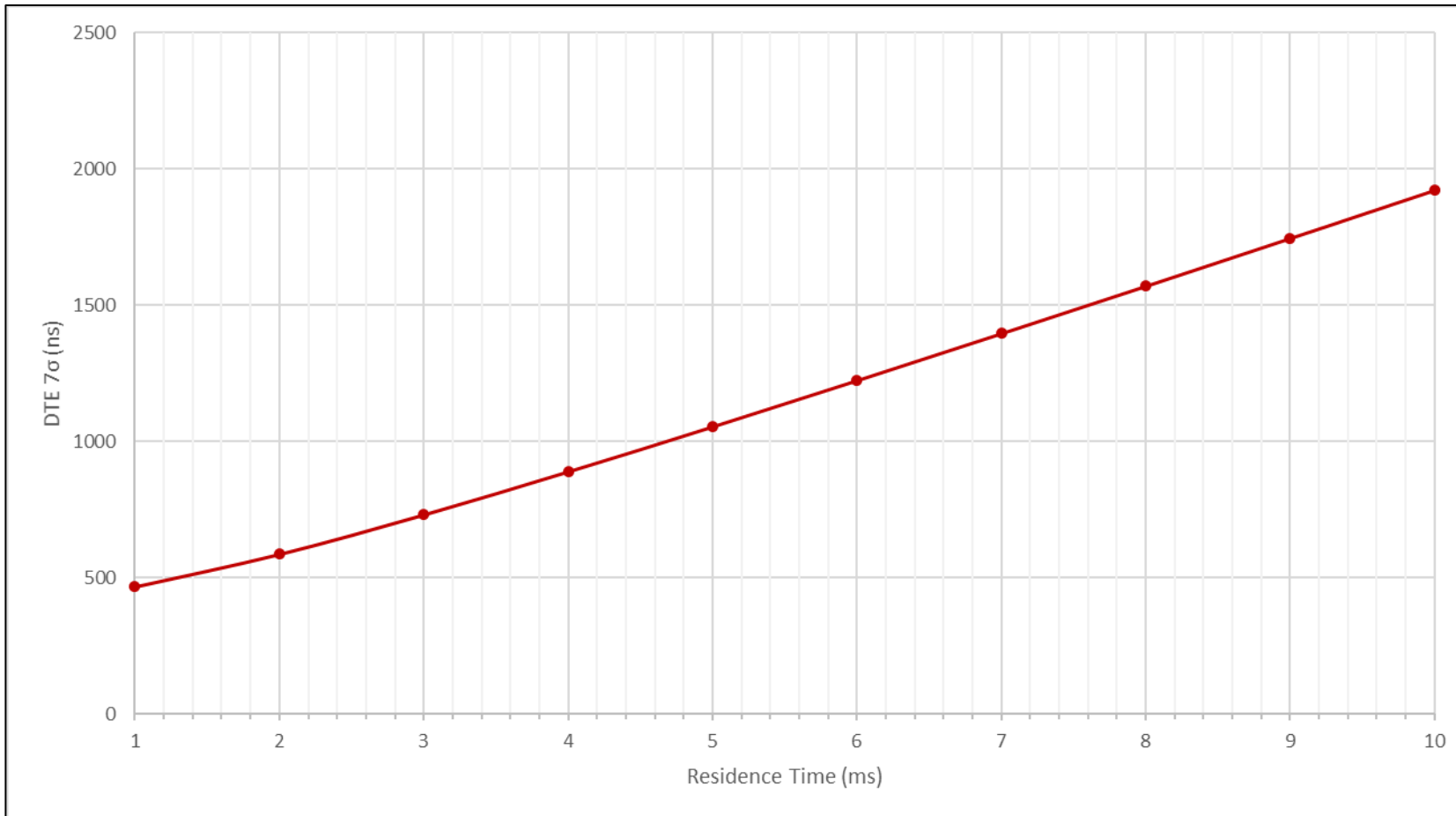


# Approaches to Reducing Dynamic Time Error

Approach	Single Approach 100% Effective Remaining DTE (Variable pDelay Interval)			% Reduction			Likely Best Case Effectiveness	Ease / Cost	Single Approach Likely Effectiveness Remaining DTE			% Reduction		
	1000ms	200ms	31.25ms	1000ms	200ms	31.25ms			1000ms	200ms	31.25ms	1000ms	200ms	31.25ms
	Base DTE - Vary pDelayInterval	6188	1923	8569							Low			
Reduce Timestamp Error	6178	1236	193	0.2%	35.7%	97.7%	50%	High	6183	1580	4381	0.1%	17.9%	48.9%
Reduce Clock Drift - GM Only	5667	1858	8568	8.4%	3.4%	0.0%	98%	High	5677	1859	8568	8.3%	3.3%	0.0%
Reduce Clock Drift - All Nodes	527	1470	8565	91.5%	23.6%	0.0%	98%	High	640	1479	8565	89.7%	23.1%	0.0%
Align pDelay & Sync messaging	1320	1490	8569	78.7%	22.5%	0.0%	98%	High	1417	1499	8569	77.1%	22.1%	0.0%
Reduce Residence Time	395	397	421	93.6%	79.4%	95.1%	90%	Med (High?)	974	550	1236	84.3%	71.4%	85.6%
mNRR Smoothing	6188	1594	922	0.0%	17.1%	89.2%	100%	Low	6188	1594	922	0.0%	17.1%	89.2%
Average Mean Link Delay	6176	1831	8404	0.2%	4.8%	1.9%	98%	Low	6176	1833	8407	0.2%	4.7%	1.9%
Compensate for Clock Drift	527	1470	8565	91.5%	23.6%	0.0%	98%	Low	640	1479	8565	89.7%	23.1%	0.0%

- Compensating for Clock Drift appears to be the only “Low” effort / cost approach that – at least on its own – gets us close to our goal.
- A combination of Reducing Residence Time and Optimising pDelayInterval also gets us close to our goal (Medium or High Ease / Cost)
- Combinations of these with other approaches are also possible.

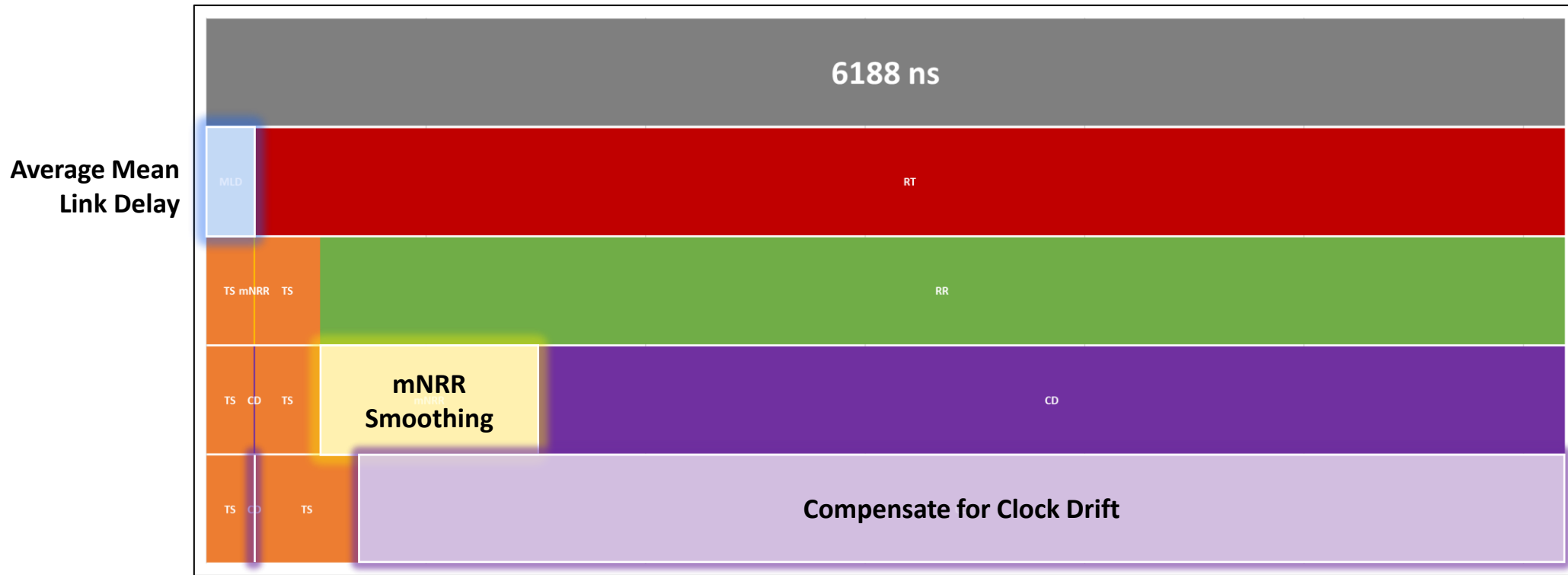
# *residenceTime* Sensitivity – 200 ms pDelay Interval



Input Errors		
GM Clock Drift Max	+0.6	ppm/s
GM Clock Drift Min	+0.6	ppm/s
Clock Drift (non-GM)	0.6	±ppm/s
Timestamp Granularity TX	4	±ns
Timestamp Granularity RX	4	±ns
Dynamic Time Stamp Error TX	4	±ns
Dynamic Time Stamp Error RX	4	±ns
Input Parameters		
pDelay Interval	<b>200</b>	ms
pDelay Response Time	10	ms
residenceTime	<b>Variable</b>	ms
Input Correction Factors		
Mean Link Delay	0	%
Drift Rate	0	%
pDelayResponse → Sync	0	%
mNRR Smoothing	1	
Configuration		
Hops	100	
Runs	100,000	

**A combination of optimising *pDelayInterval* and reducing Residence Time looks like it would require a Residence Time of <3ms to achieve our goal.**

# Combination of Low Effort / Cost Approaches

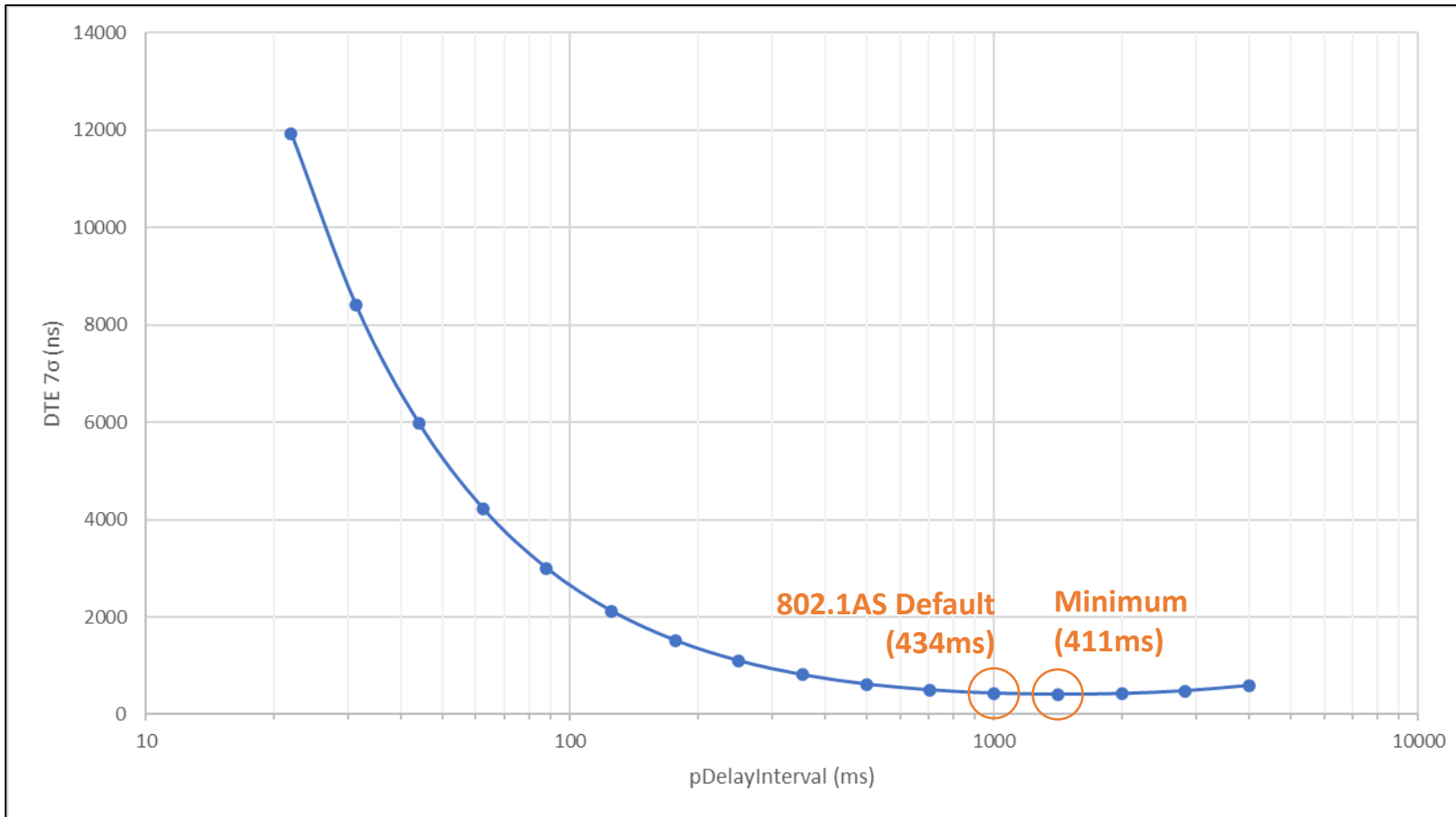


Also optimise pDelayInterval for these parameters & correction factors.

Optimising mNRR Smoothing & pDelayInterval may require some iteration as they affect each other.



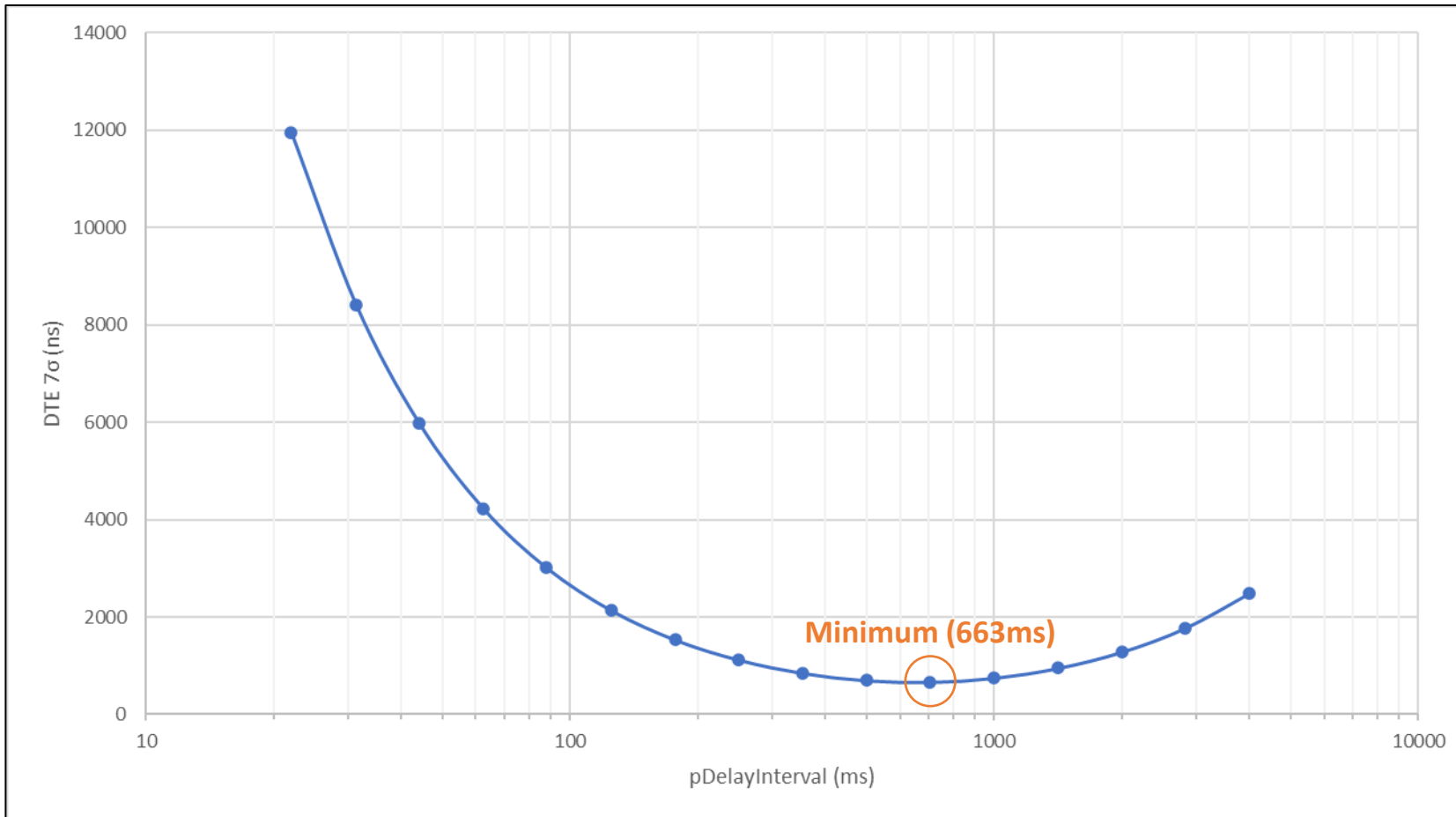
# *pDelayInterval* Sensitivity with Mean Link Delay and Drift Rate Correction Factors 98%



Input Errors		
GM Clock Drift Max	+0.6	ppm/s
GM Clock Drift Min	+0.6	ppm/s
Clock Drift (non-GM)	0.6	±ppm/s
Timestamp Granularity TX	4	±ns
Timestamp Granularity RX	4	±ns
Dynamic Time Stamp Error TX	4	±ns
Dynamic Time Stamp Error RX	4	±ns
Input Parameters		
pDelay Interval	Variable	ms
pDelay Response Time	10	ms
residenceTime	10	ms
Input Correction Factors		
Mean Link Delay	98	%
Drift Rate	98	%
pDelayResponse → Sync	0	%
mNRR Smoothing	1	
Configuration		
Hops	100	
Runs	100,000	

Minimum is at *pDelayInterval* 1.4s and looks like it could meet our goals. 802.1AS default *pDelayInterval* of 1s also looks promising.

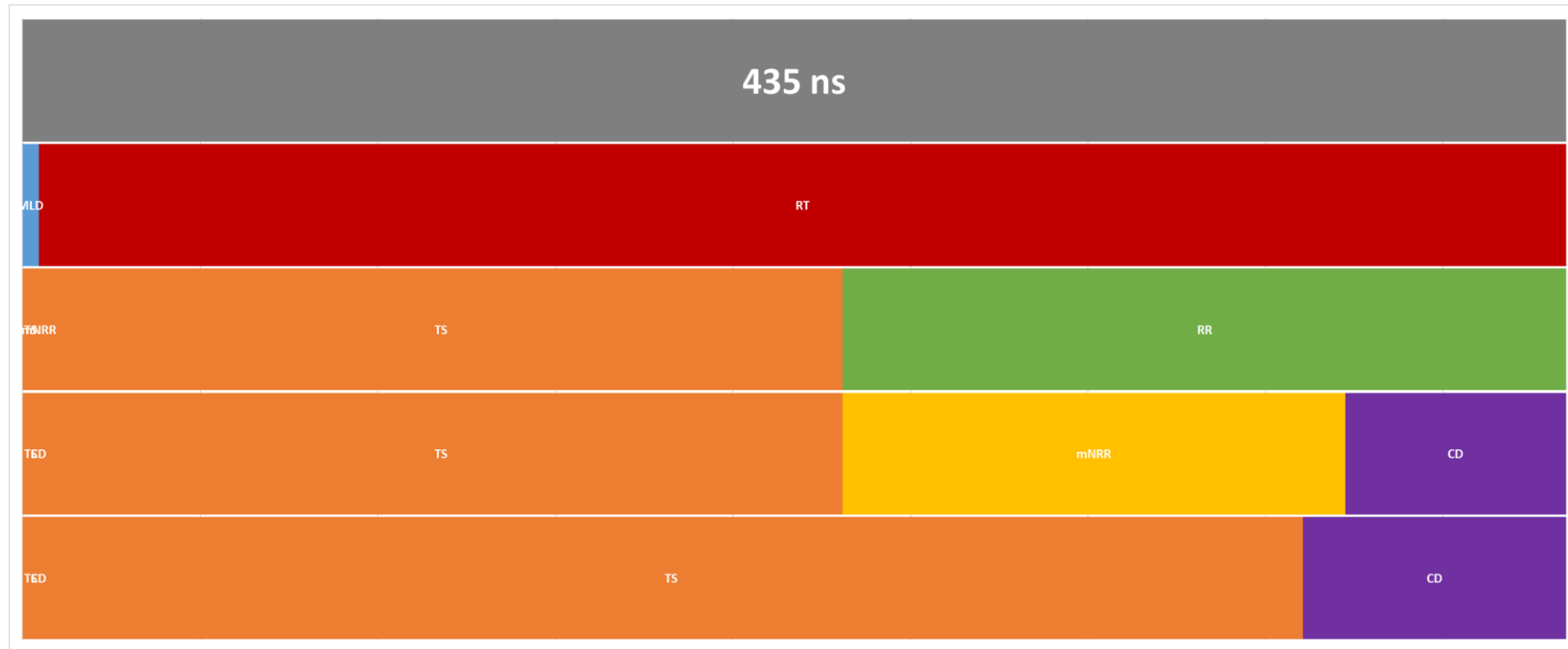
# *pDelayInterval* Sensitivity with Mean Link Delay and Drift Rate Correction Factors 90%



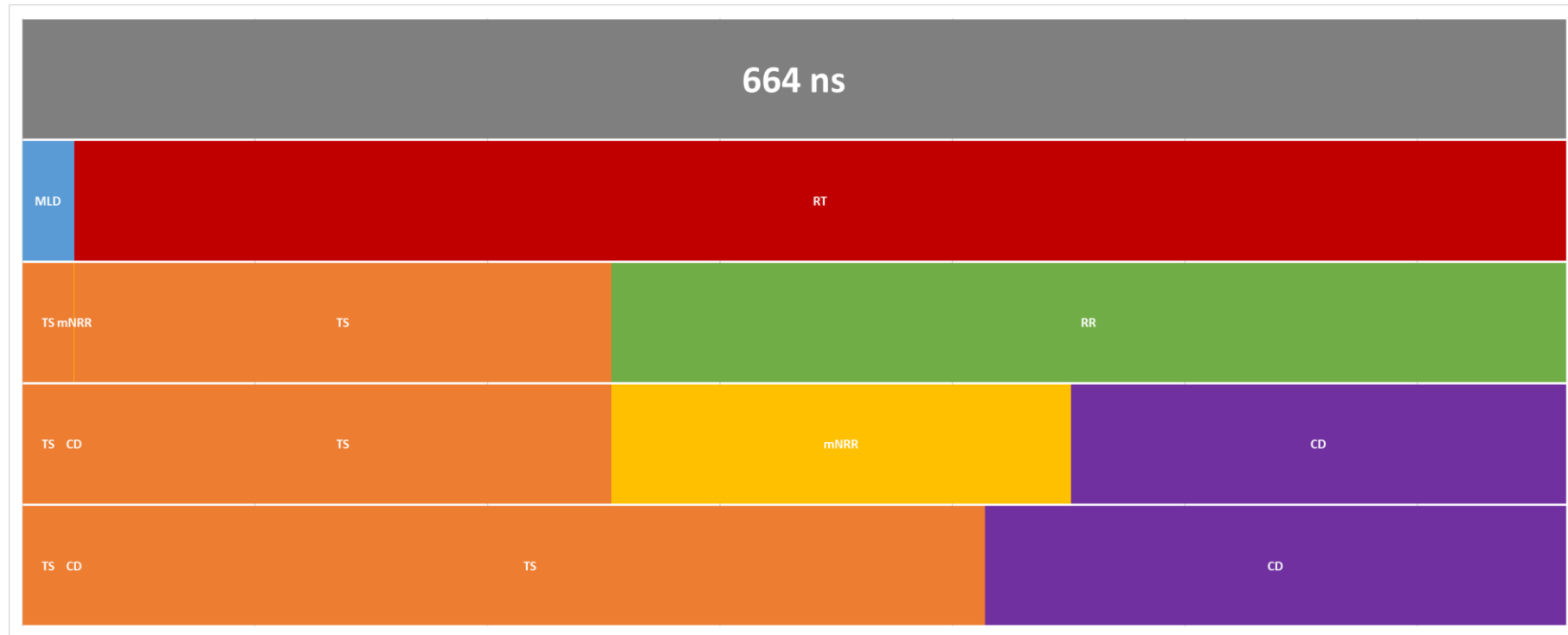
Input Errors		
GM Clock Drift Max	+0.6	ppm/s
GM Clock Drift Min	+0.6	ppm/s
Clock Drift (non-GM)	0.6	±ppm/s
Timestamp Granularity TX	4	±ns
Timestamp Granularity RX	4	±ns
Dynamic Time Stamp Error TX	4	±ns
Dynamic Time Stamp Error RX	4	±ns
Input Parameters		
pDelay Interval	Variable	ms
pDelay Response Time	10	ms
residenceTime	10	ms
Input Correction Factors		
Mean Link Delay	90	%
Drift Rate	90	%
pDelayResponse → Sync	0	%
mNRR Smoothing	1	
Configuration		
Hops	100	
Runs	100,000	

Minimum is at *pDelayInterval* 770ms and looks like it could meet our goals.

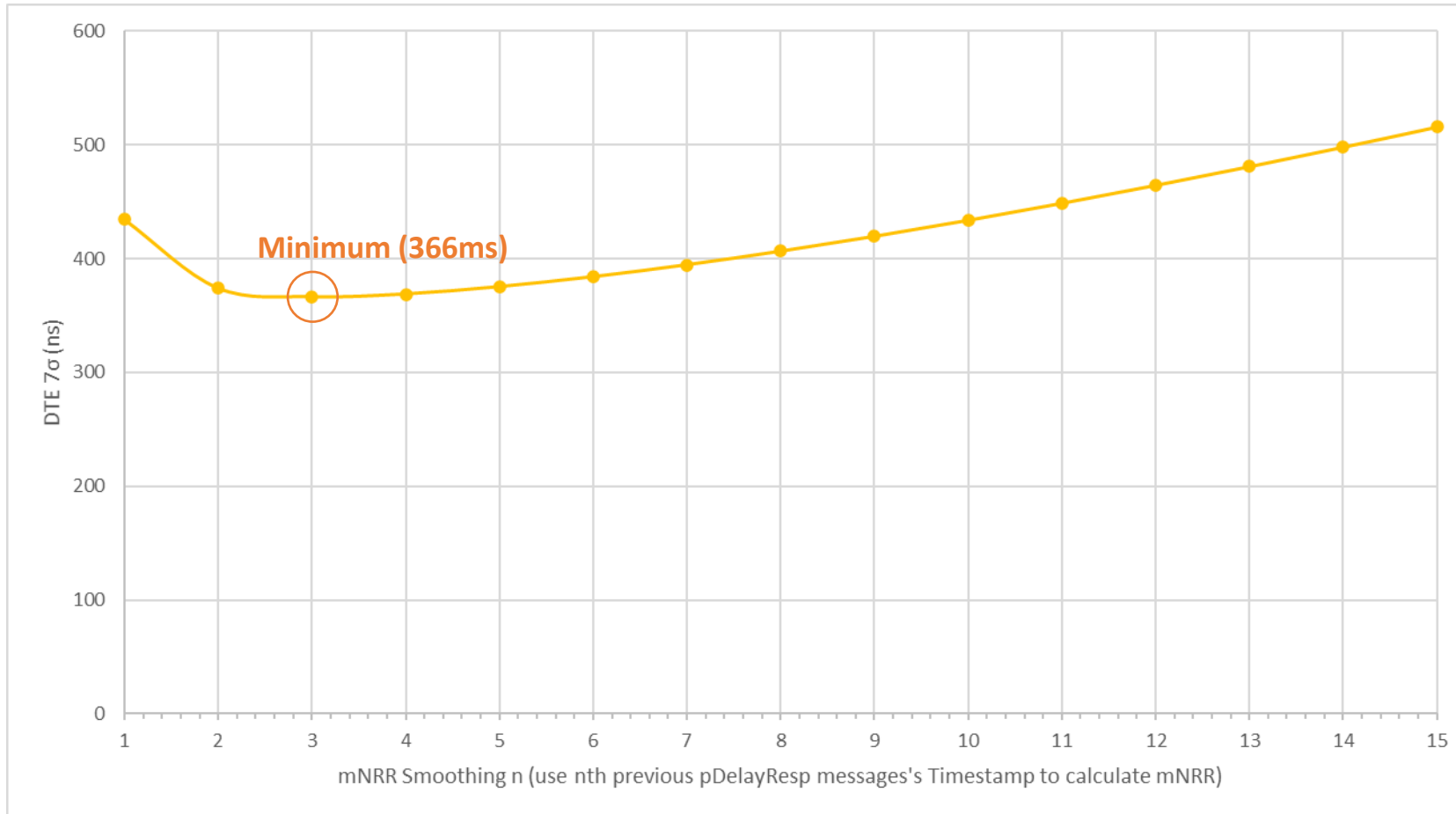
# Error Breakdown – pDelayInterval 1s, MLD & Clock Drift Correction Factors 98%



# Error Breakdown – pDelayInterval 700ms, MLD & Clock Drift Correction Factors 90%



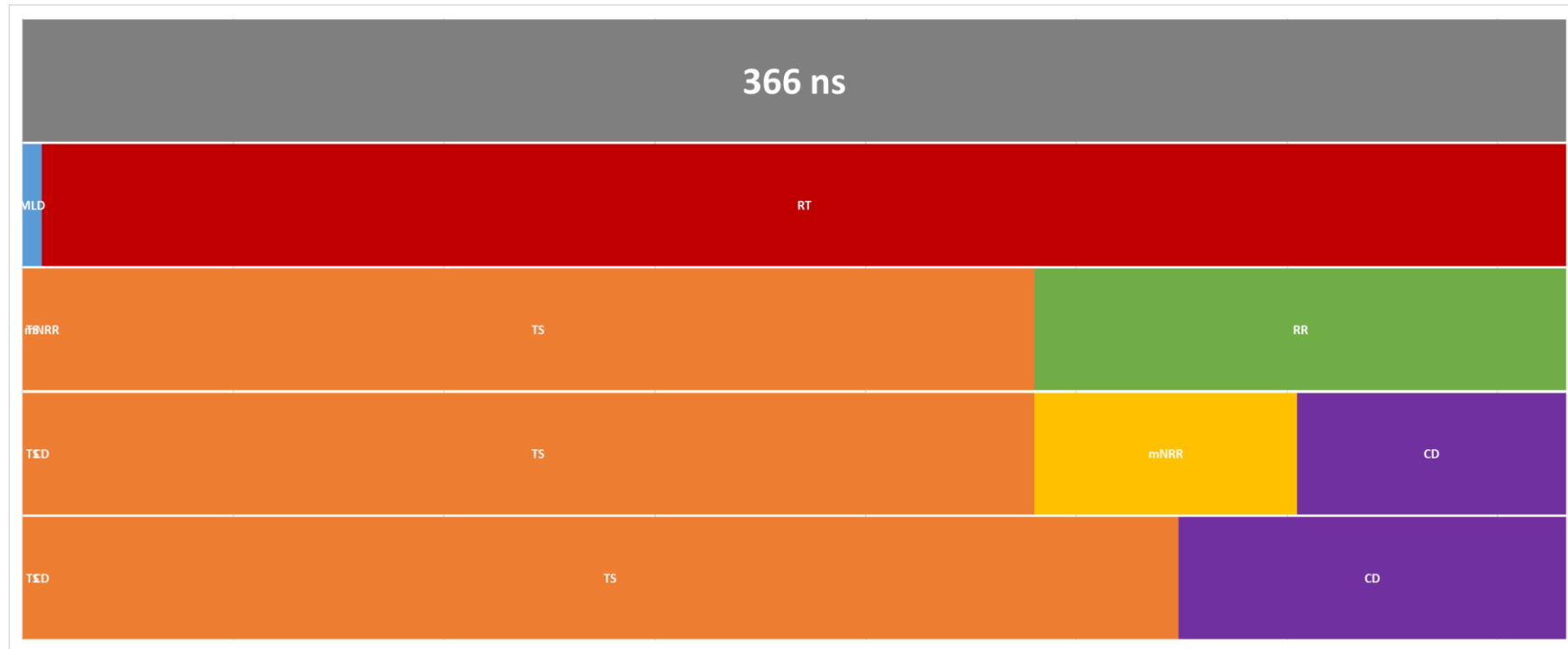
# Effect of mNRR Smoothing – pDelay Interval 1s; MLD & Clock Drift Correction Factors 98%



Input Errors		
GM Clock Drift Max	+0.6	ppm/s
GM Clock Drift Min	-0.6	ppm/s
Clock Drift (non-GM)	0.6	±ppm/s
Timestamp Granularity TX	4	±ns
Timestamp Granularity RX	4	±ns
Dynamic Time Stamp Error TX	4	±ns
Dynamic Time Stamp Error RX	4	±ns
Input Parameters		
pDelay Interval	1000	ms
pDelay Response Time	10	ms
residenceTime	10	ms
Input Correction Factors		
Mean Link Delay	98	%
Drift Rate	98	%
pDelayResponse → Sync	0	%
mNRR Smoothing	Variable	
Configuration		
Hops	100	
Runs	100,000	

**mNRR Smoothing factor of 3 helps reduce DTE further.**

# Error Breakdown – pDelayInterval 700ms, MLD & Clock Drift Correction Factors 90%



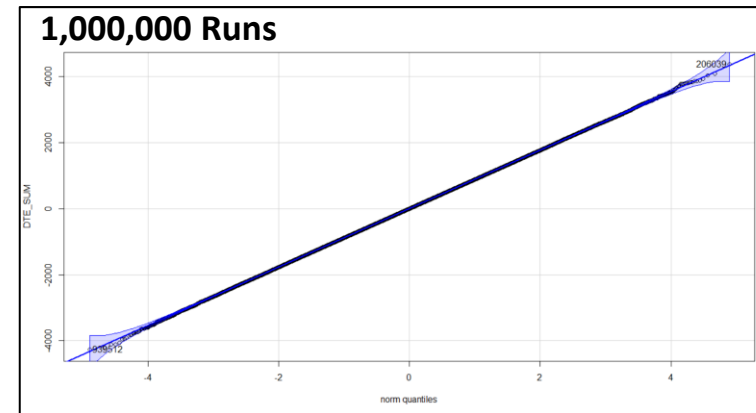
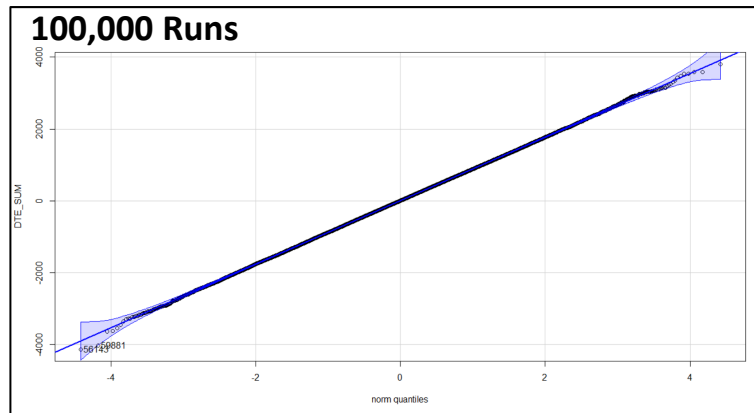
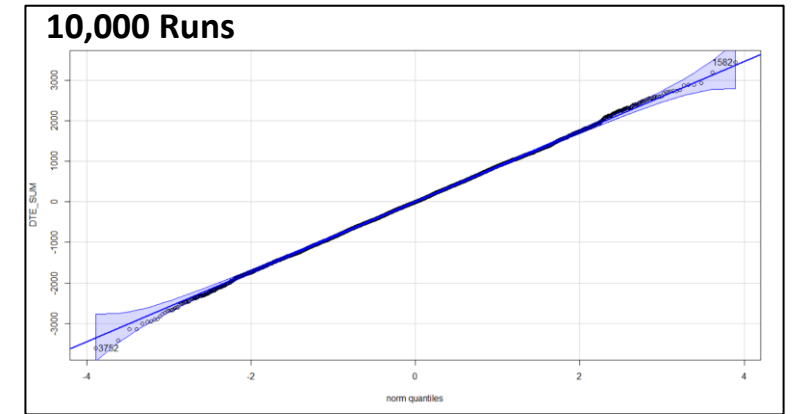
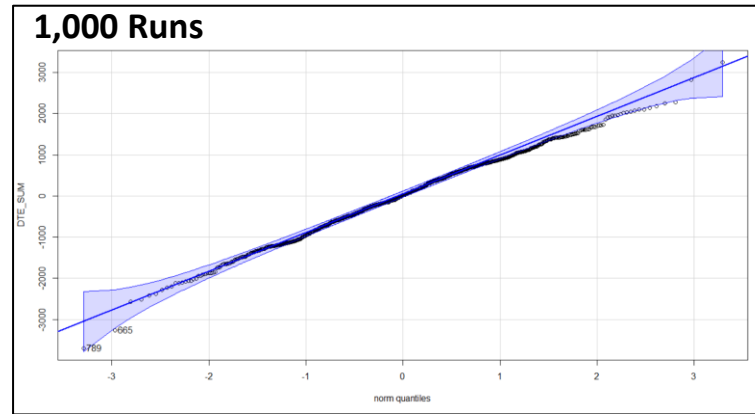
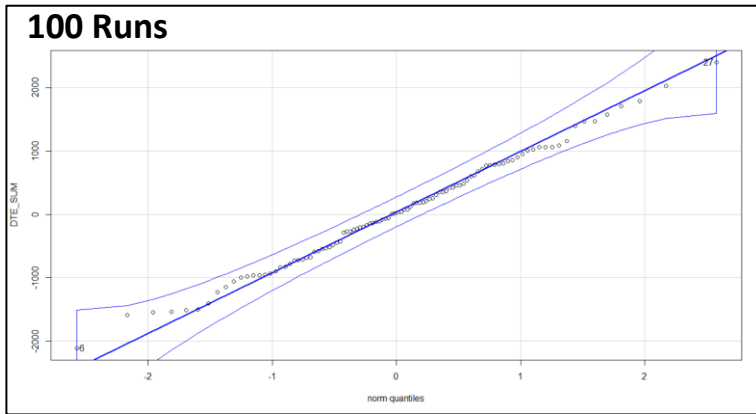
# Recommendation & Next Steps

- Carry out Time Series simulations to validate Monte Carlo Analysis
  - Effect of varying input parameters and sources of error.
  - Effect of applying correction factors
- Focus on averaging Mean Link Delay & Clock Drift Compensation
  - Mean Link Delay averaging should be straightforward, but startup may be an issue.
    - Can only be investigated via Time Series simulation
  - Clock Drift Compensation can be estimated by simply reducing Clock Drift
- I am planning another contribution in December on techniques for compensating for Clock Drift

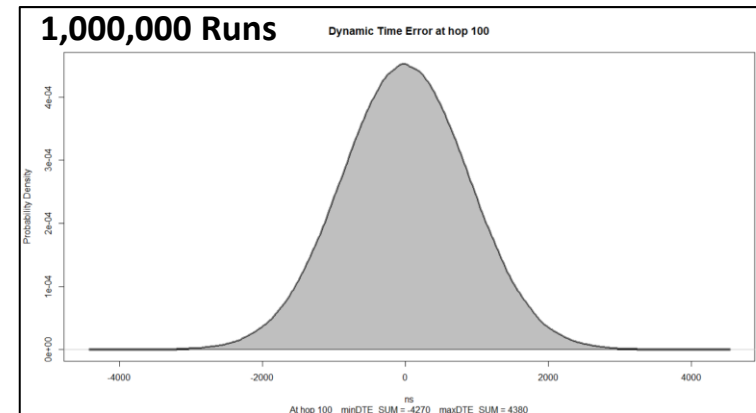
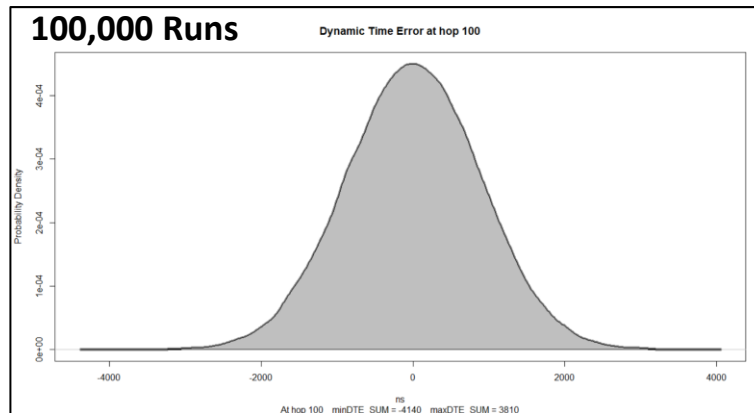
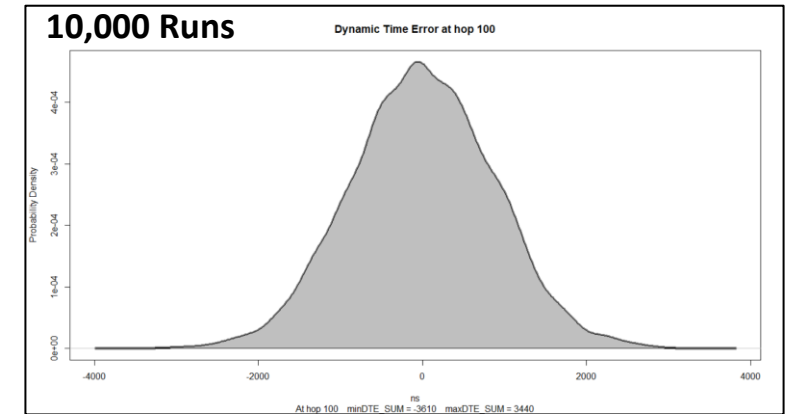
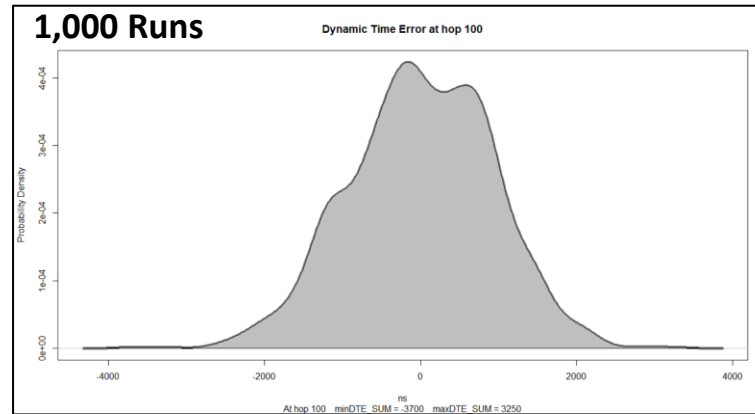
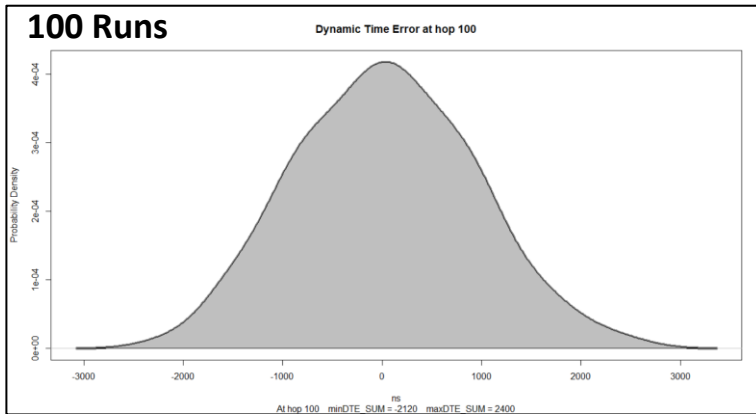
# Backup Material



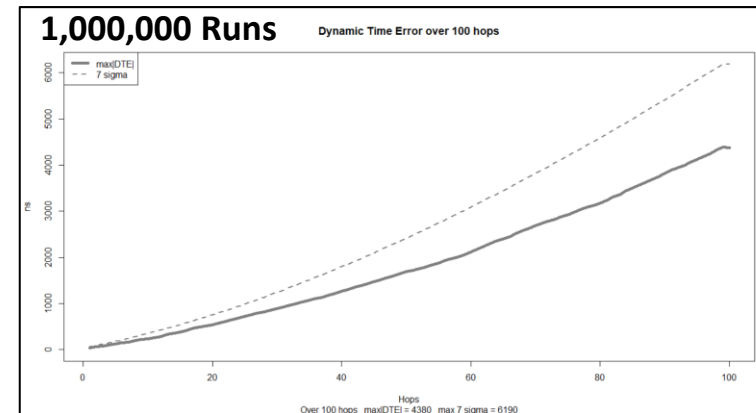
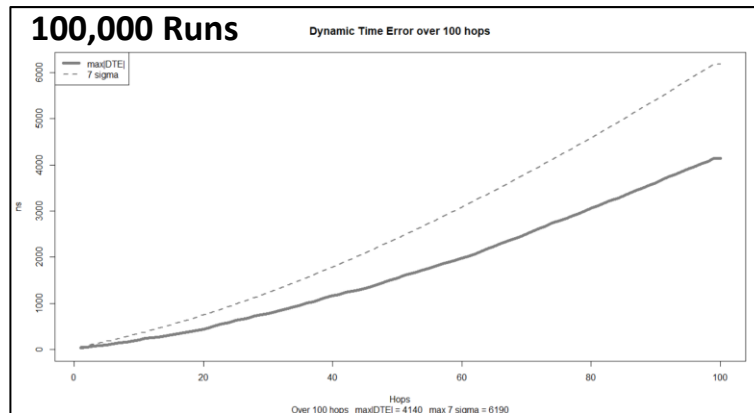
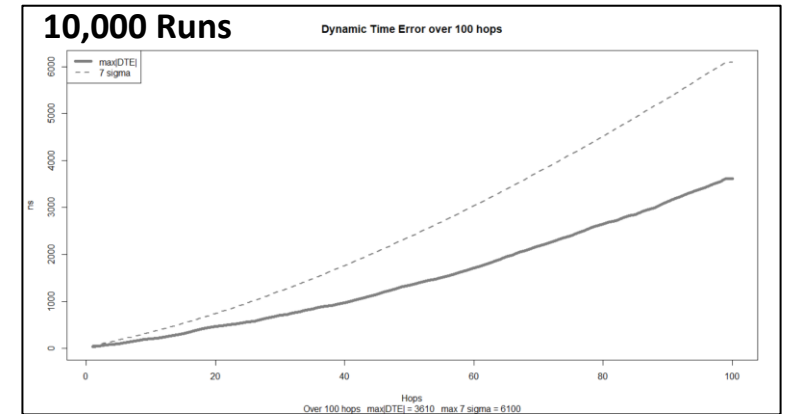
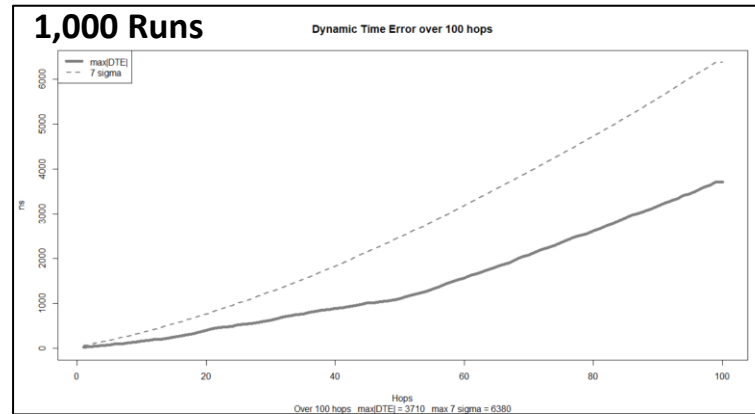
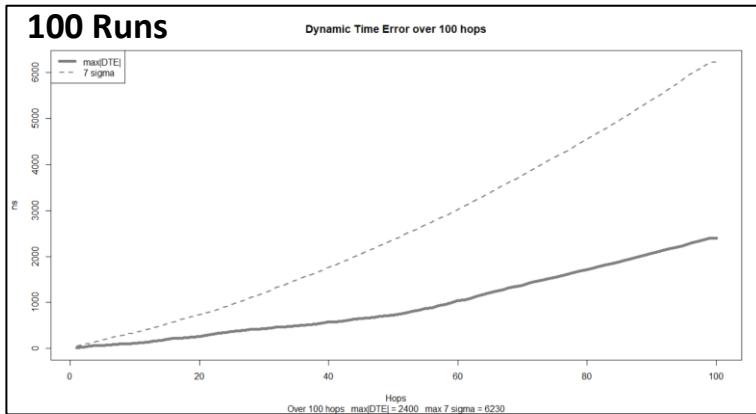
# QQ Plots for Different Numbers of Runs



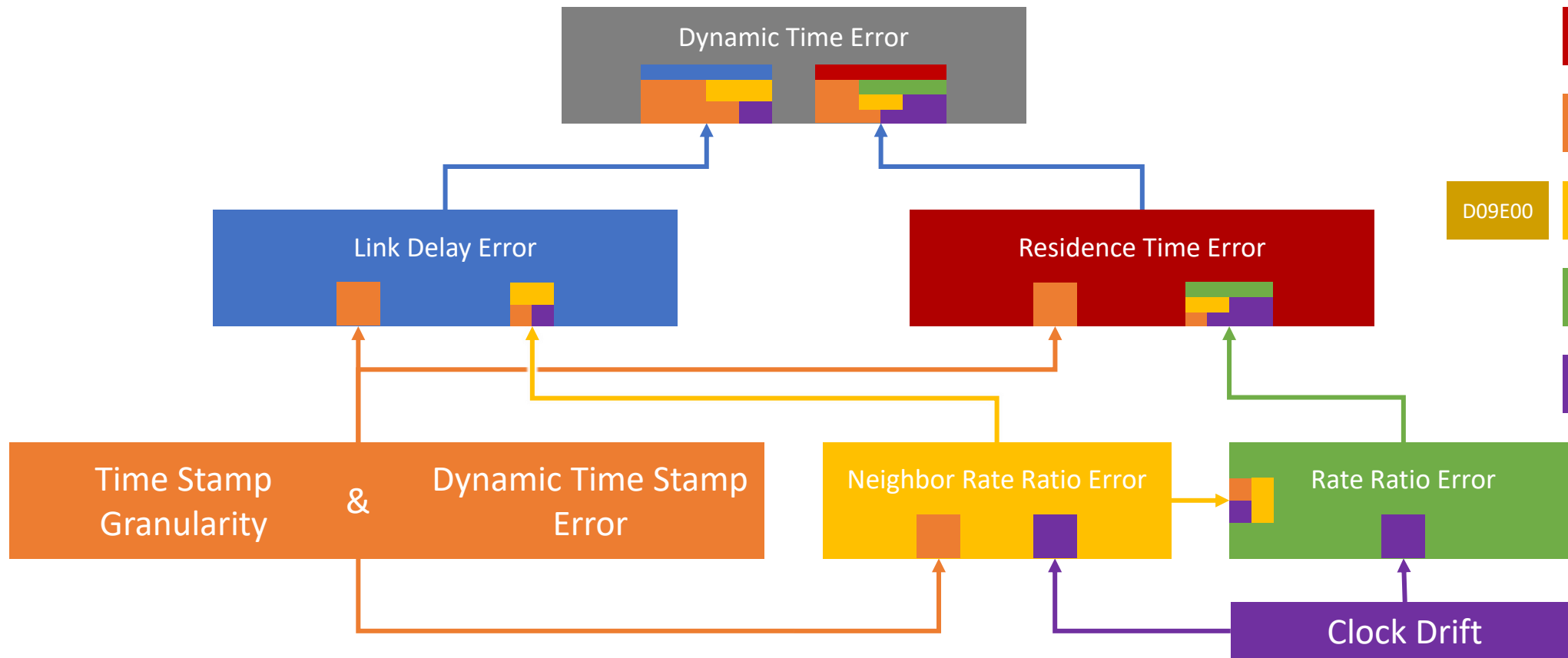
# DTE Probability Density at Hop 100 for Different Numbers of Runs



# max|DTE| & 7 $\sigma$ of DTE Across 100 Hops for Different Numbers of Runs



# Graphics Colour Palette



Lines	Areas	Backgrounds
7F7F7F	BFBFBF	F2F2F2
4472C4	B4C7E7	DAE3F3
C00000	FF8181	FFBDBD
ED7D31	F8CBAD	FBE5D6
D09E00	FFC000	FFE699
70AD47	C5E0B4	E2F0D9
7030A0	C198E0	DFC9EF